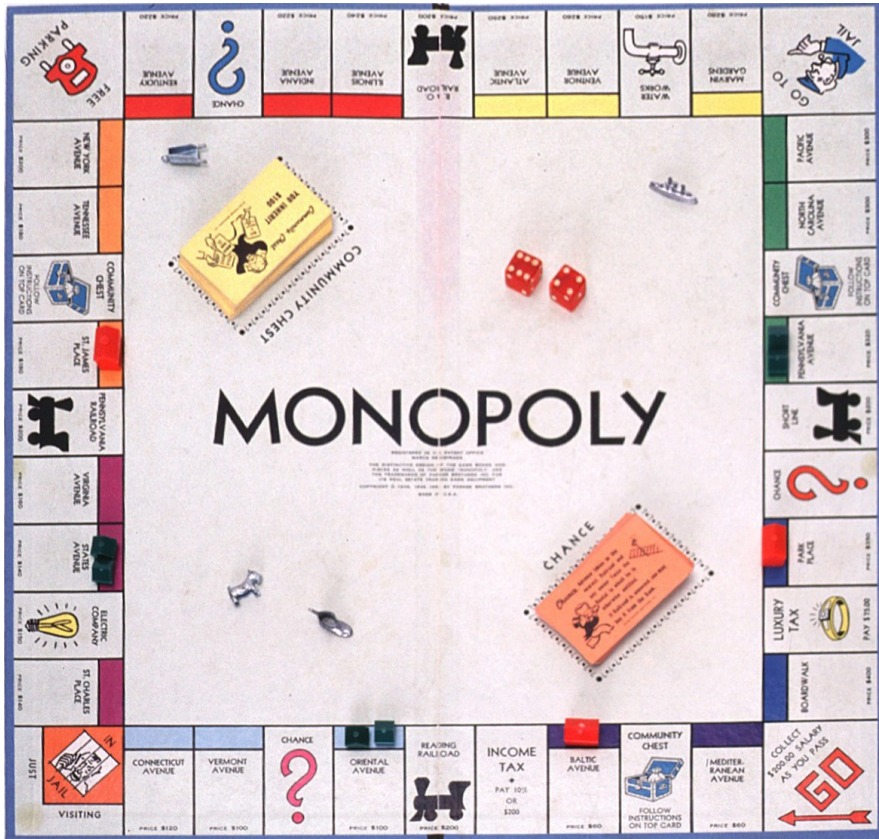


MONOPOLY

Week 3

(Chapter 25, except Appendix)

Monopoly



Board Game developed during the Great Depression

- 22 streets in Atlantic City (New Jersey), divided into 8 color groups; player must own all of a color group to build hotels
- 4 railways, player collects \$25 rent if she owns one station, \$50 for two, \$100 for three and \$200 for all four
- 2 utilities, rent is four times the dice value if one utility is owned, but ten times if both are owned

What is a monopoly?

	Perfect Competition	Monopoly
Industry structure	Fragmented; No firm has significant market share	Concentrated; One firm dominates
Pricing	Price takers	Price maker
Barriers to entry	No	Significant
Herfindahl index	0	1

Herfindhal index

$$H = \sum_{i=1}^N s_i^2$$

- Industry of N firms; s_i : market share of firm i
- Measures market concentration: 0 (most competitive) to 1 (no competition)
- United States Department of Justice's Horizontal Merger Guideline:
 - H below 0.15: unconcentrated market
 - H between 0.15 to 0.25: moderate concentration
 - H above 0.25: high concentration
 - Singapore's retail petrol market: 0.31 (in 2011)
- Equivalent to Simpson diversity index in ecology and inverse participation ratio (IPR) in physics

Consider the following monopoly

- Only airline serving the only airport in Island *Baro Baro*

- Linear market demand curve $Q = 50 - \frac{P}{40,000}$

- Total cost $TC = 10,000Q^2 + 50,000$

- Hence marginal cost $MC = \frac{dTC}{dQ} = 20,000Q$

Total Revenue and Marginal Revenue

- The demand for air travel is $Q = 50 - \frac{P}{40,000}$
- The inverse demand function is therefore $P = 2,000,000 - 40,000Q$
- Thus we can write down TR in terms of Q : $TR = PQ = (2,000,000 - 40,000Q)Q$
- Thus, $MR = \frac{dTR}{dQ} = 2,000,000 - 80,000Q$

