

# Alloy Specification of Backbone

## Organisation of Alloy Modules

Figure 1 shows the dependencies of the individual Alloy modules in the specification.

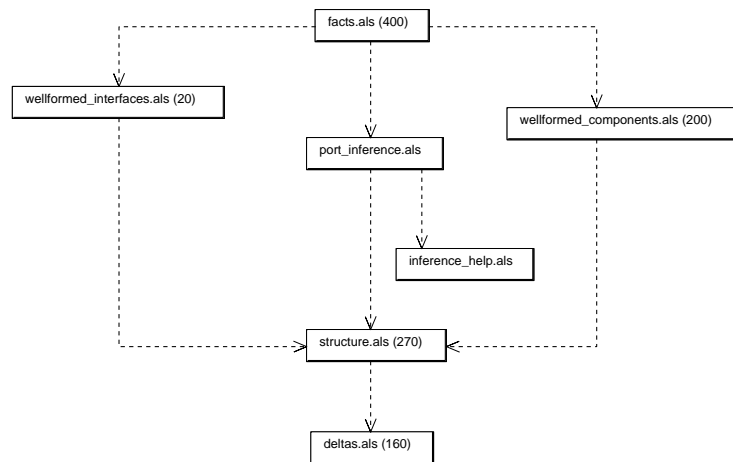


Figure 1: Module structure of the specification

## Main Signatures

A UML class diagram of the main signatures is shown in figure 2.

## Constituent Signatures

The constituent signatures are shown in figure 3.

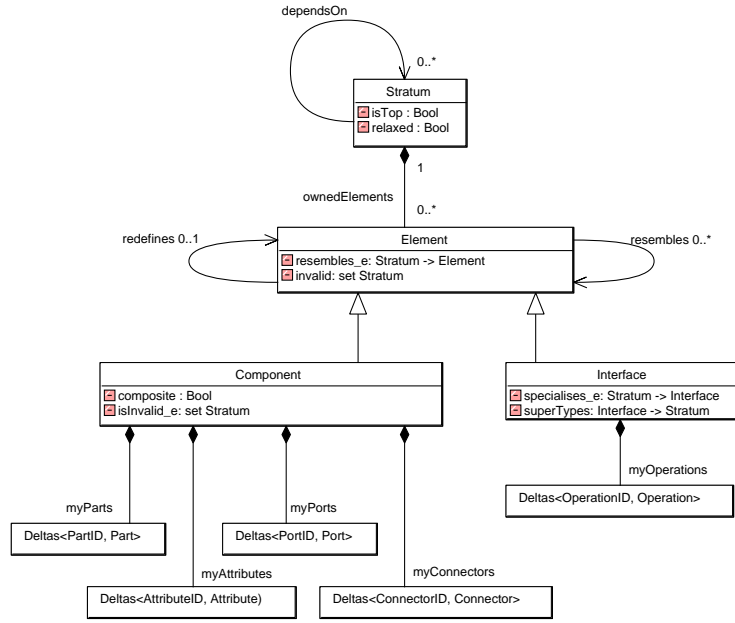


Figure 2: The main signatures of the Backbone specification

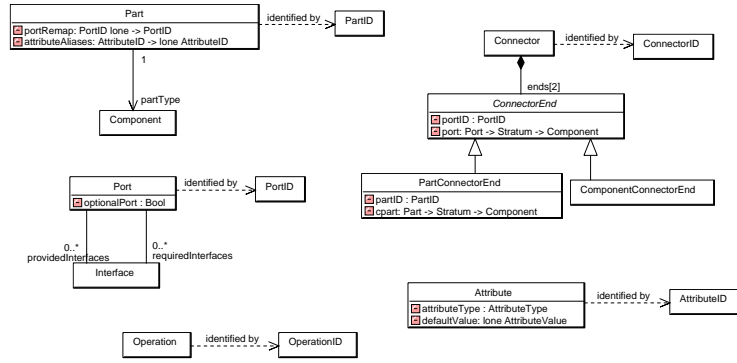


Figure 3: The constituent figures for the Backbone specification

# Structure.als

Listing 1: structure.als

```
1 module structure
2
3 open util/boolean as boolean
4 open util/relation as relation
5 open deltas[Stratum, Component, PartID, Part] as Parts
6 open deltas[Stratum, Component, PortID, Port] as Ports
7 open deltas[Stratum, Component, ConnectorID, Connector] as Connectors
8 open deltas[Stratum, Component, AttributeID, Attribute] as Attributes
9 open deltas[Stratum, Interface, OperationID, Operation] as Operations
10 open deltas[Stratum, Interface, InterfaceImplementationID, InterfaceImplementation] as
    InterfaceImplementation
11
12
13 one sig Model
14 {
15   -- normally this should be set to none
16   errorsAllowed: set Stratum,
17   providesIsOptional: Bool
18 }
19
20 sig Stratum
21 {
22   -- strata that this directly depends on
23   dependsOn: set Stratum,
24   -- does this expose stratum it depends on?
25   isRelaxed: Bool,
26
27   -- derived state -- exposes strata includes this and canSee
28   exposesStrata: set Stratum,
29   canSee: set Stratum,
30   canSeePlusMe: set Stratum,
31
32   -- simple is all that we directly depend on
33   -- taking away what any children depend on
34   simpleDependsOn: set Stratum,
35
36   -- a single top exists which binds directly
37   -- any independent stratum
38   isTop: Bool,
39   -- this is every stratum that can be seen from here down
40   transitive: set Stratum,
41   transitivePlusMe: set Stratum,
42   ownedElements: set Element,
43   -- each attribute type is owned by a single stratum
44   attributeTypes: set AttributeType,
45
46   -- elements that redefine another
47   redefining: set Element,
48   components that are new definitions
49   defining: set Element
50 }
51 {
52   defining = ownedElements - redefining
53   canSeePlusMe = canSee + this
54   transitivePlusMe = transitive + this
55 }
56
57 abstract sig Element
58 {
59   home: Stratum,
60   redefines: lone Element,
61   resembles: set Element,
62
63   -- for a given stratum, a component resembles other components in a given stratum view
64   resembles_e: Element -> Stratum,
65   -- does this act as a non-primed for a particular stratum
66   actsAs_e: Element -> Stratum,
67   -- is this element valid for a given stratum?
68   isInvalid_e: set Stratum
69 }
70 {
71   -- owned by a single stratum
72   home = ownedElements.this
73 }
74
75 sig Component extends Element
76 {
77   -- composite or leaf?
78   -- all components apart from direct impl components are always composite
79   isComposite: Bool,
80   implementation: lone ComponentImplementation,
81
82   -- the final result, after taking redef + resemblance into account
```

```

83  idParts: PartID -> Part -> Stratum,
84  parts: Part -> Stratum,
85  ports: Port -> Stratum,
86  connectors: Connector -> Stratum,
87  attributes: Attribute -> Stratum,
88
89  myParts: lone Parts/Deltas,
90  myPorts: lone Ports/Deltas,
91  myConnectors: lone Connectors/Deltas,
92  myAttributes: lone Attributes/Deltas,
93
94  -- the internal links, used for port type inferencing
95  links: PortID -> PortID,
96  inferredLinks: Port -> Port -> Stratum
97 }
98 {
99   -- for components
100   redefines + resembles in Component
101   -- propagate up the objects from the delta into the sig, to make it more convenient
102   parts = myParts.objects
103   ports = myPorts.objects
104   connectors = myConnectors.objects
105   attributes = myAttributes.objects
106
107   -- a leaf has an implementation
108   isFalse[isComposite] <=> one implementation
109
110   -- form idParts
111   idParts = {n: PartID, p: Part, s: Stratum | s -> n -> p in myParts.objects_e}
112
113   -- make sure links has no duplication
114   no "links & links"
115
116   -- we only have links for leaves, so all ports must be new
117   dom[links] + ran[links] in myPorts.newIDs
118 }
119
120 -- ensure each delta is composed by only one component
121 fact
122 {
123   all p: Parts/Deltas | one myParts.p
124   all p: Ports/Deltas | one myPorts.p
125   all c: Connectors/Deltas | one myConnectors.c
126   all a: Attributes/Deltas | one myAttributes.a
127 }
128
129 sig Interface extends Element
130 {
131   -- the expanded elements
132   operations: Operation -> Stratum,
133   implementation: InterfaceImplementation -> Stratum,
134   superTypes: Interface -> Stratum,
135
136   -- the deltas
137   myOperations: Operations/Deltas,
138   myImplementation: InterfaceImplementation/Deltas
139 }
140 {
141   -- for interfaces
142   redefines + resembles in Interface
143   -- propagate up the objects from the delta into the sig, to make it more convenient
144   operations = myOperations.objects
145   implementation = myImplementation.objects
146 }
147 -- ensure each delta is composed by only one interface
148 fact
149 {
150   all p: Operations/Deltas | one myOperations.p
151   all i: InterfaceImplementation/Deltas | one myImplementation.i
152 }
153
154
155 -- each artifact must have a id, so it can be replaced or deleted
156 sig PartID, PortID, ConnectorID, AttributeID, OperationID, InterfaceImplementationID {}
157
158 sig Part
159 {
160   partType: Component,
161   -- remap a port from this part onto the port of a part that we are replacing
162   -- (new port -> old, replaced port)
163   portRemap: PortID lone -> lone PortID,
164   portMap: Stratum -> PortID lone -> lone Port,
165
166   -- the values of the attributes are set in the part (child id -> parent id)
167   -- although they don't have to be set if we want to take the default
168   attributeValues: AttributeID -> lone AttributeValue,
169   -- do we alias a parent attribute?
170   attributeAliases: AttributeID -> lone AttributeID,
171   -- or do we simply copy a parent attribute, but retain our own state?
172   attributeCopyValues: AttributeID -> lone AttributeID,
173

