

File created: 1-Jan-99 21:45:52 {DSK}<disk>disk3>lispcore3.0>sources>LLBIGNUM.;2

changes to: (FNS \INITBIGNUMS)

previous date: 19-Jan-93 10:44:45 {DSK}<disk>disk3>lispcore3.0>sources>LLBIGNUM.;1

Read Table: INTERLISP

Package: INTERLISP

Format: XCCS

::
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```
(RPAQQ LLBIGNUMCOMS
  [(COMS (DECLARE%: EVAL@COMPILE DONTCOPY (RECORDS BIGNUM))
    (INITRECORDS BIGNUM)
    (CONSTANTS \BIGNUM.THETA (\BIGNUM.BETA (EXPT 2 14))
      (\BIGNUM.BETA1 (SUB1 \BIGNUM.BETA)))
    [DECLARE%: EVAL@COMPILE (ADDVARS (CHARACTERNAMES (INFINITY 8551)
      (ADDVARS (GLOBALVARS MIN.INTEGER MAX.INTEGER \BIG.0 \BIG.1)))
      ; entries
    (FNS \BIGNUM.COMPARE \BIGNUM.DIFFERENCE \BIGNUM.INTEGERLENGTH \BIGNUM.LOGAND \BIGNUM.LOGOR
      \BIGNUM.LOGXOR \BIGNUM.PLUS \BIGNUM.LSH \BIGNUM.TIMES \BIGNUM.QUOTIENT \BIGNUM.REMAINDER
      \BIGNUM.TO.FLOAT)
    (FNS FINITEP INFINITEP))
    (COMS ; internal functions
      (FNS \BIGNUM.TO.INT \BN.2TH \BN.ABS \BN.DIFFERENCE \BN.DIVIDE \BN.FLOAT \BN.IGNN BIGNUM.DEFPRINT
        \BN.INTEGERLENGTH \BN.LOGAND \BN.LOGANDC2 \BN.LOGOR \BN.LOGXOR \BN.MINUS \BN.PLUS2 \BN.SIGN
        \BN.TIMES2 \BN.COMPAREN \BN.D2TH \BN.FROM.FIXP \BN.ICANON \BN.IDIVIDE \BN.ISUM0 \BN.ISUM1
        \BN.MADD \BN.TO.FIXP \BN.NZEROS \BN.QRS \BN.SIGN \BN.TH2B \BN.TH2D))
      (COMS (FNS \INITBIGNUMS)
        ; MAKERATIONAL needs work
        ; needs work: MASK.1'S MASK.0'S BITTEST BITSET BITCLEAR LOGNOT LOADBYTE DEPOSITBYTE IMODLESSP IMODPLUS
        ; IMODDIFFERENCE ROT
        (DECLARE%: DONTEVAL@LOAD DOCOPY (P (\INITBIGNUMS]))

(DECLARE%: EVAL@COMPILE DONTCOPY

(DECLARE%: EVAL@COMPILE

[DATATYPE BIGNUM (ELEMENTS)
  (INIT (DEFPRINT 'BIGNUM 'BIGNUM.DEFPRINT)
)

(/DECLAREDATATYPE 'BIGNUM ' (POINTER)
  ;; ---field descriptor list elided by lister---
  '2)

(DEFPRINT 'BIGNUM 'BIGNUM.DEFPRINT)
)

(/DECLAREDATATYPE 'BIGNUM ' (POINTER)
  ;; ---field descriptor list elided by lister---
  '2)

(DEFPRINT 'BIGNUM 'BIGNUM.DEFPRINT)

(DECLARE%: EVAL@COMPILE

(RPAQQ \BIGNUM.THETA 10000)

(RPAQ \BIGNUM.BETA (EXPT 2 14))

(RPAQ \BIGNUM.BETA1 (SUB1 \BIGNUM.BETA))

(CONSTANTS \BIGNUM.THETA (\BIGNUM.BETA (EXPT 2 14))
  (\BIGNUM.BETA1 (SUB1 \BIGNUM.BETA)))
)

(DECLARE%: EVAL@COMPILE

(ADDTOVAR CHARACTERNAMES (INFINITY 8551))
)

(ADDTOVAR GLOBALVARS MIN.INTEGER MAX.INTEGER \BIG.0 \BIG.1)

;; entries

(DEFINEQ

(\BIGNUM.COMPARE
```

```
[LAMBDA (X Y)
  (COND
    ((EQ X MIN.INTEGER)
      (COND
        ((EQ Y MIN.INTEGER)
          0)
        (T -1)))
    ((EQ X MAX.INTEGER)
      (COND
        ((EQ Y MAX.INTEGER)
          0)
        (T 1)))
    ((EQ Y MIN.INTEGER)
      1)
    ((EQ Y MAX.INTEGER)
      -1)
    (T (\BN.COMPARE (\BN.FROM.FIXP X)
                    (\BN.FROM.FIXP Y)))
```

(* Imm "15-Apr-85 17:36")

(\BIGNUM.DIFFERENCE

```
[LAMBDA (X Y)
  (\BN.TO.FIXP (\BN.DIFFERENCE (\BN.FROM.FIXP X)
                                (\BN.FROM.FIXP Y)))
```

(* Imm "12-Apr-85 08:38")

(\BIGNUM.INTEGERLENGTH