MR for Linear Demand Curve

- More generally, the (linear) demand curve is

$$Q = a - bP$$

- The inverse demand curve is

$$P = \frac{a}{b} - \frac{Q}{b}$$

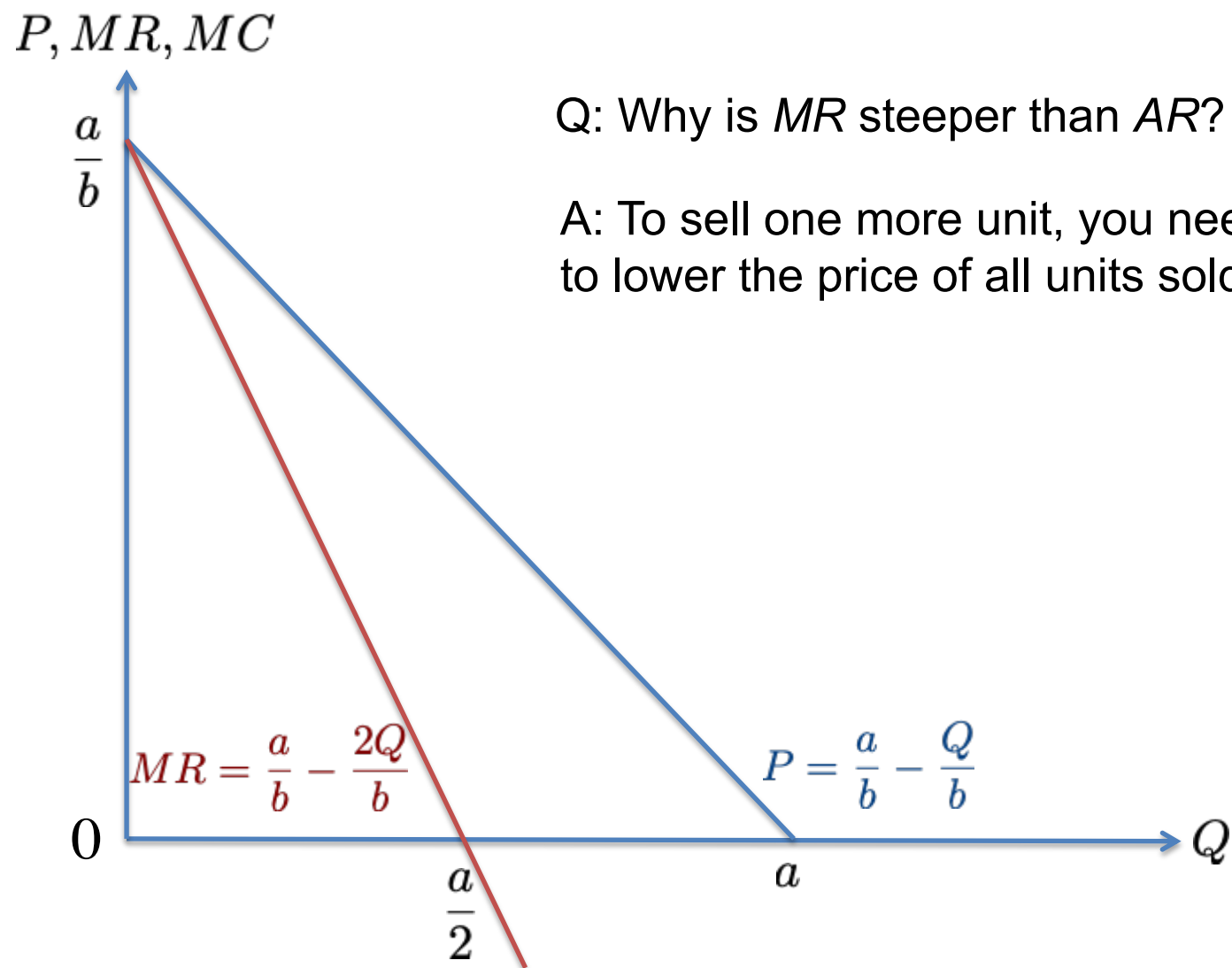
- The total revenue is

$$TR = PQ = \left(\frac{a}{b} - \frac{Q}{b}\right)Q$$

- The marginal revenue is

$$MR = \frac{a}{b} - \frac{2Q}{b} \quad (\text{linear})$$

MR for Linear Demand Curve



Profit maximizing condition: $MR=MC$

- If $MR > MC$,
 - Increasing Q increases TR faster than TC
 - If you sell a bit more, your profit will increase
 - You have not gone far enough
- If $MR < MC$,
 - Increasing Q increases TC faster than TR
 - If you sell a bit less, your profit will increase
 - You have gone too far

Profit maximizing condition: $MR=MC$

(Back to example)

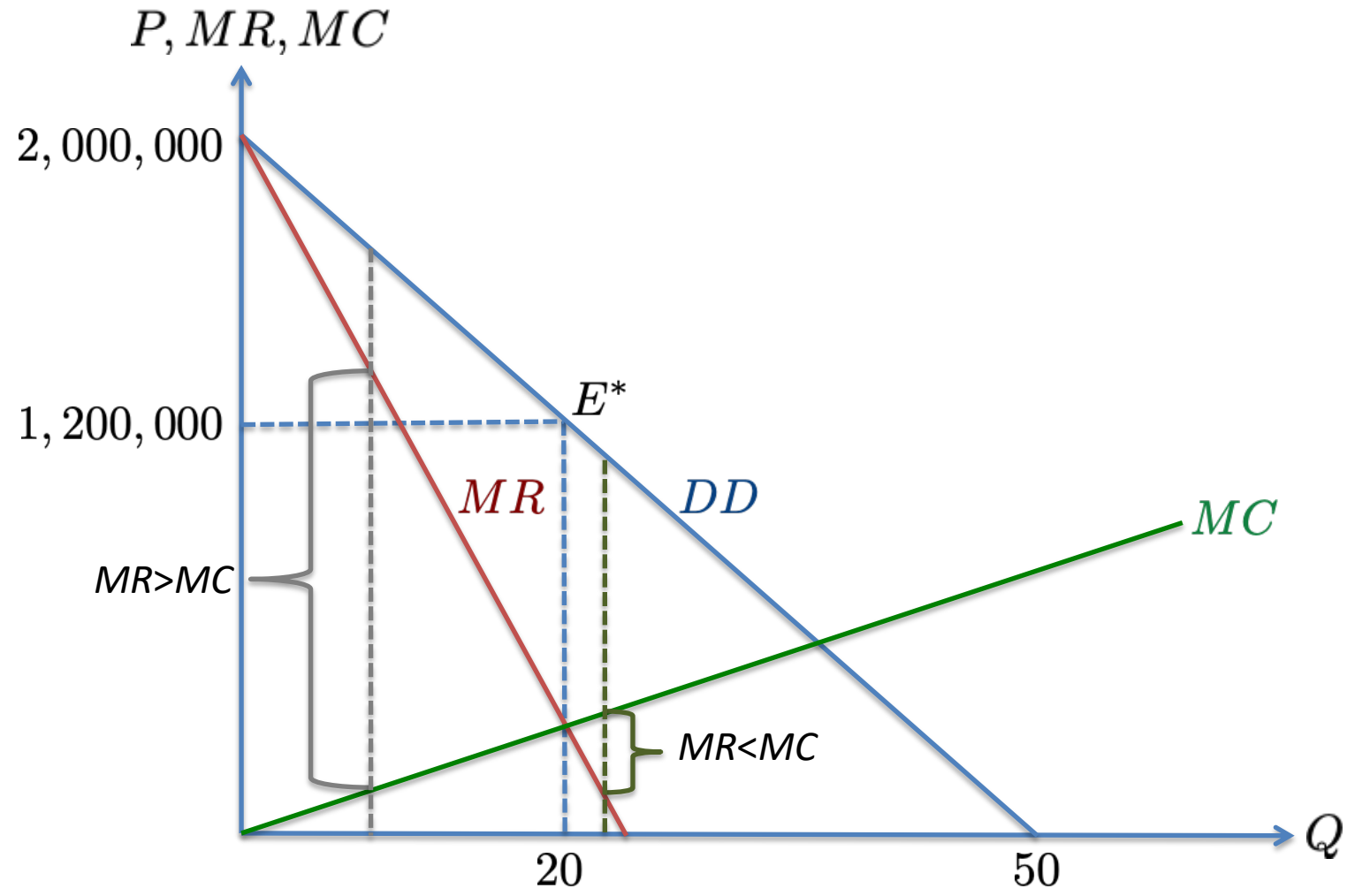
- To maximize profit, airline should set $MR = MC$

$$\Rightarrow 2,000,000 - 80,000Q = 20,000Q$$

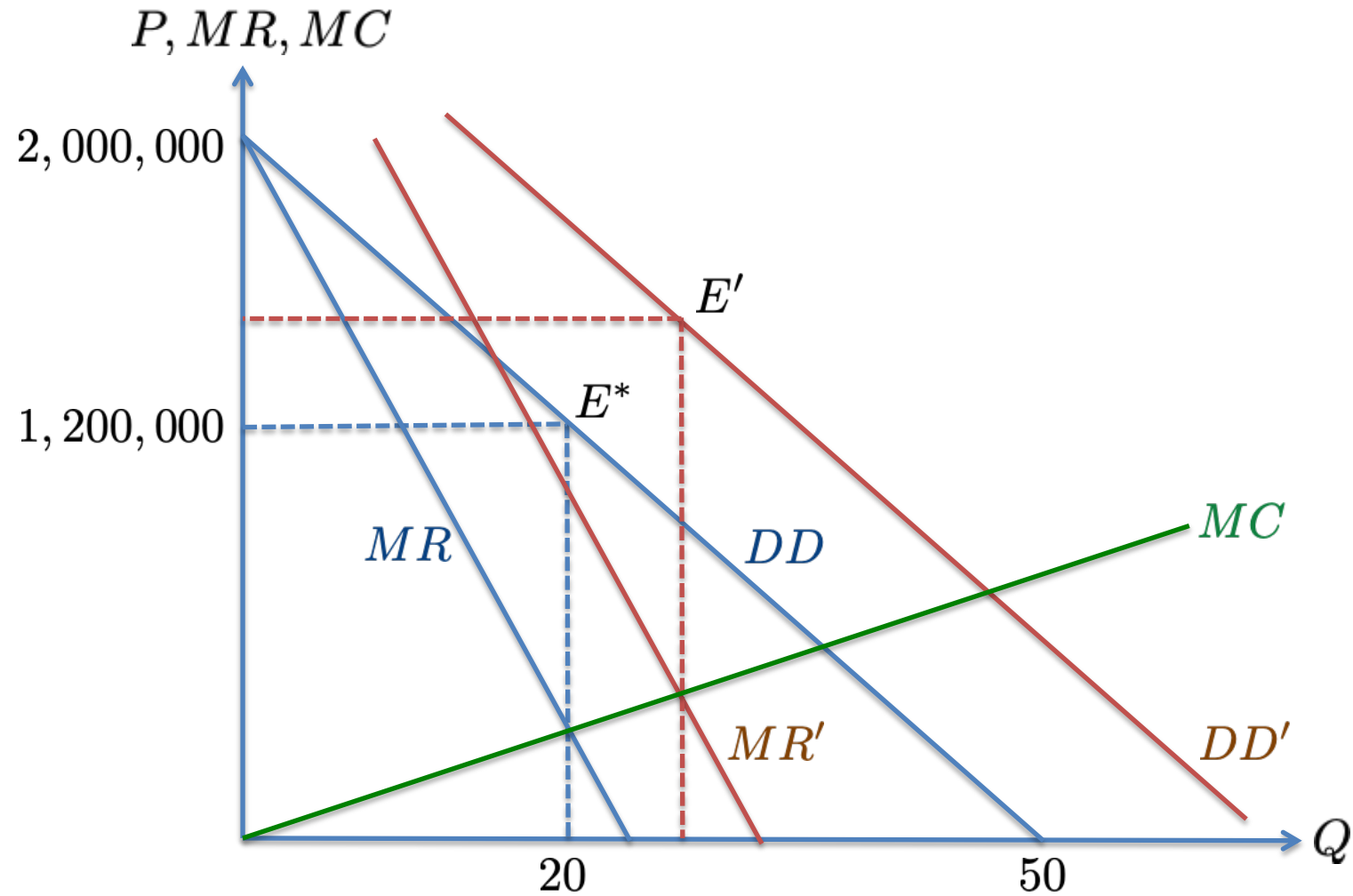
- The optimal number of trips is $Q = 20$