```

```

174 -- derived state -- the parts that the connectors link to
175 linkedToParts: Part -> Stratum -> Component,
176 -- derived state -- any componts that the connectors link to
177 linkedToOutside: Stratum -> Component
178 }
179
180 abstract sig Index {}
181 one sig Zero, One, Two, Three extends Index {}
182
183 pred isContiguousFromZero(indices: set Index)
184 {
185   indices = indices.*(Three->Two + Two->One + One->Zero)
186 }
187
188 sig Port
189 {
190   -- set values are what the user has explicitly set
191   setProvided, setRequired: set Interface,
192   -- provided and required are inferred
193   provided, required: Interface -> Stratum -> Component,
194   mandatory, optional: set Index
195 }
196 {
197   -- mandatory indices start at 0, optional start from mandatory end, no overlap
198   -- all contiguous and must have some indices
199   isContiguousFromZero[mandatory] and
200   isContiguousFromZero[mandatory + optional]
201   no mandatory & optional -- no overlap
202   some mandatory + optional -- but must have some indices
203 }
204
205
206 sig Connector
207 {
208   -- require 2 ends
209   ends: set ConnectorEnd
210 }
211 {
212   -- ensure 2 connector ends using a trick felix taught me
213   some disj end1, end2: ConnectorEnd | ends = end1 + end2
214   all end: ends |
215     end.otherEnd = ends - end
216 }
217
218 abstract sig ConnectorEnd
219 {
220   portID: PortID,
221   port: Port -> Stratum -> Component,
222   index: Index,
223   otherEnd: ConnectorEnd
224 }
225 {
226   -- an end is owned by one connector
227   one ends.this
228 }
229
230 sig ComponentConnectorEnd extends ConnectorEnd
231 {
232 }
233
234 sig PartConnectorEnd extends ConnectorEnd
235 {
236   partID: PartID,
237   cpart: Part -> Stratum -> Component
238 }
239
240
241 sig Attribute
242 {
243   attributeType: AttributeType,
244   defaultValue: lone AttributeValue
245 }
246 {
247   some defaultValue =>
248     defaultValue.valueType = attributeType
249 }
250
251 sig AttributeValue
252 {
253   valueType: AttributeType
254 }
255
256 sig AttributeType
257 {
258 }
259 {
260   -- owned by one stratum
261   one attributeTypes.this
262 }
263
264 sig Operation

```

```

265 {
266   -- this identifies the implementation id and signature
267 }
268
269 sig InterfaceImplementation
270 {
271   -- this identifies the interface implementation class or no s.dependsOns...
272 }
273
274 sig ComponentImplementation
275 {
276   -- this identifies the component implementation class...
277 }
278
279 -- used for port inference
280 -- a bit like a connector, but multiplicity and optionality don't count
281 abstract sig LinkEnd
282 {
283   linkPortID: PortID,
284   linkError: Stratum -> Component
285   -- the internal interfaces are the interfaces presented inside the component content area
286   -- for a port, it is the interfaces seen internally (opposite)
287   -- for a port instance, it is the interfaces seen externally (same)
288 }
289
290 sig ComponentLinkEnd extends LinkEnd
291 {
292 }
293
294 sig PartLinkEnd extends LinkEnd
295 {
296   linkPartID: PartID
297 }
298
299 -- translate from port id to component link end -- guaranteed to be 1 per id
300 fun GetComponentLinkEnd(id: PortID): one ComponentLinkEnd
301 {
302   { end: ComponentLinkEnd | end.linkPortID = id }
303 }
304
305 -- translate from a port/part to a part link end -- guaranteed to be 1 per pair
306 fun getPartLinkEnd(portID: PortID, partID: PartID): PartLinkEnd
307 {
308   { end: PartLinkEnd | end.linkPortID = portID and end.linkPartID = partID }
309 }
310
311 fun ComponentLinkEnd::getPort(s: Stratum, c: Component): one Port
312 {
313   c.myPorts.objects_e[s][this.linkPortID]
314 }
315
316 fun PartLinkEnd::getPortInstance(s: Stratum, c: Component): Port -> Part
317 {
318   let
319     cpart = c.myParts.objects_e[s][this.linkPartID],
320     cport = cpart.partType.myPorts.objects_e[s][this.linkPortID] |
321     cport -> cpart
322 }
323
324 -- get the port of a component connector
325 fun ComponentConnectorEnd::getPort(s: Stratum, c: Component): lone Port
326 {
327   c.myPorts.objects_e[s][this.portID]
328 }
329
330 -- should return only 1 Port, unless the component is invalid. #NOTE: the component owns the part
331 fun PartConnectorEnd::getPortInstance(s: Stratum, c: Component): Port -> Part
332 {
333   let
334     ppart = c.myParts.objects_e[s][this.portID],
335     port = ppart.portMap[s][this.portID] |
336     port -> ppart
337 }
338
339 fun PartLinkEnd::getPortInstanceRequired(s: Stratum, c: Component): set Interface
340 {
341   let portPart = this.getPortInstance[s, c],
342       pport = dom[portPart],
343       ppartType = ran[portPart].partType
344   {
345     pport.required.ppartType.s
346   }
347 }
348
349 fun PartLinkEnd::getPortInstanceProvided(s: Stratum, c: Component): set Interface
350 {
351   let portPart = this.getPortInstance[s, c],
352       pport = dom[portPart],
353       ppartType = ran[portPart].partType
354   {
355     pport.provided.ppartType.s