```
[LAMBDA (X)
  (\BN.INTEGERLENGTH (\BN.FROM.FIXP X])
```

(* Imm "12-Apr-85 08:01")

(\BIGNUM.LOGAND

```
[LAMBDA (X Y)
  (COND
    ((OR (EQ X 0)
         (EQ Y 0))
      0)
    ((OR (\INFINITEP X)
         (\INFINITEP Y))
      (ERROR "Can't do logical operations with infinity"))
    [(LESSP Y 0)
     (COND
       [(LESSP X 0)
        (DIFFERENCE -1 (LOGOR (LOGNOT X)
                              (LOGNOT Y))
          (T (\BN.TO.FIXP (\BN.LOGANDC2 (\BN.FROM.FIXP X)
                                         (\BN.FROM.FIXP (DIFFERENCE -1 Y])
          ((LESSP X 0)
           (\BIGNUM.LOGAND Y X))
          (T (\BN.TO.FIXP (\BN.LOGAND (\BN.FROM.FIXP X)
                                         (\BN.FROM.FIXP Y]))
```

(* kbr%: "16-Sep-86 12:28")

(\BIGNUM.LOGOR

```
[LAMBDA (X Y)
  (COND
    ((EQ X 0)
      Y)
    ((EQ Y 0)
      X)
    ((OR (\INFINITEP X)
         (\INFINITEP Y))
      (ERROR "Can't do logical operations with infinity"))
    [(AND (GREATERP X 0)
          (GREATERP Y 0))
     (\BN.TO.FIXP (\BN.LOGOR (\BN.FROM.FIXP X)
                              (\BN.FROM.FIXP Y])
    (T
      (* stupid slow but maybe working definition. Problem is that logors of negatives are difficult in current representation)

      (DIFFERENCE -1 (LOGAND (DIFFERENCE -1 X)
                              (DIFFERENCE -1 Y]))
```

(* kbr%: "16-Sep-86 12:29")

(\BIGNUM.LOGXOR

```
[LAMBDA (X Y)
  (COND
    ((EQ X 0)
      Y)
    ((EQ Y 0)
      X)
    ((OR (\INFINITEP X)
         (\INFINITEP Y))
      (ERROR "Can't do logical operations with infinity"))
    [(LESSP X 0)
     (COND
       [(LESSP Y 0)
```

(* kbr%: "16-Sep-86 12:29")

```

      (LOGXOR (DIFFERENCE -1 X)
              (DIFFERENCE -1 Y)))
    (T
      (\BIGNUM.DIFFERENCE (\BIGNUM.LOGOR X Y)
                          (\BIGNUM.LOGAND X Y]
      ((LESSP Y 0)
       (\BIGNUM.LOGXOR Y X))
    (T (\BN.TO.FIXP (\BN.LOGXOR (\BN.FROM.FIXP X)
                                (\BN.FROM.FIXP Y]))

```

(* stupid dumb but working definition)

(\BIGNUM.PLUS

```

[LAMBDA (X Y)
  (\BN.TO.FIXP (\BN.PLUS2 (\BN.FROM.FIXP X)
                          (\BN.FROM.FIXP Y]))

```

(* Imm "12-Apr-85 08:03")

(\BIGNUM.LSH

```

[LAMBDA (X N)
  (COND
    ((EQ X 0)
     0)
    ((EQ N MIN.INTEGER)
     (COND
       ((INFINITEP X)
        (ERROR "Can't shift infinity minus infinity places"))
       (T 0)))
    ((INFINITEP X)
     X)
    ((EQ N MAX.INTEGER)
     (COND
       ((EQ X 0)
        0)
       ((IGREATERP X 0)
        MAX.INTEGER)
       (T MIN.INTEGER)))
    [ (IGE Q N 0)
      (SETQ X (\BN.FROM.FIXP X))
      [if (>= N 14)
        then (while (>= N 14) do (SETQ N (IDIFFERENCE N 14))
                        (SETQ X (CONS 0 X]
        (\BN.TO.FIXP (\BN.TIMES2 X (\BN.FROM.FIXP (EXPT 2 N]
      (IGREATERP X 0)
      (SETQ X (\BN.FROM.FIXP X))
      [if (<= N -14)
        then (while (<= N -14) do (SETQ N (IPLUS N 14))
                        (SETQ X (CDR X]
        (\BIGNUM.QUOTIENT (create BIGNUM
                                ELEMENTS _ X)
                          (EXPT 2 (IMINUS N]
      (T ;; RIGHTSHIFT A NEGATIVE - result must be adjusted if not a bignum
        (SETQ X (MINUS (\BIGNUM.LSH (MINUS X)
                                    N)))
        (if (NOT (type? BIGNUM X))
            then (SETQ X (SUB1 X)))
        X])

```

; Edited 23-Feb-87 16:09 by jrb:

; Don't smash original input

; Don't smash original input

(\BIGNUM.TIMES

```

[LAMBDA (X Y)
  (\BN.TO.FIXP (\BN.TIMES2 (\BN.FROM.FIXP X)
                          (\BN.FROM.FIXP Y]))

```

(* Imm "12-Apr-85 08:03")

(\BIGNUM.QUOTIENT