- The optimal price of a trip is $P = 2,000,000 - 40,000 \times 20 = 1,200,000$

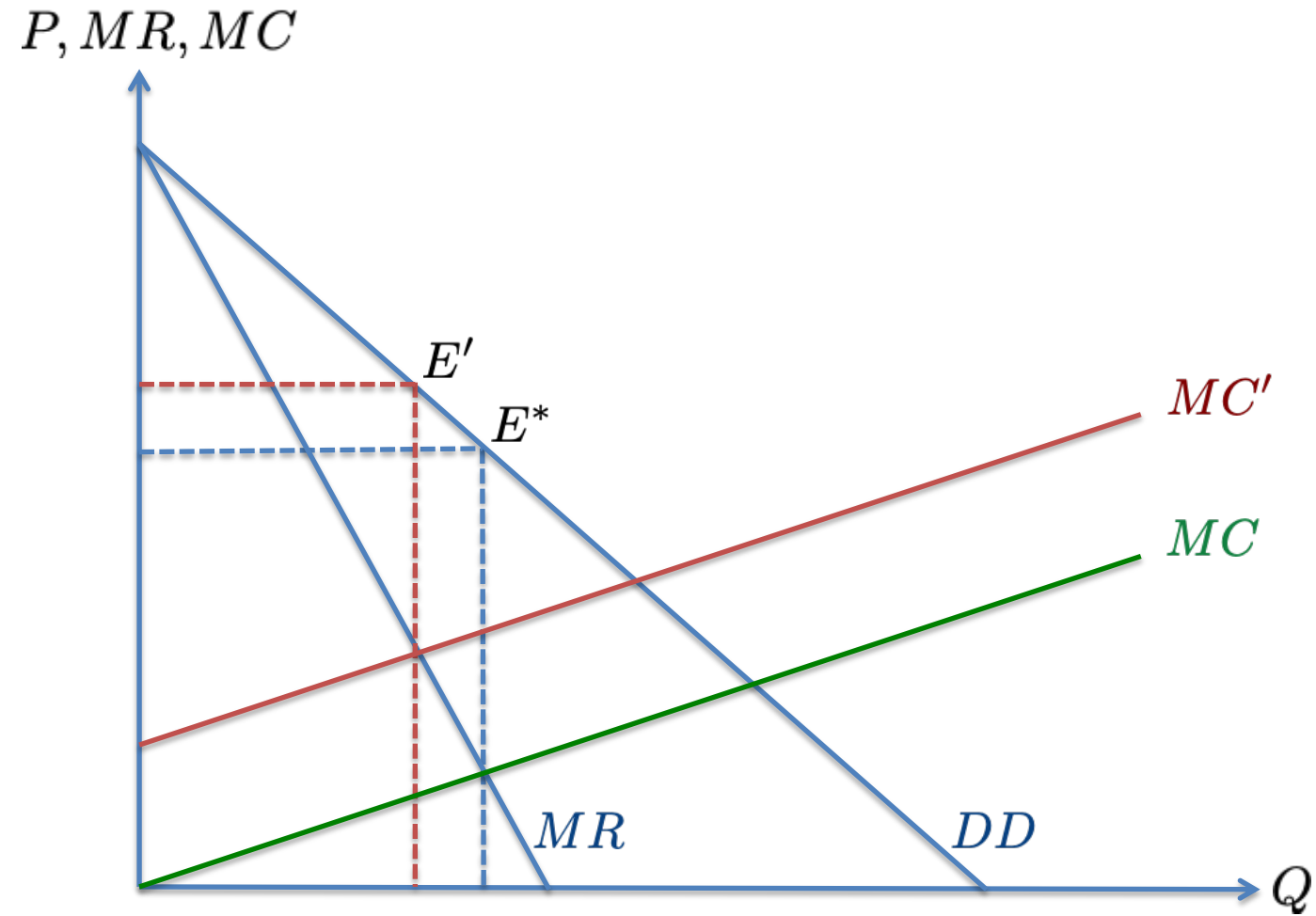
Optimal P and Q



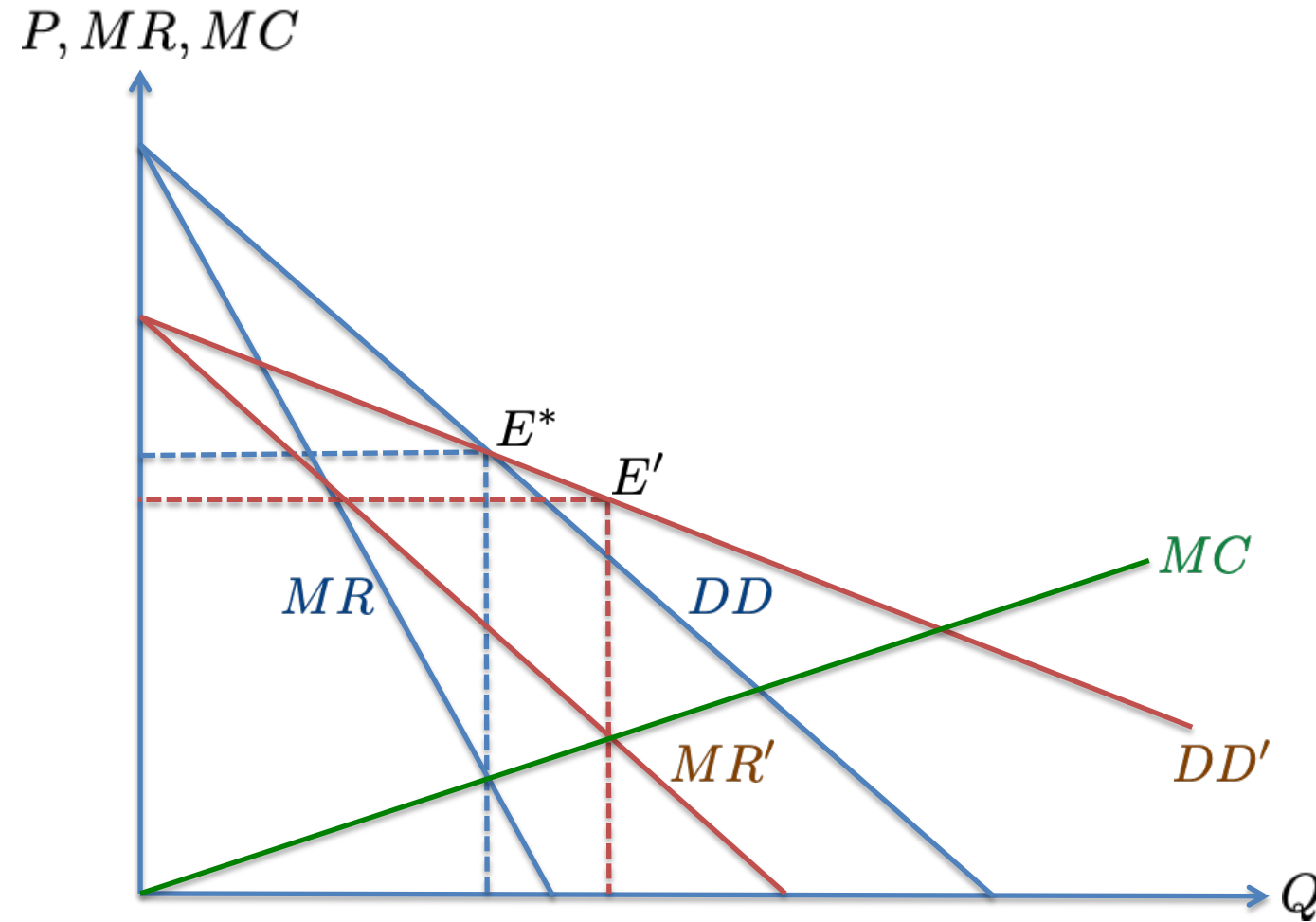
(1) What if demand increases?