```

356 }  
357 }

---

# Facts.als

Listing 2: facts.als

```
1 module facts
2
3 open util/boolean as boolean
4 open util/relation as relation
5 open util/ternary as ternary
6 open structure
7 open port_inference
8 open wellformed_components
9 open wellformed_interfaces
10 open stratum_help
11 open redefinition_types
12
13 -----
14
15 fact StratumFacts
16 {
17   invalidateUnseenPorts []
18   one isTop.True
19   all s: Stratum
20   {
21     -- for relaxed, expose what it depends on and their exposures
22     isTrue[s.isRelaxed] =>
23       s.exposesStrata = s + s.dependsOn.exposesStrata
24     else
25       s.exposesStrata = s
26
27     -- used for partial ordering
28     -- contains nothing the children already depend on
29     s.simpleDependsOn = s.dependsOn -
30       s.dependsOn.transitive
31
32     -- no cycles
33     s not in s.*dependsOn
34
35     -- can only see what others expose
36     s.canSee = s.dependsOn.exposesStrata
37
38     -- the strata we can see using the dependency graph
39     s.transitive = s.*dependsOn
40
41     -- a stratum is called top if no stratum depends on it
42     isTrue[s.isTop] <=> no simpleDependsOn.s
43
44     -- have max of one redefinition of an element per stratum
45     all e: Element |
46       lone s.ownedElements & redefines.e
47     -- ties up redefining and redefines
48     s.redefining = s.ownedElements & dom[redefines]
49   }
50 }
51
52 pred independent[stratum1, stratum2: Stratum]
53 {
54   stratum2 not in stratum1.*dependsOn
55 }
56
57 pred mutuallyIndependent[a, b: Stratum]
58 {
59   independent[a, b] and independent[b, a]
60 }
61
62 fun stratumPerspective[stratum: Stratum]: set Stratum
63 {
64   stratum.*dependsOn
65 }
66
67 -----
68 -- Handle the basics of resemblance (specialisation) and redefinition
69 -----
70
71 fact ElementFacts
72 {
73   -- nothing can resemble a redefinition -- check to see that the things we resemble don't redefine
74   no resembles.redefines
75
76   all
77     e: Element |
78     let
79       owner = e.home,
80       -- strata that can see the component
81       resemblingOwningStratum = e.resembles.home,
82       redefiningOwningStratum = e.redefines.home
83   {
```



```

84      -- no circularities in resemblance or redefinition, and must be visible
85      e not in (e.resembles + e.redefines)
86      resemblingOwningStratum in owner.canSeePlusMe
87      redefiningOwningStratum in owner.canSee
88
89      -- tie up the owning stratum and the elements owned by that stratum
90      e.home = ownedElements.e
91
92      -- we only need to form a definition for stratum that can see us
93      all s: Stratum |
94      let
95          -- who should I resemble
96          -- (taking redefinition into account)
97          iResemble = e.resembles.e.s,
98          -- if we resemble what we are redefining,
99          -- look for the original under here
100         topmostOfRedefined = getTopmost [
101             owner.simpleDependsOn,
102             e.redefines & e.resembles],
103         -- look for any other resembled components
104         -- from here down
105         topmostOfResemblances = getTopmost [
106             s,
107             e.resembles - e.redefines]
108     {
109         -- who do we act as in this stratum?
110         e.actsAs.e.s =
111             { real: Element | no real.redefines and e in getTopmost[s, real] }
112         -- rewrite the resemblance graph to handle redefinition
113         owner not in s.transitivePlusMe =>
114             no iResemble
115         else
116             iResemble = topmostOfRedefined + topmostOfResemblances
117     }
118 }
119 }
120
121 fun getTopmost(s: set Stratum, e: Element): set Element
122 {
123     let redefined = redefines.e & s.transitivePlusMe.redefining,
124     topmostRedefined = redefined - redefined.resembles.e.s
125     { some topmostRedefined => topmostRedefined else e }
126 }
127
128 -----
129 -- handle any extra rules for interfaces
130 -----
131
132 fact InterfaceFacts
133 {
134     all i: Interface |
135     let
136         owner = i.home
137     {
138         -- we only need to form a definition for stratum that can see us
139         all s: Stratum |
140         let
141             invalid = s in i.isInvalid.e,
142             visible = owner in s.transitivePlusMe
143         {
144             -- if we can see this component, test to see if it is valid in this stratum
145             not visible =>
146                 invalidateUnseenInterface[s, i]
147             else
148             {
149                 -- ensure that the subtypes are set up correctly
150                 -- this is a subtype of an interface if we can reach it transitively and
151                 -- our set of operations are a super-set of the super type's
152                 -- of operationID -> Operation. i.e. if you replace an operationID you are breaking subtype
153                 -- so the operationID is the name, and the Operation is the full spec which is assumed to have
154                 -- changed in a redef...
155                 -- NOTE: the super types are direct -- to follow use closure
156                 -- also note that we only need/want supertypes for non-primes
157                 no i.redefines =>
158                 {
159                     i.superTypes.s =
160                         { super: i.resembles |
161                             super.myOperations.objects.e[s] in
162                                 i.myOperations.objects.e[s] }
163                 }
164             else
165                 no i.superTypes.s
166
167             -- merge any parts and apply changes
168             let topmost = getTopmost[s, i] & Interface
169             {
170                 i.myOperations::mergeAndApplyChangesForResemblance [
171                     s, i, i.resembles.e.s.myOperations]
172                 i.myOperations::mergeAndApplyChangesForRedefinition [
173                     s, i, topmost, topmost.myOperations]
174                 i.myImplementation::mergeAndApplyChangesForResemblance [

