

# Fast algorithm for approximating the inner and the outer boundaries of the iris

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# Problem

## Problem

Describe and implement a fast algorithm that determines the inner and the outer boundaries of the iris in the image of the eye.

## Applications

- Biometrics
- Medicine

## Basic algorithm

- Iris border detection using a method of paired gradients  
*Y. S. Efimov, I. A. Matveev, 2015*

## Related to this paper

- Use of the Hough transformation to detect lines and curves in pictures  
*R. O. Duda, P. E. Hart, 1972*
- Learning using privileged information  
*R. Neychev, 2018*

# Data description

## Input data

Monochromatic raster graphic image  $\mathbf{I}_0$  size of  $W \times H$ , obtained by photographing wide-open eye located approximately on the optical axis.

## Output data

The radiuses and the coordinates of the centers of the circles approximating the inner and the outer borders of the iris:

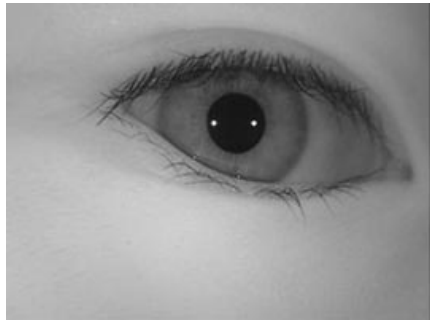
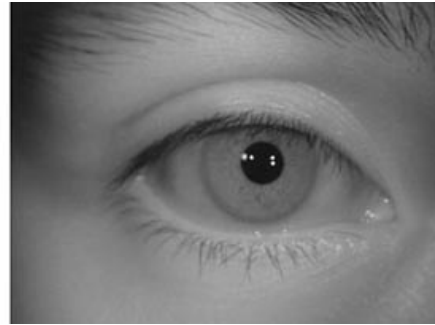
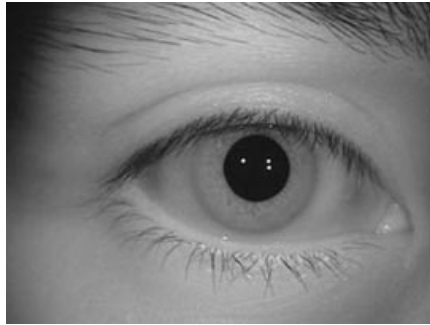
$$\{i_{\text{iris}}, j_{\text{iris}}, r_{\text{iris}}\}, \{i_{\text{pupil}}, j_{\text{pupil}}, r_{\text{pupil}}\}$$

## Expert data

True parameters are provided by an expert for each image:

$$\{\tilde{i}_{\text{iris}}, \tilde{j}_{\text{iris}}, \tilde{r}_{\text{iris}}\}, \{\tilde{i}_{\text{pupil}}, \tilde{j}_{\text{pupil}}, \tilde{r}_{\text{pupil}}\}$$

# Input data example



# Quality criterion

## Absolute error

The maximum deviation from expert values among all parameters:

$$\Delta := \max\{|\tilde{i}_{\text{iris}} - i_{\text{iris}}|, |\tilde{j}_{\text{iris}} - j_{\text{iris}}|, |\tilde{r}_{\text{iris}} - r_{\text{iris}}|, \\ |\tilde{i}_{\text{pupil}} - i_{\text{pupil}}|, |\tilde{j}_{\text{pupil}} - j_{\text{pupil}}|, |\tilde{r}_{\text{pupil}} - r_{\text{pupil}}|\}$$