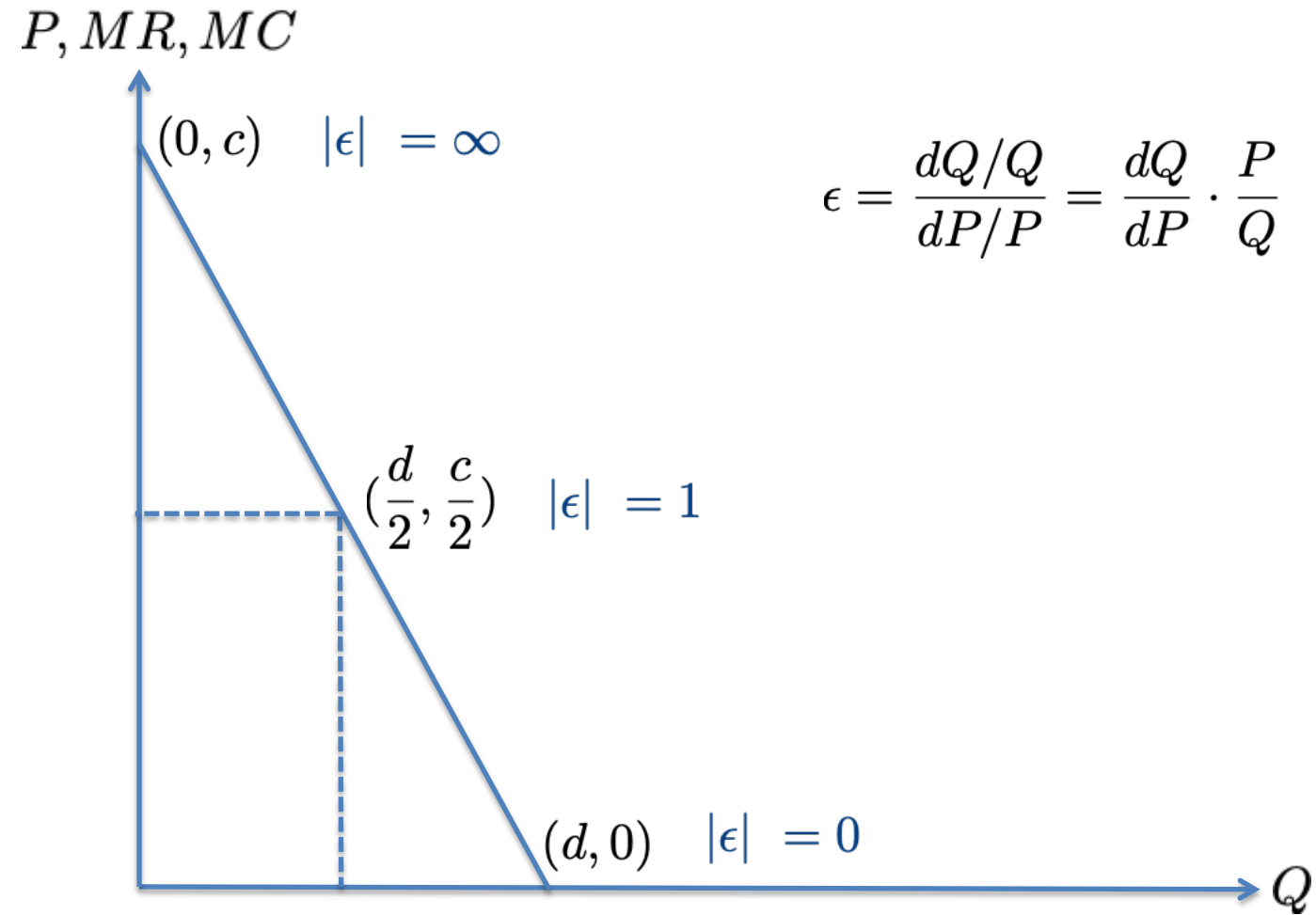
(2) What if marginal cost increases?



(3) What if demand becomes more elastic?



Price Elasticity of Demand



Inverse Elasticity Pricing Rule

- Relationship between price elasticity of demand and optimal price can be quantified

$$\frac{P^* - MC^*}{P^*} = -\frac{1}{\epsilon^*}$$

- P^* is the profit-maximizing price
- MC^* is the marginal cost at the profit-maximizing output
- ϵ^* is the price elasticity of demand at the profit-maximizing output