```

[LAMBDA (X Y)
  (COND
    ((EQ Y MAX.INTEGER)
     (COND
       ((INFINITEP X)
        (ERROR "Can't divide infinity by infinity"))
       (T 0)))
    ((EQ Y MIN.INTEGER)
     (COND
       ((INFINITEP X)
        (ERROR "Can't divide infinity by infinity"))
       (T 0)))
    ((EQ X MAX.INTEGER)
     (COND
       ((EQ Y 0)
        (ERROR "Can't divide infinity by 0"))
       ((IGREATERP Y 0)
        MAX.INTEGER)
       (T MIN.INTEGER)))
    ((EQ X MIN.INTEGER)
     (COND

```

(* kbr%: "16-Sep-86 12:30")

```

      ((EQ Y 0)
       (ERROR "Can't divide infinity by 0"))
      ((IGREATERP Y 0)
       MIN.INTEGER)
      (T MAX.INTEGER)))
      (T (\BN.TO.FIXP (CAR (\BN.DIVIDE (\BN.FROM.FIXP X)
                                         (\BN.FROM.FIXP Y))

```

(\BIGNUM.REMAINDER

```

[LAMBDA (X Y)
  (COND
    ((OR (\INFINITEP X)
          (\INFINITEP Y))
     (ERROR "Can't take remainder with infinity"))
    (T (\BN.TO.FIXP (CDR (\BN.DIVIDE (\BN.FROM.FIXP X)
                                         (\BN.FROM.FIXP Y))

```

(* kbr%: "16-Sep-86 12:30")

(\BIGNUM.TO.FLOAT

```

[LAMBDA (X)
  (\BN.FLOAT (\BN.FROM.FIXP X])

```

(* Imm "12-Apr-85 08:06")
(* called by \FLOAT)

)

(DEFINEQ

(\FINITEP

```

[LAMBDA (CL:NUMBER)
  (NOT (OR (EQ CL:NUMBER MAX.INTEGER)
            (EQ CL:NUMBER MIN.INTEGER))

```

(* kbr%: "16-Sep-86 12:24")

(\INFINITEP

```

[LAMBDA (CL:NUMBER)
  (OR (EQ CL:NUMBER MAX.INTEGER)
      (EQ CL:NUMBER MIN.INTEGER))

```

(* kbr%: "16-Sep-86 12:25")

)

;; internal functions

(DEFINEQ

(\BIGNUM.TO.INT

```

[LAMBDA (X)
  (COND
    ((NULL (CDR X))
     (CAR X))
    (T (IPLUS (CAR X)
               (ITIMES \BIGNUM.BETA (\BIGNUM.TO.INT (CDR X))

```

(* Imm "9-Jan-86 15:30")

(\BN.2TH

```

[LAMBDA (A)
  (PROG (L B)
    [while A do (PROGN (SETQ L (\BN.QRS A \BIGNUM.THETA))
                       (SETQ A (CAR L))
                       (SETQ B (CONS (CDR L)
                                      B])
    (RETURN B])

```

(* Imm "9-Jan-86 15:31")

(\BN.ABS

```

[LAMBDA (U)
  (COND
    ((ILESSP (\BN.SIGN U)
              0)
     (\BN.MINUS U))
    (T U])

```

(* Imm "20-JUL-84 02:00")

(\BN.DIFFERENCE

```

[LAMBDA (U V)
  (\BN.PLUS2 U (\BN.MINUS V])

```

(* Imm "20-JUL-84 01:33")

(\BN.DIVIDE

```

[LAMBDA (A B FLG)
  (PROG (M N K SA ST C D W E F B1 B2 A1 A2 A3 QHAT C1 R1 R2 U V Q X IP BIP L1 L2)
    [COND
      ((OR (NULL A)
            (NULL B))
       (RETURN (CONS \BIG.0 A])
      (COND
        ((CDR B)

```

(* Imm "9-Jan-86 15:33")

[illegible]

```

      (SETQ C1 (CAR IP))
      [COND
        ((ILESSP A1 0)
          (PROGN (SETQ A1 (IPLUS A1 \BIGNUM.BETA))
                 (SETQ C1 (IDIFFERENCE C1 1])
          (SETQ C1 (IPLUS C1 E))
          (RPLACA U A1)
          (SETQ X U)
          (SETQ U (CDR U))
          (COND
            (V (GO L14)))
          (SETQ A1 (IPLUS (CAR U)
                          C1))
          (SETQ U (CDR U))
          (RPLACD X \BIG.0)
          (COND
            ((EQ A1 0)
              (GO L17)))
          (SETQ U (CAR L1))
          (SETQ V B)
          (SETQ C1 0)
          (SETQ QHAT (IDIFFERENCE QHAT 1))
L16 (SETQ A1 (CAR U))
      (SETQ B1 (CAR V))
      (SETQ V (CDR V))
      (SETQ IP (\BN.IDIVIDE (IPLUS C1 (IPLUS A1 B1))
                             \BIGNUM.BETA))
      (RPLACA U (CDR IP))
      (SETQ U (CDR U))
      (COND
        (V (GO L16)))
L17 [COND
      ((OR (NEQ QHAT 0)
           Q)
        (SETQ Q (CONS (ITIMES W QHAT)
                       Q])
      (SETQ L1 (CDR L1))
      (SETQ U (CAR L2))
      (SETQ L2 (CDR L2))
      (COND
        (L1 (GO L10)))
      (RETURN (CONS Q (AND (NEQ FLG 'QUOTIENT)
                           (CAR (\BN.QRS A (ITIMES SA D]))

```

(\BN.FLOAT

[LAMBDA (X)

(* kbr%: "16-Sep-86 12:21")