```

```

175         s, i, i.resembles_e.s.myImplementation]
176         i.myImplementation::mergeAndApplyChangesForRedefinition [
177             s, i, topmost, topmost.myImplementation]
178     }
179
180     -- the component must be valid in the place it was defined
181     -- also, in any stratum (apart from the top one), a visible component must be valid
182     (s = owner or s not in Model.errorsAllowed) => !invalid
183     s = owner =>
184     {
185         i.myOperations.deltasIsWellFormed[s]
186         i.myImplementation.deltasIsWellFormed[s]
187     }
188
189     -- a component is valid if it is well formed...
190     !invalid <=> interfaceIsWellFormed[s, i]
191 }
192 }
193 }
194 }
195 }
196
197 -----
198 -- handle any extra rules for components
199 -----
200
201 fact ComponentFacts
202 {
203     -- no part or port can refer explicitly to a redefined component or interface
204     no partType.redefines
205     no (setProvided + setRequired).redefines
206
207     all c: Component |
208     let
209         owner = c.home,
210         -- strata that the component can see
211         iCanSeePlusMe = owner.canSeePlusMe,
212         types = c.myParts.newObjects.partType,
213         attrTypes = c.myAttributes.newObjects.attributeType,
214         interfaces = c.myPorts.addedObjects.(setRequired + setProvided)
215     {
216         -- resemblance has no redundancy
217         c.resembles = c.resembles - c.resembles.*resembles
218
219         -- component implementations stay the same...
220         isFalse[c.isComposite] =>
221         {
222             -- no resemblance, redef, parts + noone resembles or redefines it
223             no c.myParts
224             no c.myConnectors
225             no resembles.c
226             no c.resembles
227         }
228         else
229             no c.links
230
231         -- parts can only have types from here down, excluding myself...
232         -- attribute types can only be from here down
233         -- ports can only refer to interfaces from here down
234         types.home in iCanSeePlusMe
235         attributeTypes.attrTypes in iCanSeePlusMe
236         interfaces.home in iCanSeePlusMe
237
238         -- ensure that the port remaps are correctly formed for the stratum they are owned by
239         let delta = c.myParts |
240         all p: delta.newObjects | -- parts of the delta
241         let
242             partID = delta.replaceObjects.p,
243             oldPart = delta.oldObjects_e[owner][partID],
244             remap = p.portRemap,
245             newPortIDs = dom[remap],
246             oldPortIDs = ran[remap]
247         {
248             -- we can only alias ports that we actually have
249             newPortIDs in dom[p.partType.myPorts.objects_e[owner]]
250             -- we can only use port ids of the component we are replacing
251             oldPortIDs in dom[oldPart.partType.myPorts.objects_e[owner]]
252
253             -- each port we remap should have a different id, or there's no point
254             -- this is not strictly needed, but ensures nice witnesses
255             bijection[remap, newPortIDs, oldPortIDs]
256
257             -- can't map a port id onto the same id
258             no remap & iden
259         }
260     }
261
262     -- we only need to form a definition for stratum that can see us
263     all s: Stratum |
264     let
265         invalid = s in c.isInvalid_e,

```

```

266     visible = owner in s.transitivePlusMe
267   {
268     -- if we can see this component, test to see if it is valid in this stratum
269     not visible =>
270       invalidateUnseenComponent [s, c]
271     else
272       let topmost = getTopmost [s, c] & Component
273       {
274         -- merge any parts and apply changes
275         c.myParts::mergeAndApplyChangesForResemblance [
276           s, c, c.resembles_e.s.myParts]
277         c.myParts::mergeAndApplyChangesForRedefinition [
278           s, c, topmost, topmost.myParts]
279
280         -- merge any ports and apply changes
281         c.myPorts::mergeAndApplyChangesForResemblance [
282           s, c, c.resembles_e.s.myPorts]
283         c.myPorts::mergeAndApplyChangesForRedefinition [
284           s, c, topmost, topmost.myPorts]
285
286         -- merge any connectors and apply changes
287         c.myConnectors::mergeAndApplyChangesForResemblance [
288           s, c, c.resembles_e.s.myConnectors]
289         c.myConnectors::mergeAndApplyChangesForRedefinition [
290           s, c, topmost, topmost.myConnectors]
291
292         -- merge any attributes and apply changes
293         c.myAttributes::mergeAndApplyChangesForResemblance [
294           s, c, c.resembles_e.s.myAttributes]
295         c.myAttributes::mergeAndApplyChangesForRedefinition [
296           s, c, topmost, topmost.myAttributes]
297
298         -- if we are "home", all the deltas must be well formed...
299         -- this is not necessarily the case if we are not home
300         s = owner =>
301         {
302           c.myParts.deltasIsWellFormed [s]
303           c.myPorts.deltasIsWellFormed [s]
304           c.myConnectors.deltasIsWellFormed [s]
305           c.myAttributes.deltasIsWellFormed [s]
306         }
307
308         setupParts [s, c]
309         setupConnectors [s, c]
310         isTrue [c.isComposite] =>
311           setupCompositeLinks [s, c]
312         else
313           setupLeafLinks [s, c]
314
315         -- the component must be valid in the place it was defined
316         -- also, in any stratum (apart from the top one), a visible
317         -- component must be valid
318         (s = owner or s not in Model.errorsAllowed) => !invalid
319
320         -- a component is invalid iff it is not well formed
321         invalid <=>
322           (!componentIsWellFormed [s, c] or !linksAreWellFormed [s, c])
323       }
324     }
325   }
326 }
327
328 pred setupParts (s: Stratum, c: Component)
329 {
330   -- reference the parts we are linked to and link to the outside if true
331   let allParts = c.parts.s
332   {
333     no (Part - allParts).linkedToParts.c.s
334     all pPart: allParts |
335     {
336       pPart.linkedToParts.c.s =
337       { p: allParts - pPart |
338         some end: c.connectors.s.ends |
339         end.cpart.c.s = pPart and end.otherEnd.cpart.c.s = p }
340
341       -- reference if we are linked to the outside of the component
342       s -> c in pPart.linkedToOutside <=>
343       {
344         some end: c.connectors.s.ends |
345         end.cpart.c.s = pPart and end.otherEnd in ComponentConnectorEnd
346       }
347     }
348   }
349
350   -- form the full port map for this stratum, taking remap into account
351   all p: c.myParts.newObjects |
352   let
353     -- turn the remap from id -> id to id -> port
354     idToPort = p.partType.myPorts.objects_e [s],
355     newPorts = idToPort [PortID],
356     remap =

```

```

357     { newPort: newPorts, oldID: PortID |
358       idToPort.newPort -> oldID in p.portRemap }
359   {
360     -- remove the existing ID of the port before adding the new one
361     "(p.portMap[s]) =
362       "(p.partType.myPorts.objects_e[s]) ++ remap
363   }
364 }
365
366
367 -- if the connector is not visible to a component in a stratum, it should be zeroed out to
368 -- make it easier to interpret the results and and zeroOutUnseenElement[s, e] cut back on the state space
369   for performance reasons
370 fact ZeroOutUnseenConnectorsFact
371 {
372   all conn: Connector, c: Component, s: Stratum |
373   conn not in c.connectors.s =>
374   {
375     all end: conn.ends
376     {
377       no end.port.c.s
378       no end.cpart.c.s
379     }
380   }
381 }
382
383 -- if the part is not visible to a component in a stratum, it should also be zeroed out
384 -- for understandability and performance reasons
385 fact ZeroOutUnseenPartsFact
386 {
387   all p: Part, c: Component, s: Stratum |
388   p not in c.parts.s =>
389   {
390     no p.linkedToParts.c.s
391     s->c not in p.linkedToOutside
392   }
393 }
394
395 -- if the part is not visible to a component in a stratum, it should also be zeroed out
396 -- for understandability and performance reasons
397 -- NOTE: if you move the valid setting up into the main body, it gets slow for some bizarre reason
398 pred invalidateUnseenComponent(s: Stratum, c: Component)
399 {
400   s not in c.isInvalid_e -- it isn't valid here
401   no c.parts.s
402   no c.idParts.s
403   no c.ports.s
404   no c.connectors.s
405   no c.attributes.s
406   no c.inferredLinks.s
407   c.myParts::nothing[s]
408   c.myAttributes::nothing[s]
409   c.myPorts::nothing[s]
410   c.myConnectors::nothing[s]
411 }
412
413 pred invalidateUnseenInterface(s: Stratum, i: Interface)
414 {
415   s not in i.isInvalid_e -- it isn't valid here
416   no i.operations.s
417   no i.implementation.s
418   i.myOperations::nothing[s]
419   i.myImplementation::nothing[s]
420   no i.superTypes.s
421 }
422
423 pred invalidateUnseenPorts()
424 {
425   all s: Stratum, c: Component
426   {
427     all p: Port |
428     p not in c.ports.s =>
429     no p.(provided + required).c.s
430   }
431 }

