

data_clustering_1

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1 Data Clustering

Data clustering is a process of assigning a set of records into subsets, called clusters, such that records in the same cluster are similar and records in different clusters are quite distinct.

A typical clustering process involves the following five steps:

1. pattern representation;
2. dissimilarity measure definition;
3. clustering;
4. data abstraction;
5. assesment of output

In this interactive session, we will be reviewing the *k-means* algorithm.

1.1 The *k-means* Algorithm

The *k-means* algorithm is the most popular and the simplest partitional clustering algorithm. It has many variations. This exercise will review the standard algorithm and several implementations (possibly for different variations).

1.1.1 Description of the Algorithm

Let $X = \{\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_{n-1}\}$ be a numeric dataset containing n records and k be an integer in $\{1, 2, \dots, n\}$. The *k-means* algorithm tries to divide the dataset into k clusters C_0, C_1, \dots , and C_{k-1} by minimizing the following objective function:

$$E = \sum_{i=0}^{k-1} \sum_{\mathbf{x} \in C_i} D(\mathbf{x}, \boldsymbol{\mu}_i),$$

where $D(\cdot, \cdot)$ is a distance measure and $\boldsymbol{\mu}_i$ is the mean of cluster C_i , i.e.,

$$\boldsymbol{\mu}_i = \frac{1}{|C_i|} \sum_{\mathbf{x} \in C_i} \mathbf{x}$$

Let γ_i be the cluster membership of record \mathbf{x}_i for $i = 0, 1, \dots, n-1$. That is, $\gamma_i = j$ if \mathbf{x}_i belongs to cluster C_j . Then the objective function can be rewritten as:

$$E = \sum_{i=0}^{n-1} D(\mathbf{x}_i, \boldsymbol{\mu}_{\gamma_i})$$

To minimize the objective function, the *k-means* algorithm employs an iterative process. At the beginning, the *k-means* algorithm selects k random records from the dataset X as initial cluster centers.

Suppose $\mu_0^{(0)}, \mu_1^{(0)}, \dots$, and $\mu_{k-1}^{(0)}$ are the initial cluster centers. Based on these cluster centers, the *k-means* algorithm updates the cluster memberships $\gamma_0^{(0)}, \gamma_1^{(0)}, \dots, \gamma_{n-1}^{(0)}$ as follows:

$$\gamma_i^{(0)} = \underset{0 \leq j \leq k-1}{\operatorname{argmin}} D(\mathbf{x}_i, \mu_j^{(0)}) \quad (1)$$

where argmin is the argument that minimizes the distance. That is, $\gamma_i^{(0)}$ is set to the index of the cluster to which \mathbf{x}_i has the smallest distance.

Based on the cluster memberships $\gamma_0^{(0)}, \gamma_1^{(0)}, \dots, \gamma_{n-1}^{(0)}$, the *k-means* algorithm updates the cluster centers as follows:

$$\mu_j^{(1)} = \frac{1}{\left| \left\{ i \mid \gamma_i^{(0)} = j \right\} \right|} \sum_{i=0, \gamma_i^{(0)}=j} \mathbf{x}_i, \quad j = 0, 1, \dots, k-1 \quad (2)$$

Then the *k-means* algorithm repeats updating the cluster memberships based on equations 1 and 2.

1.2 Exercises

1.2.1 To practice your Python

1. From the datasets card in trello, use `data.tar.gz` to get the file with name `600points.csv`.
2. Use the `kmeans` implementation from `scikit-learn` to run the algorithm for $k = 3$ clusters and a max of 100 iterations. You can install that using `pip ($ pip install scikit-learn)` or `anaconda, ($ conda install scikit-learn)`.
3. Use python's `docopt` or `argparse` (available in the standard library) to parse the following command line options:

Allowed options:

```
--help           produce help message
--datafile arg    the data file
--k arg (=3)      number of clusters
--maxiter arg (=100) maximum number of iterations
```

4. Implement the algorithm by yourself and compare with the results obtained with `scikit-learn`.
5. Use `numba` to try to improve the performance of your implementation.
6. Use `matplotlib` (or another library of your preference) to visualize data and your results. Fine tune your plot so that the assesment of the result is easier to understand.

1.2.2 To practice with .NET (C# or F#)

1. Use the *k-means* implementation from version 0.2 of [ML.NET](#) as a reference implementation for comparison (correctness of results, performance, etc).
2. Use [.NET's docopt port](#) to parse command line options for your program (see analogous section for Python).
3. Implement your own version of k-means using your preferred .NET language (C#, F#, VB.NET).
4. Visualize your results with [XPlot](#), [FSharp.Charting](#), [Live-Charts](#) or any other good quality library of your preference.

1.2.3 To practice with GPUs and Python/R/C

1. Take a look at [kmcuda](#). See what the possibilities are for your favorite programming language.
2. Visualize your results with the best library for your language of choice.

1.2.4 To practice with GPUs or Multicore CPUs and Haskell

1. Take a look at [Accelerate](#) and the different supported backends (e.g. Multicore CPUs and GPUs).
2. Study and explain the [k-means sample](#)
3. Compare the implementations and performance.
4. Visualize using [matplotliblib bindings for Haskell](#).

1.2.5 To practice with Scala and Spark

1. Try to use the existing Scala implementations:
 - With [Spark's MLlib](#)
 - With [Spire](#)
2. Study and explain.
3. Hard: study if it is possible to improve performance using [sbt-javacpp](#) bindings for CUDA and previous implementation code/algorithms.
4. Visualize using [Vegas](#) or any other good quality library of your preference.