```

      (COND
        ((NULL X)
          0.0)
        [(LISTP X)
          (FPLUS (CAR X)
                  (FTIMES \BIGNUM.BETA (\BN.FLOAT (CDR X]
        ((OR (EQ X 'MAX.INTEGER)
              (EQ X 'MIN.INTEGER))

```

(* KBR%: After some consideration, I've decided that it would be best that rational infinities and floating point infinities be kept distinct in the same way that we consider 1 distinct from 1.0.

This is an admission that the systems of Lisp rationals and Lisp floating point numbers are two disjoint sets of Lisp expressions. The semantics of these expressions--what they denote--is slightly more than the rational numbers we attach to them. These expressions should be viewed as denoting a pair consisting of a rational number and an atom recording the type of the expression. A Lisp rational X denotes the pair (X CL:RATIONAL) and a Lisp floating point number X denotes (X FLOAT) in our mind. The FLOAT operation is an injection that changes an expression denoting a pair (X CL:RATIONAL) into an expression denoting a pair (X FLOAT)%.

Arithmetic on these expressions is typed arithmetic with rounding of the results in the case of FLOATPs according to IEEE spec. Let's suppose that MAX.INTEGER and MAX.FLOAT are Lisp expressions denoting the respective rational and floating point infinities. (We now know with the advent of Common Lisp that MAX.INTEGER and MIN.INTEGER should have been called MAX.RATIONAL and MIN.RATIONAL) Then rules of floating point coercion can continue to make sense%:

(EQL (/ MAX.INTEGER) 0) (EQL (/ MAX.FLOAT) 0.0) (EQL (EXPT 2 MAX.INTEGER) MAX.INTEGER)

(EQL (EXPT 2.0 MAX.INTEGER) MAX.FLOAT) (EQL (EXPT 2 MAX.FLOAT) MAX.FLOAT)

(EQL (EXPT 2.0 MAX.FLOAT) MAX.FLOAT) etc. But if we tried to make rational infinities and floating point infinities

identical, then we would have to arbitrarily decide in an unnatural way whether

(EQL (/ MAX.INTEGER) 0) or (EQL (/ MAX.FLOAT) 0.0) is true, etc.

Recommendation%: Currently Xerox Lisp does not support floating point infinities.

Larry Masinter added rational infinities. If there is a desire to add floating point infinities at some point in the future, then I recommend that rational and floating point infinities be kept distinct.

*)

(* * Error because Xerox Lisp does not support floating point infinities
(at this time)%.*)

```

      (ERROR "Can't float integer infinity.")
      (T (SHOULDNT])

```

(\BN.IGNN

[LAMBDA (U)

(* Imm "9-Jan-86 15:30")

```

(COND
  ((NULL U)
   NIL)
  ((ILESSP U \BIGNUM.BETA)
   (LIST U))
  (T (PROG (Y)
        (SETQ Y (IQUOTIENT U \BIGNUM.BETA))
        (SETQ U (IDIFFERENCE U (ITIMES Y \BIGNUM.BETA)))
        (RETURN (CONS U (\BN.FROM.FIXP Y)))))

```

(BIGNUM.DEFPRINT

```

[LAMBDA (BIGN STREAM)
  (COND
    [(INFINITEP BIGN)
     (* kbr%: "16-Sep-86 12:31")
     (* Distinguished integers smaller/larger than any others.
       Print using "evaluate at read time" syntax)
     (CONS (CONCAT (CHARACTER (fetch (READTABLEP HASHMACROCHAR) of *READTABLE*))
            ".")
            (COND
              ((EQ BIGN MIN.INTEGER)
               'MIN.INTEGER)
              (T 'MAX.INTEGER)
              (T (LET* ((RADIX (\CHECKRADIX *PRINT-BASE*))
                        [TH (SELECTQ RADIX
                                   (10 10000)
                                   (8 4096)
                                   (bind (TH _ RADIX)
                                         NEWTH while (LEQ (SETQ NEWTH (TIMES TH RADIX))
                                                             \BIGNUM.BETA)
                                         do (SETQ TH NEWTH) finally (RETURN TH)
                                         (CHARS (\BN.TH2D (bind (ELS _ (fetch (BIGNUM.ELEMENTS) of BIGN))
                                                             L B while ELS do (SETQ L (\BN.QRS ELS TH))
                                                             (SETQ ELS (CAR L))
                                                             (SETQ B (CONS (CDR L)
                                                             B))
                                                             finally (RETURN B))
                                                             RADIX TH))
              (COND
                (*PRINT-RADIX*
                 (COND
                   ((AND (EQ RADIX 8)
                        (NOT (fetch (READTABLEP COMMONLISP) of *READTABLE*)))
                    (NCONC1 CHARS (CHARCODE Q)))
                   (T [push CHARS (SELECTQ RADIX
                                           (8 (CHARCODE o))
                                           (16 (CHARCODE x))
                                           (2 (CHARCODE b))
                                           (PROGN (push CHARS (CHARCODE r))
                                                  [COND
                                                    ((IGEQ RADIX 10)
                                                     (push CHARS (IPLUS (CHARCODE 0)
                                                                           (IMOD RADIX 10)))
                                                    (SETQ RADIX (IQUOTIENT RADIX 10)
                                                     (IPLUS RADIX (CHARCODE 0)
                                                     (push CHARS (fetch (READTABLEP HASHMACROCHAR) of *READTABLE*))
                                                     (.SPACECHECK. STREAM (LENGTH CHARS))
                                                     (for C in CHARS do (\OUTCHAR STREAM C))
                                                     T])
                                                  (* Return T to show we have done it ourselves)
                ]))

```

(\BN.INTEGERLENGTH