```

---

# Deltas.als

Listing 3: deltas.als

```
1 module deltas[Stratum, Element, ID, Object]
2
3 open util/boolean as boolean
4 open util/relation as relation
5
6 sig Deltas
7 {
8   -- the expanded objects for this stratum. these 2 fields are the output of the merge!
9   objects:      Object -> Stratum,
10
11   -- old objects is what was there before any replacing was done
12   oldObjects_e: Stratum -> ID -> Object,
13   originalOldObjects_e: Stratum -> ID -> Object,
14
15   -- working variables to track the expansion of objects, and allow it to happen cumulatively
16   -- note: we need to keep track of what has been deleted and replaced to handle the cumulative effects
17   -- e.g. delete in one stream, not in the other.
18   -- NOTE: original is taking only resemblance_e into account, non-original is the full definition
19   -- taking redefinition into account also
20   objects_e: Stratum -> ID -> Object,
21   deletedObjects_e: Stratum -> ID,
22   replacedObjects_e: Stratum -> ID -> Object,
23   originalObjects_e: Stratum -> ID -> Object,
24   originalDeletedObjects_e: Stratum -> ID,
25   originalReplacedObjects_e: Stratum -> ID -> Object,
26
27   -- newObjects is any objects added or replaced. these fields allow new object creation to be controlled
28   newObjects: set Object,
29   addedObjects: set newObjects,
30   replacedObjects: set Object,
31   -- newIDs are any new IDs added
32   newIDs: set ID,
33   -- the deltas that are to be applied. these 3 fields are the input to the merge
34   deleteObjects: set ID,
35   addObjects: newIDs one -> one addedObjects,
36   replaceObjects: ID one -> lone replacedObjects
37 }
38 {
39   -- cannot delete and replace
40   no dom[replaceObjects] & deleteObjects
41   replacedObjects = newObjects - addedObjects
42 }
43
44 -- indicate that any new part/ID can only be introduced by one component
45 fact Owned
46 {
47   all o: Object |
48     one newObjects.o
49
50   -- do we also test for IDs?
51   all n: ID |
52     one newIDs.n
53 }
54
55
56 pred Deltas::oneObjectPerID(s: Stratum)
57 {
58   let objects = this.objects_e[s] |
59     function[objects, dom[objects]]
60 }
61
62 pred Deltas::nothing(s: Stratum)
63 {
64   no this.objects.s
65   no this.objects_e[s]
66   no this.oldObjects_e[s]
67   no this.deletedObjects_e[s]
68   no this.replacedObjects_e[s]
69   no this.originalObjects_e[s]
70   no this.originalDeletedObjects_e[s]
71   no this.originalReplacedObjects_e[s]
72 }
73
74 -- ensure that deletes and replaces makes sense from the perspective of the original stratum
75 pred Deltas::deltasIsWellFormed(owner: Stratum)
76 {
77   -- no overlap between deleted and replaced IDs
78   let
79     deleteIDs = this.deleteObjects,
80     replaceIDs = dom[this.replaceObjects]
81   {
82     -- no overlap between deleted and replaced
83     no deleteIDs & replaceIDs
84   }
85 }
```

```

84      -- anything we delete or replace must be there already
85      deleteIDs + replaceIDs in dom[this.originalOldObjects_e[owner]]
86    }
87  }
88
89  -- ensures that this delta removes everything
90  pred Deltas::cleanSlate(owner: Stratum)
91  {
92    this.deleteObjects = dom[this.oldObjects_e[owner]]
93  }
94
95  -- ensures that we only have adds, no deletes or replaces
96  pred Deltas::onlyAdds(owner: Stratum)
97  {
98    no this.deleteObjects
99    no this.replaceObjects
100  }
101
102
103  -- the predicate to merge any underlying resembled entities and apply current changes
104  -- this is driven off the newly computed resemblance graph for each component in each stratum
105  pred Deltas::mergeAndApplyChangesForResemblance(
106    s: Stratum,
107    c: Element,
108    -- who should I resemble, taking redefinition into account
109    iResembleDeltas_e: set Deltas)
110  {
111    -- handle add, delete etc as if we are only taking resemblance into account
112    -- nothing will ever resemble itself
113    this.originalOldObjects_e[s] =
114      (iResembleDeltas_e.originalObjects_e[s]
115       - iResembleDeltas_e.originalDeletedObjects_e[s]->Object)
116      ++ iResembleDeltas_e.originalReplacedObjects_e[s]
117
118    this.originalDeletedObjects_e[s] =
119      iResembleDeltas_e.originalDeletedObjects_e[s]
120      - dom[iResembleDeltas_e.originalReplacedObjects_e[s]] + this.deleteObjects
121
122    this.originalReplacedObjects_e[s] =
123      (iResembleDeltas_e.originalReplacedObjects_e[s] - this.deleteObjects->Object)
124      ++ this.replaceObjects
125
126    this.originalObjects_e[s] =
127      (((iResembleDeltas_e.originalObjects_e[s] - this.originalDeletedObjects_e[s]->Object)
128       ++ this.originalReplacedObjects_e[s]) + this.addObjects)
129      ++ this.replaceObjects
130  }
131
132  pred Deltas::mergeAndApplyChangesForRedefinition(
133    s: Stratum,
134    c: Element,
135    topmost: set Element,
136    -- who should I resemble, taking redefinition into account
137    iResembleDeltas_e: set Deltas)
138  {
139    -- expand out into a easier form for expressing well-formedness rule, where IDs don't count
140    this.objects = {p: Object, s: Stratum |
141      some n: ID | s->n->p in this.objects_e}
142
143    -- handle add, delete etc as if we are only taking resemblance into account
144    topmost = c =>
145      this.oldObjects_e[s] = iResembleDeltas_e.originalOldObjects_e[s]
146    else
147      this.oldObjects_e[s] =
148        (iResembleDeltas_e.originalObjects_e[s]
149         - iResembleDeltas_e.originalDeletedObjects_e[s]->Object)
150        ++ iResembleDeltas_e.originalReplacedObjects_e[s]
151
152    this.deletedObjects_e[s] =
153      iResembleDeltas_e.originalDeletedObjects_e[s]
154      - dom[iResembleDeltas_e.originalReplacedObjects_e[s]]
155
156    this.replacedObjects_e[s] = iResembleDeltas_e.originalReplacedObjects_e[s]
157
158    this.objects_e[s] =
159      (iResembleDeltas_e.originalObjects_e[s] - this.deletedObjects_e[s]->Object)
160      ++ this.replacedObjects_e[s]
161  }