Deriving the Rule

$$TR = PQ$$

$$dTR = PdQ + QdP$$

$$\frac{P^* - MC^*}{P^*} = -\frac{1}{\epsilon^*}$$

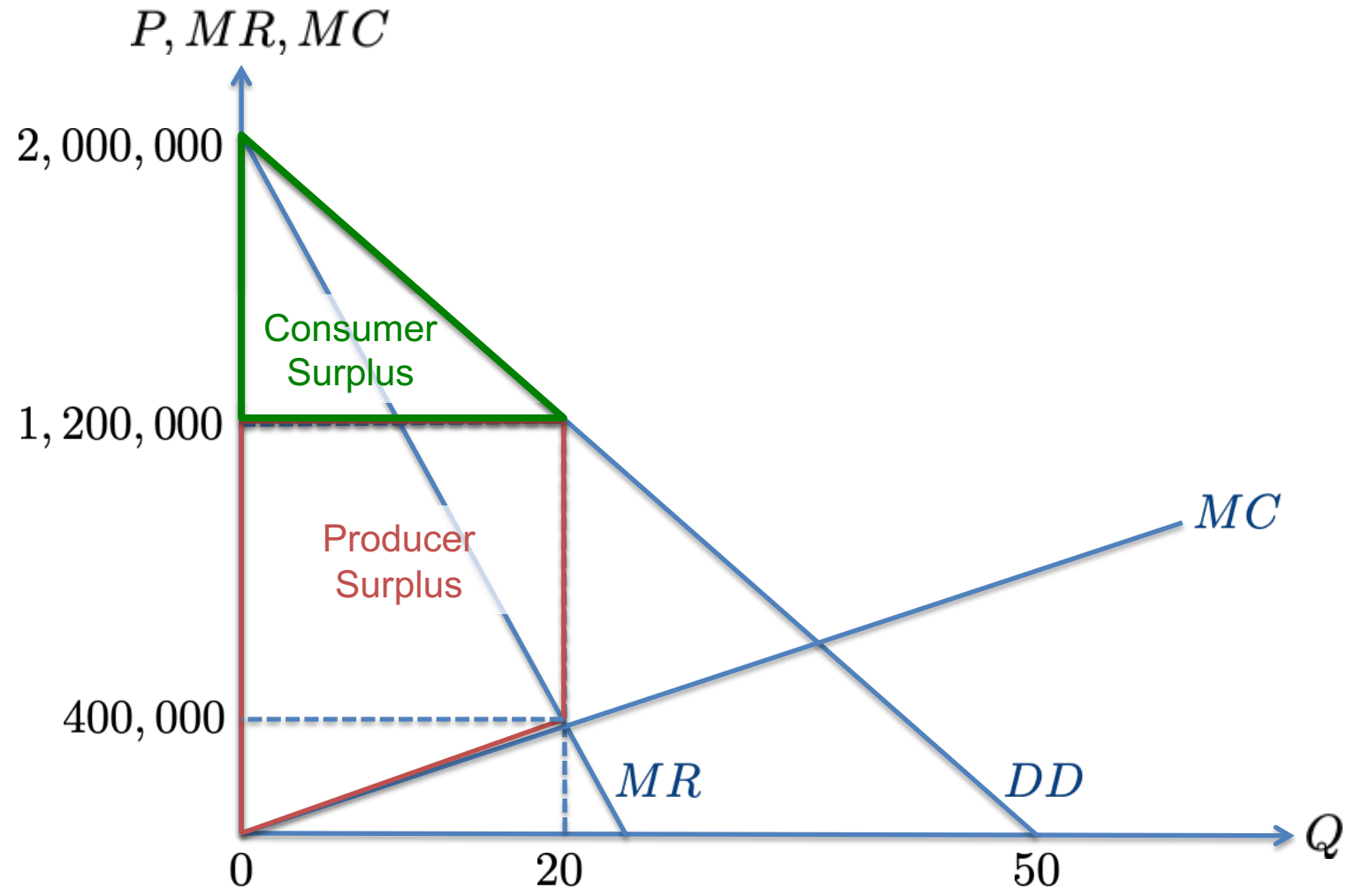
Market Power

- Generally, a monopolist's profit maximizing price is above the level of marginal cost at the profit maximizing quantity
- Generally, a monopolist's **price markup** ($P^* - MC^*$) is strictly positive
- If a firm has some control over price, it has *market power*
 - In perfectly competitive market, no firm has market power
- Even if a firm is not a monopolist, it may still have market power (next lecture)

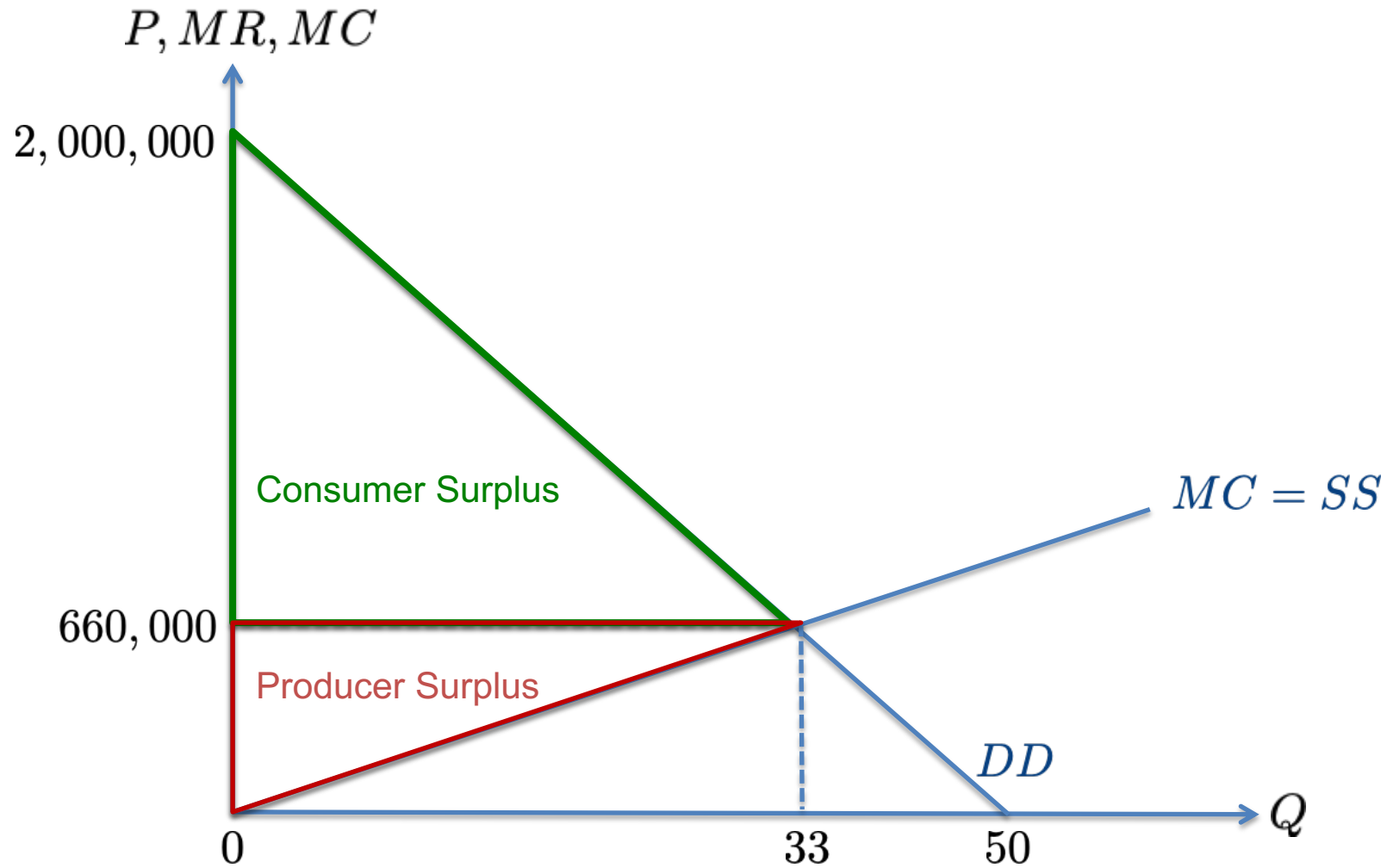
Lerner Index

- $\frac{P^* - MC^*}{P^*}$ is known as the **Lerner index** of market power
- In perfectly competitive market, every firm has a Lerner index of 0
- A firm with market power has a Lerner index above 0 and below 1