```

[LAMBDA (X)
  (COND
    ((NULL X)
     0)
    [(LISTP X)
     (COND
       [(CDR X)
        (IPLUS (CONSTANT (INTEGERLENGTH (SUB1 \BIGNUM.BETA)))
                (\BN.INTEGERLENGTH (CDR X))
        (T (INTEGERLENGTH (CAR X))
        ((INFINITEP X)
         MAX.INTEGER)
        (T (SHOULDNT])

```

(\BN.LOGAND

```

[LAMBDA (B1 B2)
  (COND
    ((NULL B1)
     NIL)
    ((NULL B2)
     NIL)
    (T (PROG (B)
              (SETQ B (\BN.LOGAND (CDR B1)
                                   (CDR B2)))
              (SETQ B1 (LOGAND (CAR B1)

```

```

                (CAR B2)))
(COND
  ((AND (NULL B)
        (EQ B1 0))
    (RETURN B)))
(RETURN (CONS B1 B])

```

(\BN.LOGANDC2

(* Imm "14-May-86 10:47")

```

[LAMBDA (B1 B2)
  (COND
    ((NULL B1)
     NIL)
    ((NULL B2)
     B1)
    (T (PROG (B)
              (SETQ B (\BN.LOGANDC2 (CDR B1)
                                     (CDR B2)))
              [SETQ B1 (LOGAND (CAR B1)
                               (DIFFERENCE -1 (CAR B2])
              (COND
                ((AND (NULL B)
                      (EQ B1 0))
                 (RETURN B)))
              (RETURN (CONS B1 B])

```

(\BN.LOGOR

(* Imm "21-JUL-84 23:57")

```

[LAMBDA (B1 B2)
  (COND
    ((NULL B1)
     B2)
    ((NULL B2)
     B1)
    (T (CONS (LOGOR (CAR B1)
                    (CAR B2))
              (\BN.LOGOR (CDR B1)
                         (CDR B2]))

```

(\BN.LOGXOR

(* Imm "21-JUL-84 23:59")

```

[LAMBDA (B1 B2)
  (COND
    ((NULL B1)
     B2)
    ((NULL B2)
     B1)
    (T (CONS (LOGXOR (CAR B1)
                    (CAR B2))
              (\BN.LOGXOR (CDR B1)
                         (CDR B2]))

```

(\BN.MINUS

(* kbr%: "11-Sep-86 15:00")

```

[LAMBDA (U)
  (COND
    ((NULL U)
     NIL)
    [(LISTP U)
     (CONS (IMINUS (CAR U))
            (\BN.MINUS (CDR U))
     ((EQ U 'MAX.INTEGER)
      'MIN.INTEGER)
     ((EQ U 'MIN.INTEGER)
      'MAX.INTEGER)
     (T (SHOULDNT]))

```

(\BN.PLUS2

(* kbr%: "11-Sep-86 15:26")

```

[LAMBDA (U V)
  (COND
    ((NULL U)
     V)
    ((NULL V)
     U)
    [(AND (LISTP U)
          (LISTP V))
     (PROG (L)
            (SETQ L (IDIFFERENCE (FLENGTH U)
                                (FLENGTH V)))
            [COND
              [(ILESSP L 0)
               (SETQ U (APPEND U (\BN.NZEROS (IDIFFERENCE 0 L))
                                (IGREATERP L 0))
               (SETQ V (APPEND V (\BN.NZEROS L])
              (RETURN (COND
                        ((EQ (\BN.SIGN U)

```



```

                (\BN.SIGN V))
            (\BN.ISUM0 U V))
            (T (\BN.ISUM1 U V])
    ((EQ U 'MAX.INTEGER)
     (COND
      ((EQ V 'MIN.INTEGER)
       (ERROR "Can't add plus infinity to minus infinity"))
      (T U)))
    ((EQ U 'MIN.INTEGER)
     (COND
      ((EQ V 'MAX.INTEGER)
       (ERROR "Can't add plus infinity to minus infinity"))
      (T U)))
    (T V])

```

(\BN.SIGN

(* kbr%: "11-Sep-86 15:22")