```

---

# Wellformed\_components.als

Listing 4: wellformed\_components.als

```
1 module wellformed_components
2
3 open util/boolean as boolean
4 open util/relation as relation
5 open util/ternary as ternary
6 open structure
7
8
9 -- check that the component is well formed
10 pred componentIsWellFormed(s: Stratum, c: Component)
11 {
12   -- ***RULE W4: the type of the part must not be in a cyclic relationship with itself through containment
13   -- it also cannot be cyclical with respect to resemblance
14   c not in c.^(resembles_e.s)
15   -- the original (either the thing being redefined or the original)
16   -- is not in the composition hierarchy taking resemblance into account
17   -- NOTE: if c cannot be composed if it is a redefinition
18   -- NOTE: a further constraint is that we cannot be composed of the thing we
19   -- are redefining
20   let
21     resembling = resembles_e.s, partTypes = parts.s.partType,
22     original = no c.redefines => c else c.redefines
23   {
24     original not in c.*(resembling + partTypes).partTypes
25   }
26   -- ***RULE W6: a component must have some ports
27   some c.ports.s
28
29   -- to be well formed, we must have one element per ID
30   c.myPorts.oneObjectPerID[s]
31   c.myAttributes.oneObjectPerID[s]
32
33   // if this is composite, ensure the ports, parts and connectors are well formed
34   isTrue[c.isComposite] =>
35   {
36     -- must always have some parts
37     some c.parts.s
38
39     -- to be well formed, we must have one element per ID
40     c.myParts.oneObjectPerID[s]
41     c.myConnectors.oneObjectPerID[s]
42
43     -- don't require any parts -- e.g. junction components for altering connection interfaces
44     partsAreWellFormed[s, c]
45     connectorsAreWellFormed[s, c]
46     portAndPortInstancesAreConnected[s, c]
47   }
48 }
49
50 pred portAndPortInstancesAreConnected(s: Stratum, c: Component)
51 {
52   all port: c.ports.s |
53     portIsConnected[s, c, port]
54
55   all cpart: c.parts.s |
56     all port: cpart.partType.ports.s |
57       portInstancesIsConnected[s, c, port, cpart]
58 }
59
60
61 pred partsAreWellFormed(s: Stratum, c: Component)
62 {
63   all pPart: c.parts.s
64   {
65     -- ***RULE C8: it must be possible to reach this part from a series of connections from the owning
66     -- component
67     -- otherwise, this part will be completely internally connected -- an island
68     s -> c in pPart.*(linkedToParts.c.s).linkedToOutside
69     -- check the attributes
70     let
71       valueIDs = dom[pPart.attributeValues],
72       aliasIDs = dom[pPart.attributeAliases],
73       copyIDs = dom[pPart.attributeCopyValues],
74       parentAttrs = c.myAttributes.objects_e[s],
75       partAttrs = pPart.partType.myAttributes.objects_e[s],
76       partAttrIDs = dom[partAttrs]
77     {
78       -- should have no overlap between the different types of possibilities
79       disj[valueIDs, aliasIDs, copyIDs]
80       -- all the IDs must exist in the list of attributes
81       (valueIDs + aliasIDs + copyIDs) in partAttrIDs
82     }
83   }
84   -- any new values must have the correct type
```

```

83     all ID: valueIDs |
84         pPart.attributeValues[ID].valueType = partAttrs[ID].attributeType
85
86     -- any aliased or copied attributes must exist and have the correct type
87     all ID: aliasIDs |
88         partAttrs[ID].attributeType =
89             parentAttrs[pPart.attributeAliases[ID]].attributeType
90     all ID: copyIDs |
91         partAttrs[ID].attributeType =
92             parentAttrs[pPart.attributeCopyValues[ID]].attributeType
93
94     -- anything left over must have a default value or else the parts attribute is unspecified
95     all ID: partAttrIDs - (valueIDs + aliasIDs + copyIDs) |
96         one partAttrs[ID].defaultValue
97     }
98 }
99 }
100
101 pred setupConnectors(s: Stratum, c: Component)
102 {
103     all end: c.connectors.s.ends |
104         let other = end.otherEnd, aPort = end.port.c.s, otherPort = other.port.c.s |
105         {
106             -- if just one end of the connector goes to the component, it must be mandatory
107             -- if the part end is mandatory
108             end in ComponentConnectorEnd =>
109             {
110                 end.port.c.s = (end & ComponentConnectorEnd)::getPort[s, c]
111             }
112             else
113             {
114                 -- this is a part connector end, make sure we connect to a single port instance
115                 let
116                     portAndPart = (end & PartConnectorEnd)::getPortInstance[s, c],
117                     resolvedPort = dom[portAndPart]
118                 {
119                     end.port.c.s = resolvedPort
120                     end.cpart.c.s = ran[portAndPart]
121                 }
122             }
123         }
124     }
125 }
126
127 pred connectorsAreWellFormed(s: Stratum, c: Component)
128 {
129     all end: c.connectors.s.ends |
130         let other = end.otherEnd, aPort = end.port.c.s, otherPort = other.port.c.s |
131         {
132             end.index in end.port.c.s.(mandatory + optional)
133             one end.port.c.s
134
135             -- if just one end of the connector goes to the component, it must be mandatory
136             -- if the part end is mandatory
137             end in ComponentConnectorEnd =>
138             {
139                 -- note: other end must be a part connector end, as no component to component connectors are allowed
140                 -- if the outside is optional, the inside cannot be mandatory...
141                 end.index in aPort.optional => other.index in otherPort.optional
142             }
143             else
144             {
145                 one end.cpart.c.s
146                 end.index in aPort.optional <=> other.index in otherPort.optional
147             }
148         }
149     }
150 }
151
152 ----- support predicates
153
154 pred portIsConnected(s: Stratum, c: Component, o: Port)
155 {
156     -- ports on the component must always be connected internally
157     all idx: o.mandatory + o.optional |
158         one end: c.connectors.s.ends & ComponentConnectorEnd |
159         {
160             end.port.c.s = o
161             idx = end.index
162         }
163     }
164 }
165
166 pred portInstanceIsConnected(s: Stratum, c: Component, o: Port, p: Part)
167 {
168     -- don't need to check any provided interfaces -- as these are always optional
169     -- match up any mandatory required interfaces on the port with a single connector
170     all idx: o.mandatory + o.optional |
171         let ends =
172         { end: c.connectors.s.ends & PartConnectorEnd |
173           end.port.c.s = o and end.cpart.c.s = p and idx = end.index

```



```
174   }
175   {
176     (some o.required.c.s or isFalse[Model::providesIsOptional]) =>
177     {
178       idx in o.mandatory =>
179         -- must have a connection
180         one ends
181       else
182         -- can only have at most one connection
183         lone ends
184     }
185   }
186 }
```

---

## Wellformed\_interfaces.als

Listing 5: wellformed\_interfaces.als

---

```
1 module wellformed_interfaces
2
3 open util/boolean as boolean
4 open util/relation as relation
5 open util/ternary as ternary
6 open structure
7
8 -- check that the interface is well formed
9 pred interfaceIsWellFormed(s: Stratum, i: Interface)
10 {
11   -- no circular resemblance for the interface, from the perspective of this stratum
12   i not in i.^(resembles_e.s)
13   -- must have some operations
14   some i.myOperations.objects.s
15   -- should have only 1 operation definition per id
16   i.myOperations.oneObjectPerID[s]
17   -- don't necessarily have to introduce a new implementation
18   lone i.myImplementation.newObjects
19   -- we should only have one implementation, so if we resemble something
20   -- we must replace the implementation
21   one i.implementation.s
22 }
```