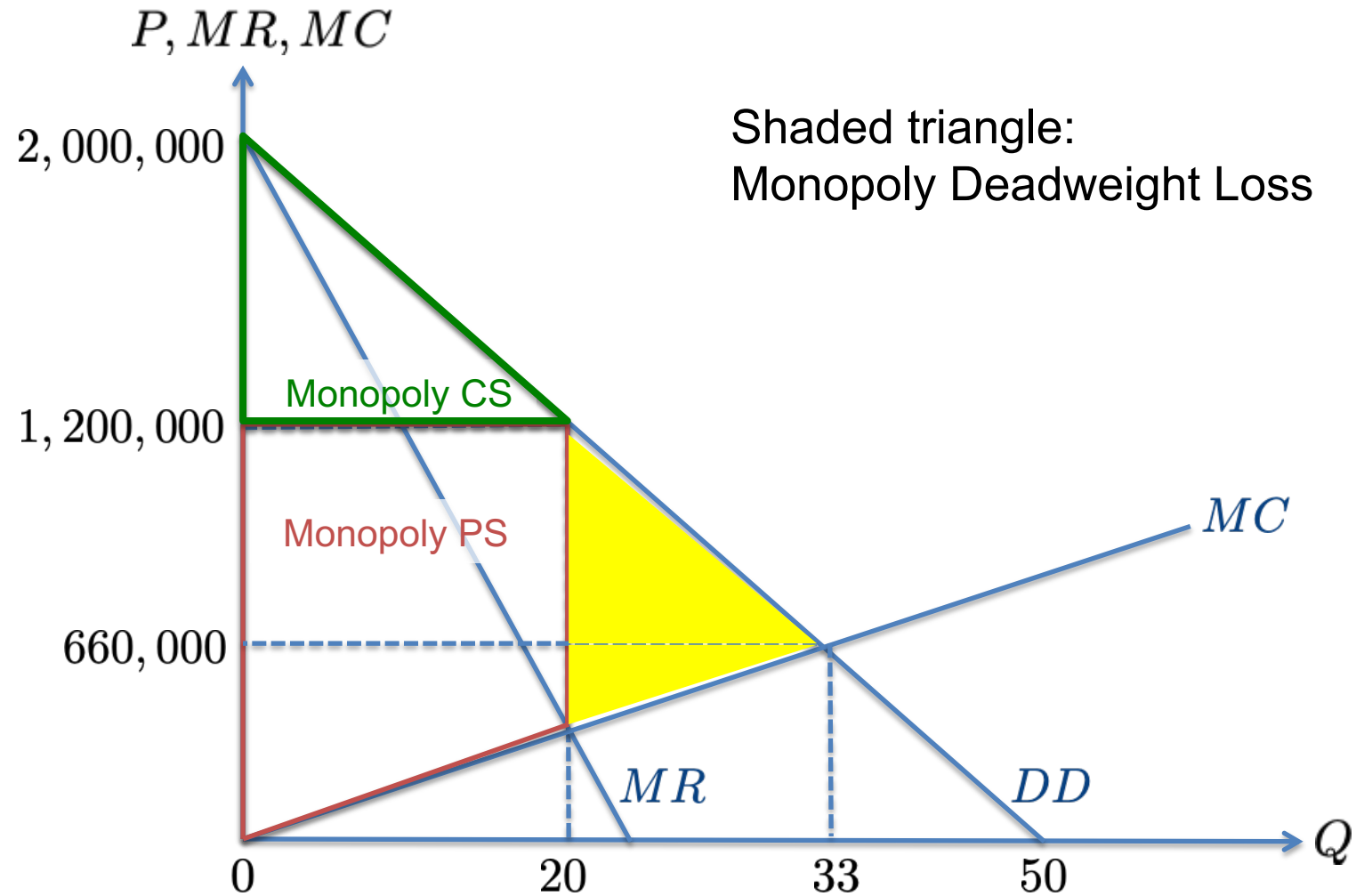
Welfare of Monopoly



CS and PS under Perfect Competition



Monopoly vs. Perfect Competition



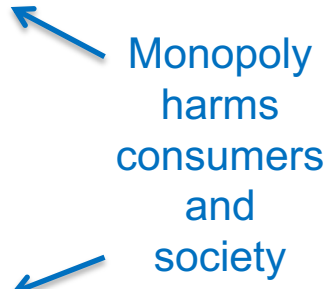
Monopoly Deadweight Loss

- DWL: Difference between the total surplus if the market were perfectly competitive and the total surplus attained in monopoly market
- Arises because a monopolist produces less quantity and sets higher price than perfectly competitive market

Monopoly vs. Perfect Competition

	Perfect Competition	Monopoly
Equilibrium price	Lower ($P=MC$)	Higher ($P>MC$)
Equilibrium quantity	Higher	Lower
Consumer surplus	Higher	Lower
Producer surplus	Lower	Higher
Total surplus	Higher	Lower

Monopoly harms consumers and society



Barriers to Entry

- Why do monopoly markets exist?
 - In perfectly competitive market, if existing firms are making profit, new entrants will enter the market and drive the profit down
- Monopoly markets have *barriers to entry*
 - i.e., Factors that allow an existing firm to earn positive profit while making it unprofitable for newcomers to enter the industry

Types of Barriers to Entry

- Legal

Patents prevent entry of generic drug companies

- Strategic

Incumbent firms actively take steps to deter entry

- Marketing
- Limit pricing
 - Incumbent firm charges a lower price before entry occurs
- Predatory pricing
 - Firm with deep pockets lowers price to drive rivals out of market