```

[LAMBDA (U)
  (COND
   [(ATOM U)
    (COND
     ((NULL U)
      0)
     ((EQ U 'MAX.INTEGER)
      1)
     ((EQ U 'MIN.INTEGER)
      -1)
     (T (SHOULDNT]
    ((IGREATERP (CAR U)
     0)
    1)
    ((ILESSP (CAR U)
     0)
    -1)
    (T (\BN.SIGN (CDR U))

```

(\BN.TIMES2

(* kbr%: "11-Sep-86 15:19")

```

[LAMBDA (U V)
  (PROG (TAIL U1 W W1 W2 L C AP BP)
    [COND
     [(NULL U)
      (COND
       ((OR (EQ V 'MAX.INTEGER)
            (EQ V 'MIN.INTEGER))
        (ERROR "Can't multiply infinity and zero.")]
       (T (RETURN NIL]
     [(EQ U 'MAX.INTEGER)
      (COND
       ((NULL V)
        (ERROR "Can't multiply infinity and zero.")]
       ((EQ (\BN.SIGN V)
        1)
        (RETURN U))
       (T (RETURN 'MIN.INTEGER]
     ((EQ U 'MIN.INTEGER)
      (COND
       ((NULL V)
        (ERROR "Can't multiply infinity and zero.")]
       ((EQ (\BN.SIGN V)
        1)
        (RETURN U))
       (T (RETURN 'MAX.INTEGER]
     (SETQ TAIL (LIST 0 0))
     (SETQ L (IPLUS (FLENGTH U)
                    (IDIFFERENCE (FLENGTH V)
                                   2)))
     (SETQ W TAIL)
     (for I from 1 to L do (SETQ W (CONS 0 W)))
     (SETQ W1 W)
A   (SETQ U1 U)
     (SETQ W2 W1)
     (SETQ C 0)
B   (SETQ AP (\BN.IDIVIDE (ITIMES (CAR U1)
                                   (CAR V))
                          \BIGNUM.BETA))
     (SETQ BP (\BN.IDIVIDE (IPLUS (CAR W2)
                                   (IPLUS (CDR AP)
                                           C))
                          \BIGNUM.BETA))
     (RPLACA W2 (CDR BP))
     (SETQ C (IPLUS (CAR AP)
                    (CAR BP)))
     (SETQ W2 (CDR W2))
     (SETQ U1 (CDR U1))
     (COND
      (U1 (GO B)))

```

```

(RPLACA W2 C)
(SETQ W1 (CDR W1))
(SETQ V (CDR V))
(COND
  (V (GO A)))
(COND
  ((EQ C 0)
   (RPLACD TAIL NIL)))
(RETURN W])

```

(\BN.COMPAREN

(* Imm "12-Apr-85 08:33")

```

[LAMBDA (U V)
  (PROG ((SU 0)
         (SV 0)
         (ST 0)
         (S 0))
    [COND
      [(EQ (SETQ SU (\BN.SIGN U))
            0)
       (RETURN (IMINUS (\BN.SIGN V)
                        (EQ (SETQ SV (\BN.SIGN V))
                            0)
                        (RETURN SU))
              (NEQ (SETQ S (IDIFFERENCE SU SV))
                    0)
              (RETURN (COND
                        ((IGREATERP S 0)
                         1)
                        ((ILESSP S 0)
                         -1)
                        (T (SHOULDNT))
                        ))
              ))]
      A (COND
          ((NEQ (SETQ ST (IDIFFERENCE (CAR U)
                                       (CAR V)))
                0)
           (SETQ S ST)))
          (SETQ V (CDR V))
          (SETQ U (CDR U))
          (COND
            [(NULL U)
             (RETURN (COND
                       (V (IMINUS SU))
                       (T (COND
                           ((IGREATERP S 0)
                            1)
                           ((ILESSP S 0)
                            -1)
                           (T 0)
                           ))
                       ))]
            (V (GO A))
            (T (RETURN SU]))
    ]

```

(\BN.D2TH

(* Imm "9-Jan-86 15:31")

```

[LAMBDA (U)
  (PROG (B S V BI M AI)
    (COND
      ((NULL U)
       (RETURN B)))
    [COND
      [(OR (EQ (CAR U)
                '+)
           (EQ (CAR U)
                '-))
       (PROGN (SETQ S (CAR U))
              (SETQ U (CDR U))
              (T (SETQ S '+)]
            (COND
              ((NULL U)
               (RETURN B)))
              (SETQ U (SETQ V (REVERSE U)))
              (SETQ BI 0)
              (SETQ M 1)
              [while (AND U (ILESSP M \BIGNUM.THETA)) do (PROGN (SETQ AI (CAR U))
                                                                    (SETQ U (CDR U))
                                                                    (SETQ BI (IPLUS (ITIMES AI M)
                                                            BI))
                                                                    (SETQ M (ITIMES 10 M)
                                                                    ))]
              (COND
                ((EQ S '-)
                 (SETQ BI (IMINUS BI)
                 (SETQ B (CONS BI B))
                 (COND
                   (U (GO L2)))
                 (RETURN B))
                ))]
    ]

```

(\BN.FROM.FIXP

(* kbr%: "11-Sep-86 14:54")