---

# Port\_inference.als

Listing 6: port\_inference.als

```
1 module port_inference
2
3 open util/boolean as boolean
4 open util/relation as relation
5 open structure
6 open inference_help
7
8 pred setupLeafLinks(s: Stratum, c: Component)
9 {
10   -- make sure we have enough link ends
11   ensureLinkEndsExist[s, c]
12
13   let
14     idToPorts = c.myPorts.objects_e[s],
15     inferred =
16       { p1, p2: ran[idToPorts] |
17         idToPorts.p1 -> idToPorts.p2 in c.links }
18   {
19     -- copy over the links
20     c.inferredLinks.s = inferred
21
22     -- copy over the sets
23     all cport: c.ports.s |
24       let
25         end = getComponentLinkEnd[idToPorts.cport],
26         errors =
27           some other: c.ports.s |
28             cport -> other in c.inferredLinks.s and
29             (cport.required.c.s != other.provided.c.s or
30              cport.provided.c.s != other.required.c.s)
31       {
32         -- propagate the set value into the inferred value
33         cport.required.c.s = cport.setRequired
34         cport.provided.c.s = cport.setProvided
35
36         -- we have no errors if all linked match up exactly
37         s -> c in end.linkError <=> errors
38       }
39   }
40 }
41
42 pred setupCompositeLinks(s: Stratum, c: Component)
43 {
44   ensureLinkEndsExist[s, c]
45
46   let
47     allPorts = c.ports.s,
48     allParts = c.parts.s,
49     idToPorts = c.myPorts.objects_e[s],
50     idToParts = c.myParts.objects_e[s],
51     -- flatten everything into a LinkEnd->LinkEnd structure so we can
52     -- use transitive closure to navigate
53     portToPort = makePortToPort[s, c],
54     partInternal = makePartInternal[s, c],
55     partToPart = makePartToPart[s, c],
56     portToPart = makePortToPart[s, c],
57     partToPart = "portToPart",
58     -- we connect by going from a port to a port,
59     -- or from a port to part to possibly the other side of the part
60     -- and then onto another part etc, until we get to a final part,
61     -- or to a final port
62     fromPortToPart = portToPart.*(partInternal.partToPart),
63     fromPartToPort = "fromPortToPart",
64     fromPartToPart = partToPart.*(partInternal.partToPart),
65     -- harsh allows us to bounce around looking for any possibly connected other elements.
66     -- used to disallow inferredLinks via fainting
67     harshFromPortToAny =
68       portToPart.*(portToPart + partToPart + portToPort + partInternal + partToPart),
69     fromPortToPort = portToPort + fromPortToPart.partInternal.partToPort
70   {
71     -- set up the inferred links, propagating the constraints to the next level
72     propagateInferredCompositeLinks[
73       s, c, harshFromPortToAny, fromPortToPort,
74       partInternal, portToPort]
75
76     -- get the provided and required interfaces of ports
77     all cport: allPorts |
78       let
79         end = getComponentLinkEnd[idToPorts.cport],
80
81         infReq = cport.required.c.s,
82         reqEnds = end.fromPortToPart,
83         requiresFromEnds =
```

```

84     { r: Interface |
85       some ce: reqEnds |
86       r in ce.getPortInstanceRequired [s, c] },
87   matchingRequires = extractLowestCommonSubtypes [s, requiresFromEnds],
88
89   infProv = cport.provided.c.s,
90   provEnds = end.fromPortToPort - end +
91   { e: PartLinkEnd |
92     e in end.fromPortToPart and no e.partInternal
93   },
94   providesFromEnds =
95   { p: Interface |
96     {
97       (some e: provEnds & ComponentLinkEnd |
98         p in e.getPort [s, c].required.c.s)
99       or
100       (some e: provEnds & PartLinkEnd |
101         p in e.getPortInstanceProvided [s, c])
102     }
103   },
104   matchingProvides = extractHighestCommonSupertypes [s, providesFromEnds]
105 {
106   infReq = matchingRequires
107   infProv = matchingProvides
108
109   s -> c not in end.linkError <=>
110   (oneToOneProvidedMappingExists [s, c, infProv, reqEnds] and
111    oneToOneRequiredMappingExists [s, c, infReq, reqEnds])
112 }
113
114 -- enforce the constraints for each port instance
115 all cpart: allParts,
116 cport: cpart.partType.ports.s |
117 let
118   type = cpart.partType,
119   end = getPartLinkEnd [cpart.portMap[s].cport, idToParts.cpart]
120 {
121
122   {
123     let
124       infReq = end.getPortInstanceRequired [s, c],
125       infProv = end.getPortInstanceProvided [s, c],
126       terminalEnds = end.fromPartToPort +
127       { e: PartLinkEnd |
128         e in end.fromPartToPart and no e.partInternal
129       },
130       provFromTerminalEnds =
131       { p: Interface |
132         {
133           (some e: terminalEnds & ComponentLinkEnd |
134             p in e.getPort [s, c].provided.c.s)
135           or
136           (some e: terminalEnds & PartLinkEnd |
137             p in e.getPortInstanceRequired [s, c])
138         }
139       },
140       allEnds = end.fromPartToPort +
141       { e: PartLinkEnd |
142         e in end.fromPartToPart
143       },
144       matchingTerminalProvides =
145       extractLowestCommonSubtypes [s, provFromTerminalEnds]
146     {
147       s -> c not in end.linkError <=>
148       {
149         no end.partInternal =>
150         providesEnough [s, infProv, matchingTerminalProvides]
151         oneToOneRequiredMappingExists [s, c, infProv, allEnds]
152         oneToOneProvidedMappingExists [s, c, infReq, allEnds]
153       }
154     }
155   }
156 }
157 }
158 }
159
160 pred linksAreWellFormed (s: Stratum, c: Component)
161 {
162   let
163     allPorts = c.ports.s,
164     allParts = c.parts.s,
165     idToParts = c.myParts.objects_e[s],
166     portToPort = makePortToPort [s, c]
167   {
168     -- enforce that no ports connect directly to each other
169     -- as this can lead to indeterminate interface assignment
170     isTrue [c.isComposite] =>
171       no portToPort
172
173     -- enforce the constraints for each port
174     all cport: allPorts |

```

```

175     let
176       infProv = cport.provided.c.s,
177       infReq = cport.required.c.s,
178       idToPorts = c.myPorts.objects_e[s],
179       end = getComponentLinkEnd[idToPorts.cport],
180       amHome = c.home = s,
181       setInterfaces = cport.(setProvided + setRequired)
182     {
183       -- check any set values only if we are "home"
184       (amHome and some setInterfaces) =>
185       {
186         infProv = cport.setProvided
187         infReq = cport.setRequired
188       }
189
190       -- must have some interfaces
191       some infProv + infReq
192       s -> c not in end.linkError
193     }
194
195     -- enforce the constraints for each port instance
196     all cpart: allParts,
197     cport: cpart.portType.ports.s |
198     let
199       end = getPartLinkEnd[cpart.portMap[s].cport, idToParts.cpart],
200       infReq = end.getPortInstanceRequired[s, c],
201       infProv = end.getPortInstanceProvided[s, c]
202     {
203       -- must have some interfaces
204       some infProv + infReq
205       s -> c not in end.linkError
206     }
207   }
208 }
209
210
211 -- set up the inferred links for this component for a leaf, just use the links
212 -- for a composite, trace through from port to port, but only infer a link if there
213 -- is no terminal part involve anywhere
214 pred propagateInferredCompositeLinks (
215   s: Stratum,
216   c: Component,
217   harshFromPortToAny: ComponentLinkEnd -> LinkEnd,
218   fromPortToPort: ComponentLinkEnd -> ComponentLinkEnd,
219   partInternal: PartLinkEnd -> PartLinkEnd,
220   portToPort: ComponentLinkEnd -> ComponentLinkEnd)
221 {
222   let
223     idToPorts = c.myPorts.objects_e[s],
224     allPorts = c.ports.s,
225     terminateInternallyIDs =
226     { id: dom[idToPorts] & PortID |
227       some end: PartLinkEnd |
228         let instance = end.getPortInstance[s, c],
229         cport = dom[instance],
230         cpart = ran[instance]
231       {
232         getComponentLinkEnd[id] in harshFromPortToAny.end
233         no end.partInternal
234         -- only provided terminals break linking
235         some cport.provided.(cpart.portType).s
236       }
237     }
238   {
239     -- find all port->port combinations that go through a leaf part and link up
240     -- but which don't have a termination on a provided port instance interface
241     let inferred =
242     { p1, p2: Port |
243       some end: dom[fromPortToPort] | let other = end.fromPortToPort
244       {
245         disj[end, other]
246         p1 = idToPorts[end.linkPortID]
247         p2 = idToPorts[other.linkPortID]
248         -- if we can reach a port which links internally,
249         -- do not create an alias
250         no (end + other).portToPort.linkPortID & terminateInternallyIDs
251       }
252     } |
253     c.inferredLinks.s = inferred
254   }
255 }

