### Formula 1

#### Alessandro Tenaglia

Machine and Reinforcement Learning in Control Applications

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#### **Problem**



Learn to follow a track.

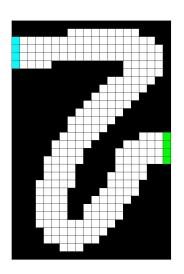
### Problem



Learn to follow a track.

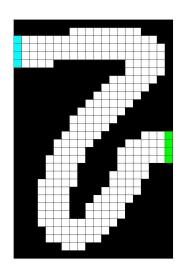
#### Problem formulation

- The car starts from the starting line (cyan);
- The car must reach the finish line (green);
- The goal is to find the shortest path to the finish line;



#### Problem formulation

- The car can move in 8 directions:N, S, E, W, NE, NW, SE, SW;
- Reward:
  - $\bullet \ -dist \ {\rm for \ each \ step}$
  - $\bullet$   $-10^6$  for hitting the boundary



#### Model

- The **state** is the position of the car in the track
  - ullet we have  $X\cdot Y$  states.
- The action is the direction along which the car moves
  - we have 8 actions.

# Planning: Dynamic Programming

- Model the problem as an MDP;
- Compute the transition matrix **P**;
- Compute the reward matrix R;
- Find the optimal policy  $\pi_{\star}$  using **Dynamic Programming** method (PI or VI).

## Learning: Monte Carlo

- Model-free: no knowledge of MDP transitions and rewards;
- Simulate episodes:

$$S_0, A_0, R_0, S_1, A_1, R_1 \dots, S_T, A_T, R_T$$

• Use experience to estimate  $q_{\star}$ :

$$\pi_{\star}(s) = \arg\max_{a} q_{\star}(s, a)$$

## Assignment #3

- Learn to play Blackjack.
  - The goal is to obtain cards whose sum is the closest to 21;
  - All face cards count as 10, an ace counts as 1 or as 11;
  - Player start with two cards;
  - Dealer starts with two cards, one face up and one face down;
  - The player can request additional cards (hit) or stop (stick);
  - The dealer plays according to a fixed strategy:
    - Stick on any sum of 17 or greater, and hit otherwise.
  - If the player exceeds 21, he goes burst an loses the game.
  - If the dealer goes burst, the player wins; otherwise, the outcome is determined by whose final sum is closer to 21;
  - Reward:
    - $\bullet$  +1 for winning;
    - -1 for losing;
  - Do not discount ( $\gamma = 1$ ).
  - Find the best strategy based on the player's cards and the dealer's face-up card.