```

[LAMBDA (U)
  (COND
    ((type? BIGNUM U)
     (fetch (BIGNUM ELEMENTS) of U))
    ((OR (NULL U)
         (EQ U 0))
     NIL)
    ((LISTP U)
     U)
    [(ILESSP U 0)
     (COND
       ((EQUAL U MIN.FIXP)
        (\BN.DIFFERENCE (\BN.FROM.FIXP (IPLUS U \BIGNUM.THETA))
                          (\BN.FROM.FIXP \BIGNUM.THETA)))
       (T (\BN.MINUS (\BN.IGNN (IMINUS U)
                                (T (\BN.IGNN U))
```

(\BN.ICANON

(* jrb%: "6-Nov-86 15:30")

```

[LAMBDA (U SIGN)
  (PROG ((U0 U)
         U1
         (CARRY 0)
         B)
    A (SETQ B (IPLUS (CAR U)
                     CARRY))
      (SETQ CARRY (COND
                    ((AND (IGREATERP SIGN 0)
                          (ILESSP B 0))
                     -1)
                    ((AND (ILESSP SIGN 0)
                          (IGREATERP B 0))
                     1)
                    (T 0)))
      (SETQ B (IDIFFERENCE B (ITIMES CARRY \BIGNUM.BETA)))
      (RPLACA U B)
      (COND
        ((NEQ B 0)
         (SETQ U1 U)))
    B [COND
        ((CDR U)
         (SETQ U (CDR U))
         (GO A))
        (T
         (CL:IF (NEQ U1 U)
                 (RPLACD U1 NIL]
      (RETURN U0]))
```

(* "U1 points to the high-order non-zero bignum node")

(* "If U1 is not eq to U here, we have high-order zero nodes in this bignum")

(\BN.IDIVIDE

(* Imm "20-JUL-84 01:37")

```

[LAMBDA (A B)
  (CONS (IQUOTIENT A B)
        (IREMAINDER A B))
```

(\BN.ISUM0

(* Imm "9-Jan-86 15:30")

```

[LAMBDA (U V)
  (PROG ((CARRY 0)
         RES BP)
    A (SETQ BP (\BN.IDIVIDE (IPLUS (CAR U)
                                   (IPLUS (CAR V)
                                           CARRY))
                            \BIGNUM.BETA))
      (SETQ CARRY (CAR BP))
      (SETQ RES (CONS (CDR BP)
                      RES))
      (SETQ U (CDR U))
      (SETQ V (CDR V))
      (COND
        (V (GO A)))
    [COND
      ((NEQ CARRY 0)
       (SETQ RES (CONS CARRY RES]
      (RETURN (REVERSE RES]))
```

(\BN.ISUM1

(* Imm "20-JUL-84 02:22")

```

[LAMBDA (U V)
  (PROG (C S RES)
    (SETQ C 0)
    (SETQ S 0)
    A (SETQ C (IPLUS (CAR U)
                     (CAR V)))
      (COND
        ((NEQ C 0)
```

```

      (SETQ S C)))
    (SETQ RES (CONS C RES))
    (SETQ U (CDR U))
    (SETQ V (CDR V))
    (COND
      (V (GO A)))
    (RETURN (COND
      ((EQ S 0)
        NIL)
      (T (\BN.ICANON (DREVERSE RES)
        (COND
          ((ILESSP S 0)
            -1)
          (T 1))
        )
      )
    )
  )

```

(\BN.MADD

(* Imm "9-Jan-86 15:30")

```

[LAMBDA (A B C)
  (PROG (H TT TTT IP IPP)
    (SETQ TT A)
    (SETQ H 0)
    L2 (SETQ IP (\BN.IDIVIDE (ITIMES B (CAR TT))
      \BIGNUM.BETA))
      (SETQ IPP (\BN.IDIVIDE (IPLUS C (IPLUS (CDR IP)
        H))
        \BIGNUM.BETA))
      (RPLACA TT (CDR IPP))
      (SETQ H (CAR IP))
      (SETQ C (CAR IPP))
      (SETQ TTT TT)
      (SETQ TT (CDR TT))
      (COND
        (TT (GO L2)))
      (SETQ C (IPLUS C H))
      (COND
        ((EQ C 0)
          (RETURN A)))
      (RPLACD TTT (CONS C (CDR TTT)))
      (RETURN A])
  )

```

(\BN.TO.FIXP

(* kbr%: "11-Sep-86 14:58")

```

[LAMBDA (X)
  (COND
    [(LISTP X)
      (COND
        ((OR (EQ (\BN.COMPAREN X (CONSTANT (\BN.FROM.FIXP MAX.FIXP)))
          1)
          (EQ (\BN.COMPAREN X (CONSTANT (\BN.FROM.FIXP MIN.FIXP)))
            -1))
          (create BIGNUM
            ELEMENTS _ X))
          (T (\BIGNUM.TO.INT X]
        )
      )
    ]
    ((NULL X)
      0)
    ((EQ X 'MAX.INTEGER)
      MAX.INTEGER)
    ((EQ X 'MIN.INTEGER)
      MIN.INTEGER)
    (T (SHOULDNT])
  )

```

(\BN.NZEROS

(* Imm "20-JUL-84 02:30")