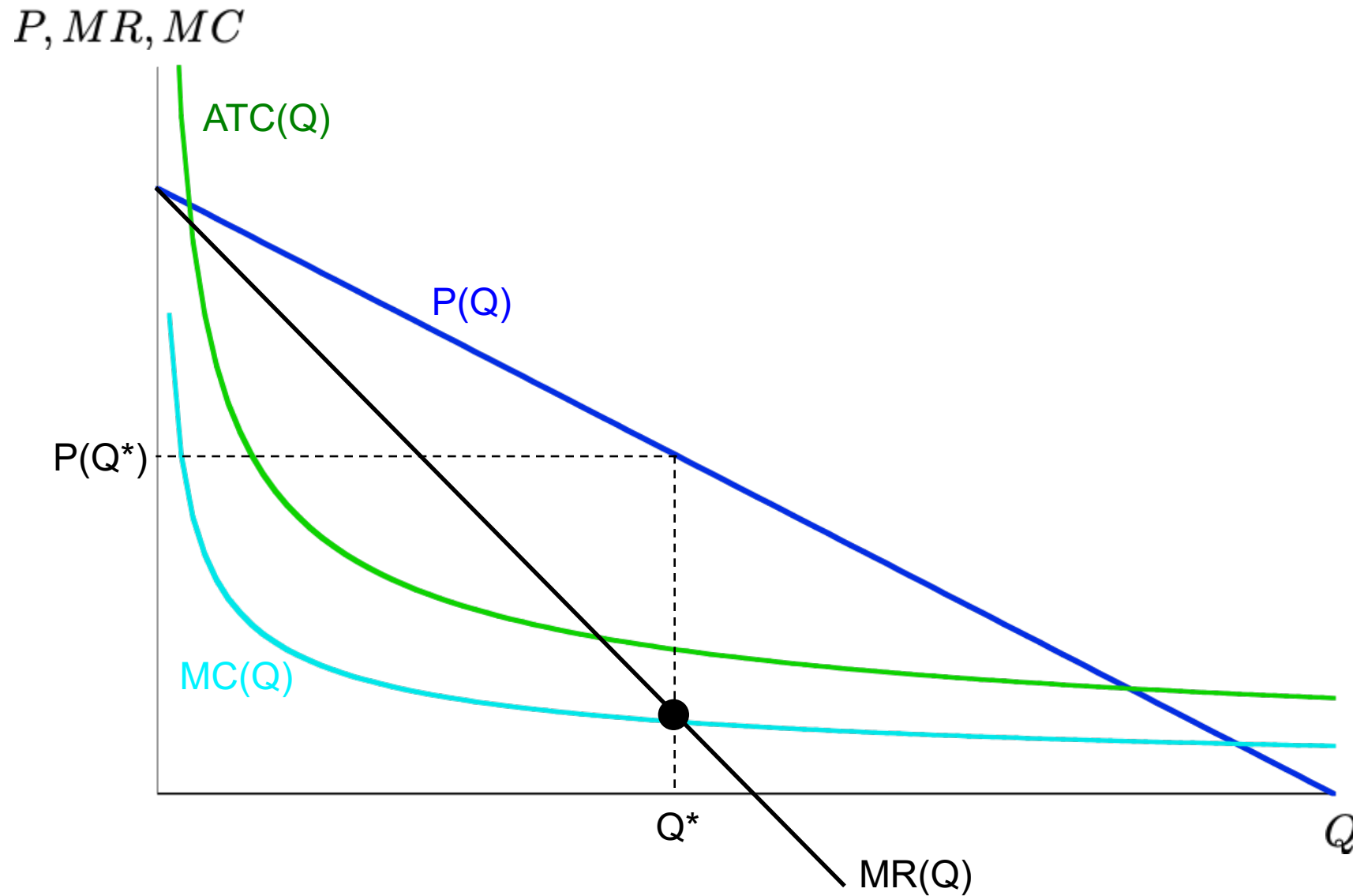
- Structural

- Positive network externality
- Natural monopoly

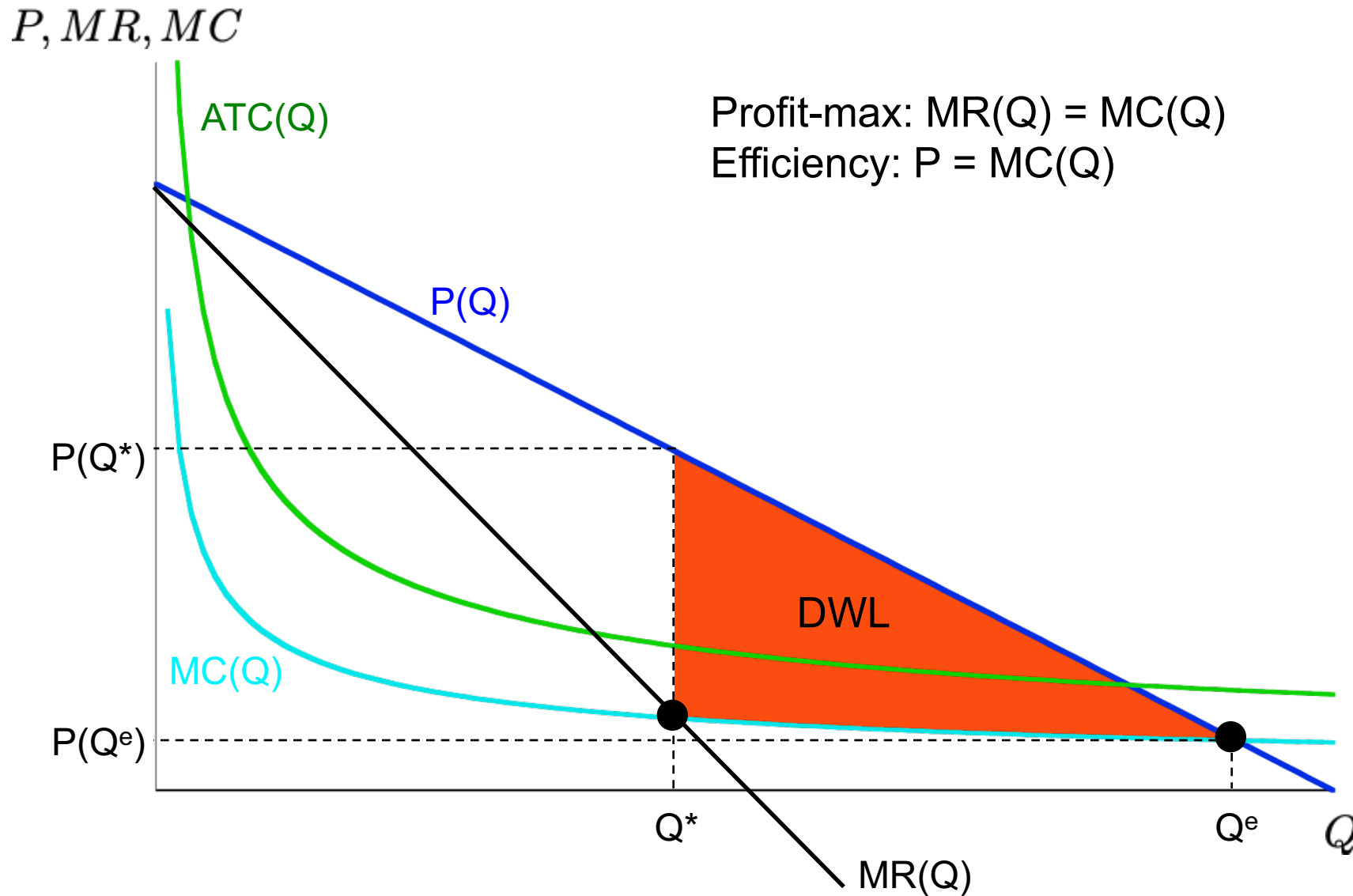
Natural Monopoly

- A market is a *natural monopoly* if the total cost a single firm would incur is less than the combined total cost that two or more firms would incur if they divide the output among them
- Economies of scale
 - High fixed cost/Low MC
 - ATC decreasing
- Demand is small (relative to cost structure)
 - TV stations in Singapore