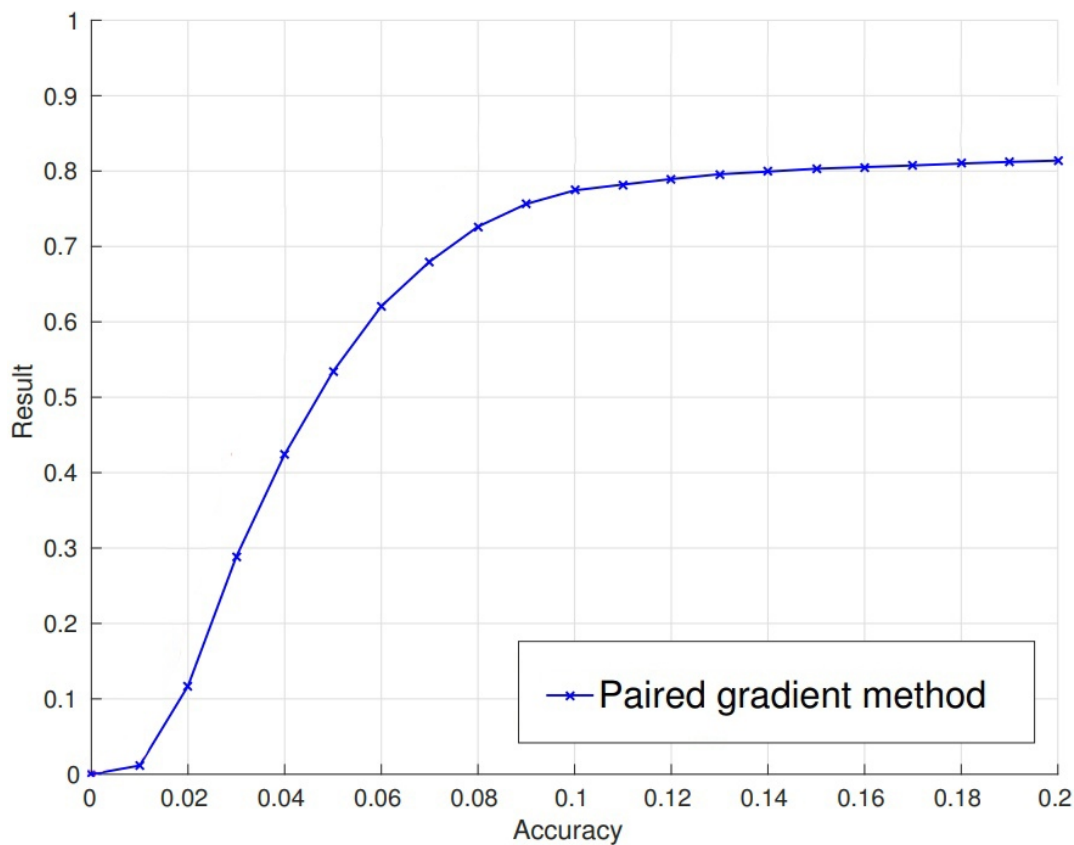
## Relative error

The ratio of the absolute error to the outer circle's radius:  $\varepsilon := \frac{\Delta}{\tilde{r}_{\text{iris}}}$

## Quality

The percentage of images on which the absolute error does not exceed the threshold  $\delta$  set by the expert.

# Basic algorithm results



# Algorithm flowchart



Figure 1: Algorithm stages



# Space transformation

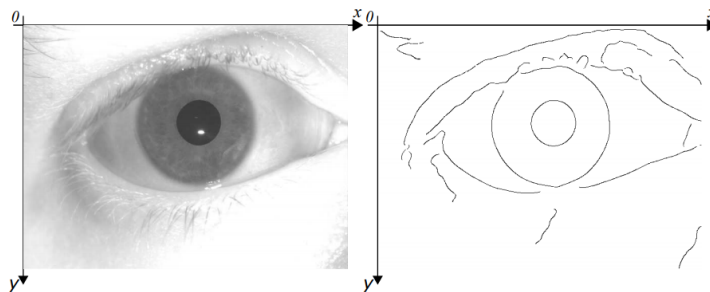


Figure 2: Detection of boundary points

Let  $\rho(i, j) \rightarrow \{0, 1\}$  be the result of the binarization stage.

Consider the following space transformation  $T : \mathbb{R}^2 \rightarrow \mathbb{R}^5$ :  
 $T(x, y) \triangleq (x^2, x, y^2, y, 1)$ .

Let  $\mathcal{X}$  be the result of transformation  $T$  applied to the boundary points:  $\mathcal{X} = \{T(i, j) : \rho(i, j) = 1\}$ .

# Multimodel optimization problem

Let  $\mathbf{w}_j = (x_j^2, x_j, y_j^2, y_j, 1)$ ,  $j = 1, 2$  denote the approximating circles.

Let  $\pi_{j, \mathbf{z}_i}$  be the indicator of point  $\mathbf{z}_i$  belonging to class  $j$ .

The classes are:

- 1. The inner boundary
- 2. The outer boundary
- 3. Noise, which is assumed to be normally distributed

## Multimodel optimization problem

$$\mathbf{w}_1, \mathbf{w}_2 = \operatorname{argmin}_{\mathbf{w}_1, \mathbf{w}_2} \sum_{\mathbf{z}_i \in \mathcal{X}} \pi_{1,i} \left( \mathbf{z}_i^\top \mathbf{w}_1 \right)^2 + \pi_{2,i} \left( \mathbf{z}_i^\top \mathbf{w}_2 \right)^2 + \pi_{3,i} \frac{(z_i - \mathbf{Ez})^2}{\operatorname{Varz}}$$

# Summary