```

[LAMBDA (N)
  (for I from 1 to N collect 0])

```

(\BN.QRS

(* Imm "9-Jan-86 15:30")

```

[LAMBDA (B I)
  (PROG (D CP C1 C2)
    [COND
      ((NULL B)
        (RETURN (CONS B 0])
      )
    ]
    (COND
      ((EQ I 0)
        (ERROR " QRS DIV BY 0 ")))
      (SETQ B (REVERSE B))
      (SETQ C1 0)
    A (SETQ C2 (CAR B))
      (SETQ CP (\BN.IDIVIDE (IPLUS (ITIMES C1 \BIGNUM.BETA)
        C2)
        I))
    ]
    [COND
      ((OR D (NOT (EQ (CAR CP)
        0))))
      (SETQ D (CONS (CAR CP)
        D])
    ]
  )

```

```

    (SETQ B (CDR B))
    (SETQ C1 (CDR CP))
    [COND
      ((NULL B)
        (RETURN (CONS D C1]
      (GO A])

```

(\BN.SIGN

(* kbr%: "11-Sep-86 15:22")

```

[LAMBDA (U)
  (COND
    [(ATOM U)
      (COND
        ((NULL U)
          0)
        ((EQ U 'MAX.INTEGER)
          1)
        ((EQ U 'MIN.INTEGER)
          -1)
        (T (SHOULDNT]
      ((IGREATERP (CAR U)
        0)
        1)
      ((ILESSP (CAR U)
        0)
        -1)
      (T (\BN.SIGN (CDR U))

```

(\BN.TH2B

(* Imm "9-Jan-86 15:31")

```

[LAMBDA (U)
  (PROG (AI B)
    (COND
      ((NULL U)
        (RETURN B)))
    (SETQ AI (CAR U))
    (SETQ U (CDR U))
    (SETQ B (CONS AI B))
    [while U do (PROGN (SETQ AI (CAR U))
      (SETQ U (CDR U))
      (SETQ B (\BN.MADD B \BIGNUM.THETA AI]
    (RETURN B])

```

(\BN.TH2D

(* bvm%: "15-Apr-86 14:28")

(* * A is a list of integers obtained by repeatedly dividing some bignum by TH, which is a power of RADIX, hopefully chosen to keep the integers small. The elements of A concatenated thus make up the print name of the bignum in the indicated RADIX. Convert the list to a series of character codes by computing the print names of each subpart)

```

(OR RADIX (SETQ RADIX 10))
(COND
  ((NULL A)
    (LIST (CHARCODE 0)))
  (T (for AI in A bind (MAXFACTOR _ (IQUOTIENT TH RADIX))
    DIGIT RESULT
    do [for (M _ MAXFACTOR) by (IQUOTIENT M RADIX) repeatuntil (EQ M 1)
      do (SETQ DIGIT (IQUOTIENT AI M))
        (SETQ AI (IDIFFERENCE AI (ITIMES DIGIT M)))
      (COND
        ((OR RESULT (NEQ DIGIT 0))
          (push RESULT (COND
            ((GEQ (SETQ DIGIT (ABS DIGIT))
              10) (* Use alphabets for digits greater than 9)
            (IPLUS (IDIFFERENCE DIGIT 10)
              (CHARCODE A)))
          (T (IPLUS DIGIT (CHARCODE 0]
        finally (RETURN (COND
          ((IGREATERP (CAR A)
            0)
            (REVERSE RESULT))
          (T
            (CONS (CHARCODE -)
              (REVERSE RESULT]))

```

(* Negative bignum)

(DEFINEQ

(\INITBIGNUMS

(* JDS "1-JAN-99 22:00")

```

[LAMBDA NIL
  ;; Initialize the BIGNUM datatype.
  ;; First, set up the type info so that newly created BIGNUM pages are correct.
  (\SETTYPMASK (\TYPENUMBERFROMNAME 'BIGNUM)
    (LOGOR \TT.FIXP \TT.NUMBERP \TT.ATOM))

```

```
;; Now create some initial bignums for later use:
```

```
(SETQ \BIG.0 (\BN.FROM.FIXP 0)) ; BIGNUM of 0
(SETQ \BIG.1 (\BN.FROM.FIXP 1)) ; BIGNUM of 1
(SETQ MIN.INTEGER (create BIGNUM
                           ELEMENTS _ 'MIN.INTEGER))
(SETQ MAX.INTEGER (create BIGNUM
                           ELEMENTS _ 'MAX.INTEGER])
```

```
)
```

```
;; MAKERATIONAL needs work
```

```
;; needs work: MASK.1'S MASK.0'S BITTEST BITSET BITCLEAR LOGNOT LOADBYTE DEPOSITBYTE IMODLESSP IMODPLUS
;; IMODDIFFERENCE ROT
```

```
(DECLARE%: DONTEVAL@LOAD DOCOPY
```

```
(\INITBIGNUMS)
```

```
)
```

```
(PUTPROPS LLBIGNUM COPYRIGHT ("Venue & Xerox Corporation" 1985 1986 1987 1990 1993 1999))
```

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