```

---

# Inference\_help.als

Listing 7: inference\_help.als

```
1 module inference_help
2
3 open structure
4 open util/boolean as boolean
5
6
7 pred providesEnough(s: Stratum, provided: set Interface, required: set Interface)
8 {
9   all prov: provided |
10     one req: required |
11       req in prov.*(superTypes.s)
12
13   -- ensure that it works the other way around
14   all req: required |
15     one prov: provided |
16       req in prov.*(superTypes.s)
17 }
18
19 pred oneToOneProvidedMappingExists[s: Stratum, c: Component, provided: set Interface, ends: LinkEnd]
20 {
21   all end: ends & ComponentLinkEnd |
22     oneToOneMappingExists[s, provided, end.getPort[s, c].required.c.s]
23
24   all end: ends & PartLinkEnd |
25     oneToOneMappingExists[s, provided, end.getPortInstanceProvided[s, c]]
26 }
27
28 pred oneToOneRequiredMappingExists[s: Stratum, c: Component, required: set Interface, ends: LinkEnd]
29 {
30   all end: ends & ComponentLinkEnd |
31     oneToOneMappingExists[s, required, end.getPort[s, c].provided.c.s]
32
33   all end: ends & PartLinkEnd |
34     oneToOneMappingExists[s, required, end.getPortInstanceRequired[s, c]]
35 }
36
37 pred oneToOneMappingExists[s: Stratum, a: set Interface, b: set Interface]
38 {
39   all aa: a |
40     one bb: b |
41       bb in expand[s, aa]
42
43   -- ensure that it works the other way around
44   all bb: b |
45     one aa: a |
46       aa in expand[s, bb]
47 }
48
49 fun extractHighestCommonSupertypes(s: Stratum, require: Interface): set Interface
50 {
51   let
52     -- map is an interface in require (i) with all matching interfaces in require (e)
53     map =
54       { i: require, e: require |
55         some expand[s, i] & expand[s, e] },
56     highestCommonSupertypes =
57       {
58         super: Interface |
59           some i: require |
60             super = highestCommonSupertype[s, map[i]]
61       }
62   {
63     highestCommonSupertypes
64   }
65 }
66
67 fun highestCommonSupertype(s: Stratum, required: set Interface): lone Interface
68 {
69   { i: Interface |
70     {
71       required in *(superTypes.s).i
72       no sub: superTypes.s.i |
73         required in *(superTypes.s).sub
74     }
75   }
76 }
77
78 fun extractLowestCommonSubtypes(s: Stratum, require: Interface): set Interface
79 {
80   let
81     -- map is an interface in require (i) with all matching interfaces in require (e)
82     map =
83       { i: require, e: require |
```

```

84     some expand[s, i] & expand[s, e] },
85     lowestCommonSubtypes =
86     {
87       sub: Interface |
88         some i: require |
89         sub = lowestCommonSubtype[s, map[i]]
90     }
91   {
92     lowestCommonSubtypes
93   }
94 }
95
96 fun lowestCommonSubtype(s: Stratum, required: set Interface): lone Interface
97 {
98   { i: Interface |
99     {
100       required in i.*(superTypes.s)
101       no super: i.superTypes.s {
102         required in super.*(superTypes.s)
103       }
104     }
105   }
106 }
107
108 fun expand(s: Stratum, i: Interface): set Interface
109 {
110   -- expand forms the full expanded supertype and subtype hierarchy
111   i.*(superTypes.s) + ~(superTypes.s).i
112 }
113
114 -- a generator axiom to ensure that we have a unique link end per port, or port instance
115 pred ensureLinkEndsExist(s: Stratum, c: Component)
116 {
117   let
118     idToPorts = c.myPorts.objects_e[s],
119     idToParts = c.myParts.objects_e[s]
120   {
121     -- set up the linkends
122     -- ensure all ports have a link end
123     all portID: dom[idToPorts] |
124       one l: ComponentLinkEnd |
125         l.linkPortID = portID
126
127     -- ensure all part/ports have a link end
128     all ppart: c.parts.s |
129       let partID = idToParts.ppart |
130         all portID: ppart.portMap[s].Port |
131           one l: PartLinkEnd |
132             l.linkPortID = portID and l.linkPartID = partID
133   }
134 }
135
136 fun makePortToPort(s: Stratum, c: Component): ComponentLinkEnd -> ComponentLinkEnd
137 {
138   isTrue[c.isComposited] =>
139   { p1, p2: ComponentLinkEnd |
140     some end: c.connectors.s.ends | let other = end.otherEnd
141     {
142       disj[end, other]
143       end + other in ComponentConnectorEnd
144       end.portID = p1.linkPortID
145       other.portID = p2.linkPortID
146     }
147   }
148   else
149   { p1, p2: ComponentLinkEnd |
150     some end: dom[c.links], other: c.links[end]
151     {
152       -- these are disjoint because of a clause in structure.als
153       end = p1.linkPortID
154       other = p2.linkPortID
155     }
156   }
157 }
158
159 fun makePartInternal(s: Stratum, c: Component): PartLinkEnd -> PartLinkEnd
160 {
161   let
162     idToParts = c.myParts.objects_e[s] |
163   { p1, p2: PartLinkEnd |
164     some partID: dom[idToParts] |
165     let
166       realPart = idToParts[partID],
167       realType = realPart.partType,
168       inferredOneWay = realType.inferredLinks.s,
169       inferred = inferredOneWay + ~inferredOneWay,
170       idToPorts = realPart.portMap[s],
171       realPort = idToPorts[p1.linkPortID]
172     {
173       disj[p1, p2]
174       p1.linkPartID = partID

```

```

175         p2.linkPartID = partID
176         realPort in dom[inferred]
177         idToPorts[p2.linkPortID] = inferred[realPort]
178     }
179 }
180 }
181
182 fun makePartToPart(s: Stratum, c: Component): PartLinkEnd -> PartLinkEnd
183 {
184     { p1, p2: PartLinkEnd |
185         some end: c.connectors.s.ends | let other = end.otherEnd
186         {
187             disj[end, other]
188             end.portID = p1.linkPortID
189             end.partID = p1.linkPartID
190             other.portID = p2.linkPortID
191             other.partID = p2.linkPartID
192         }
193     }
194 }
195
196
197 fun makePortToPart(s: Stratum, c: Component): ComponentLinkEnd -> PartLinkEnd
198 {
199     { p1: ComponentLinkEnd, p2: PartLinkEnd |
200         some end: c.connectors.s.ends | let other = end.otherEnd
201         {
202             end in ComponentConnectorEnd
203             end.portID = p1.linkPortID
204             other.portID = p2.linkPortID
205             other.partID = p2.linkPartID
206         }
207     }
208 }

```

---