Natural Monopoly



Inefficiency of a Natural Monopoly

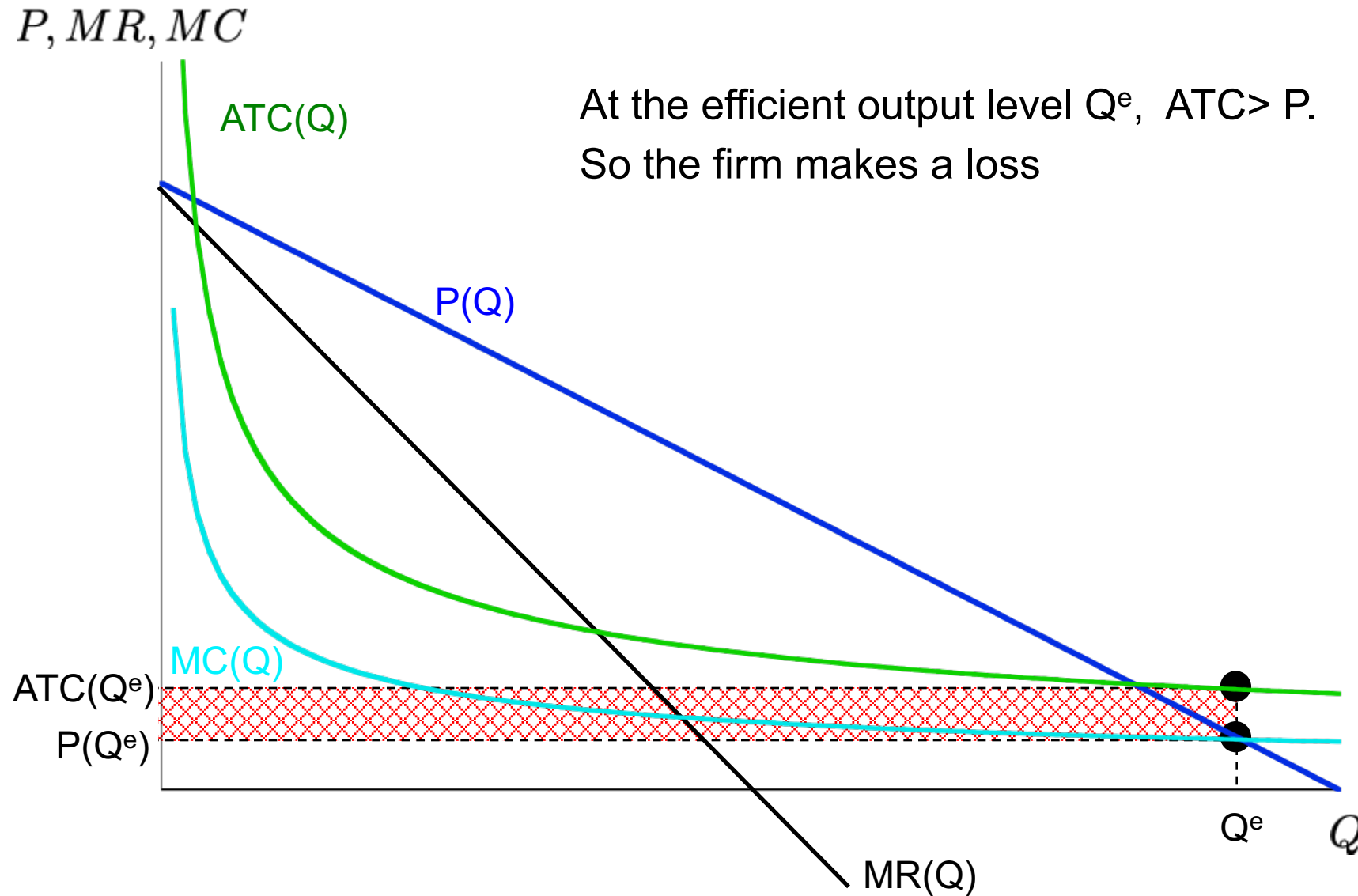


Regulating a Natural Monopoly

Solution 1: Legislate $P=MC$

- Why not command that a natural monopoly produce the efficient amount of output ($P=MC$)?
- Then the deadweight loss will be zero?

Regulating a Natural Monopoly



A Profits Tax Levied on a Monopoly

Solution 2: Levy a Profits Tax

- A profits tax levied at rate t reduces profit from $\pi(Q_{pretax}^*)$ to $(1 - t) \cdot \pi(Q_{posttax}^*)$
- Profits tax is non-distortionary tax (i.e., $Q_{pretax}^* = Q_{posttax}^*$)
- It does not create new distortions, but neither does it fix existing distortions

An Example: (a) No tax

- Suppose inverse demand function is $P = 100 - Q$, and total cost is given by $C = 10Q$
- So the monopolist's profit function is $\pi = TR - TC = PQ - 10Q = (100 - Q)Q - 10Q$

- To max profit, set
$$\frac{d\pi}{dQ} = 0$$
$$100 - 2Q - 10 = 0$$
$$Q = 45, P = 55, \pi = 2025$$

An Example: (b) Profit tax

- Suppose government set a 10% tax on the monopolist's profits.
- So the monopolist's profit function is $\pi_{posttax} = 0.9\pi$
$$= 0.9(TR - TC) = 0.9(PQ - 10Q) = 0.9(100 - Q)Q - 9Q$$
- To max profit, set $\frac{d\pi_{posttax}}{dQ} = 0$
$$90 - 1.8Q - 9 = 0$$
$$Q = 45, P = 55, \pi = 1822.5$$
- Equilibrium output and price unchanged because $90 - 1.8Q - 9 = 0.9(100 - 2Q - 10) = 0$
has the same solution as $100 - 2Q - 10 = 0$

Quantity Tax Levied on a Monopolist

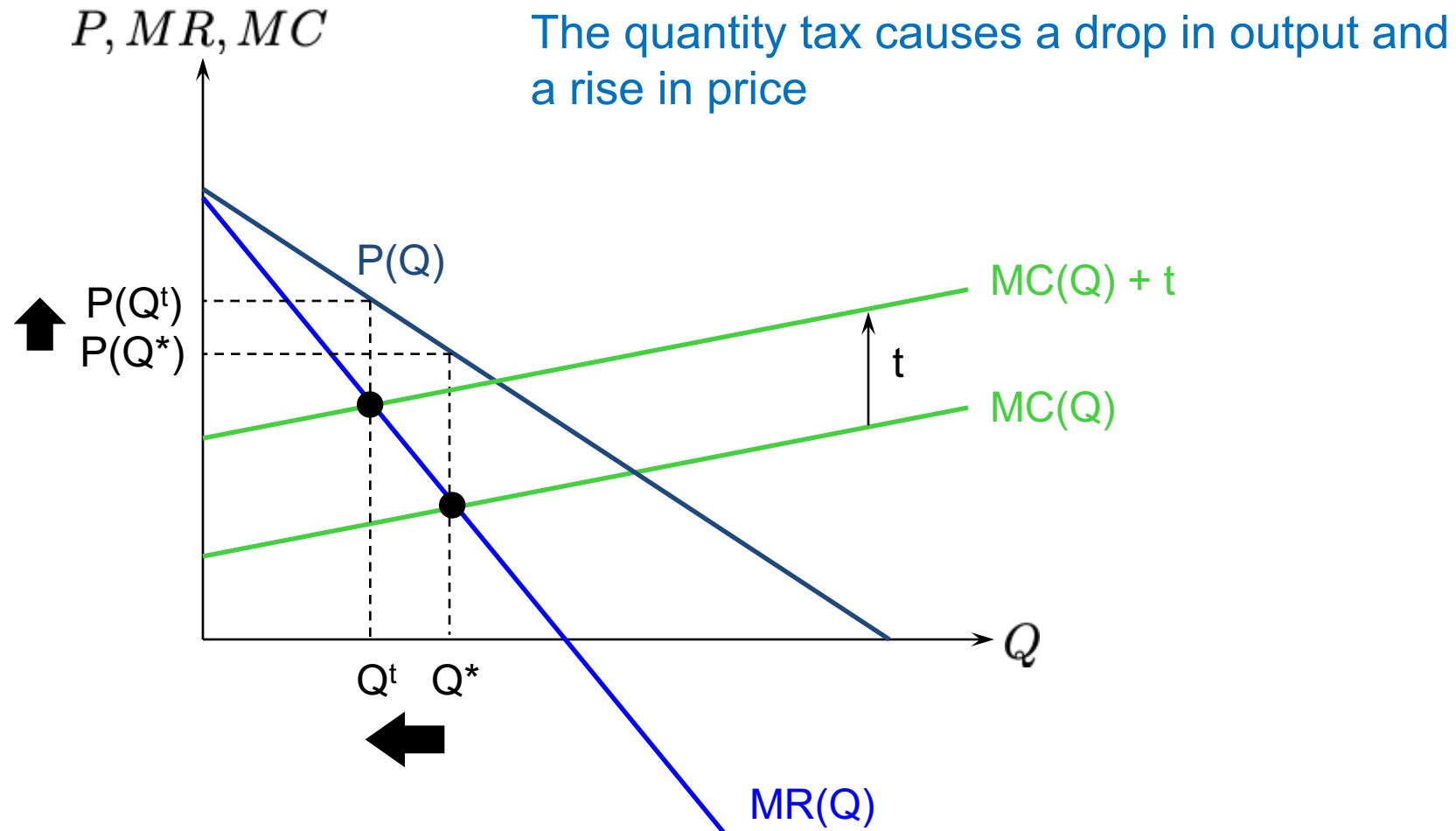
Solution 3: Levy a Quantity Tax

- A quantity tax of \$ t per unit of output raises the marginal cost of production by \$ t
- So the tax reduces the profit-maximizing output level, causes the market price to rise, and input demands to fall
- The quantity tax is distortionary

Same Example: (c) Quantity tax

- Suppose government set a tax of \$10 on each unit sold
- Now the monopolist's profit function is $\pi' = TR - TC - Tax = PQ - 10Q - 10Q = (100 - Q)Q - 20Q$
- To max profit, set $\frac{d\pi'}{dQ} = 0$
$$100 - 2Q - 20 = 0$$
$$Q = 40, P = 60, \pi = 1600$$
- Equilibrium output and price changed because the quantity tax discourages the monopolist from selling more

Quantity Tax Levied on a Monopolist



Competition Policy in Singapore

- Competition Commission Singapore (CCS) oversees anti-competitive activities
- Competition Act (effective since 2004) is the law in Singapore that protects consumers and businesses from anti-competitive activities
 - Abuse of dominance
 - Anti-competitive agreements
 - Merger

Abuse of Dominance

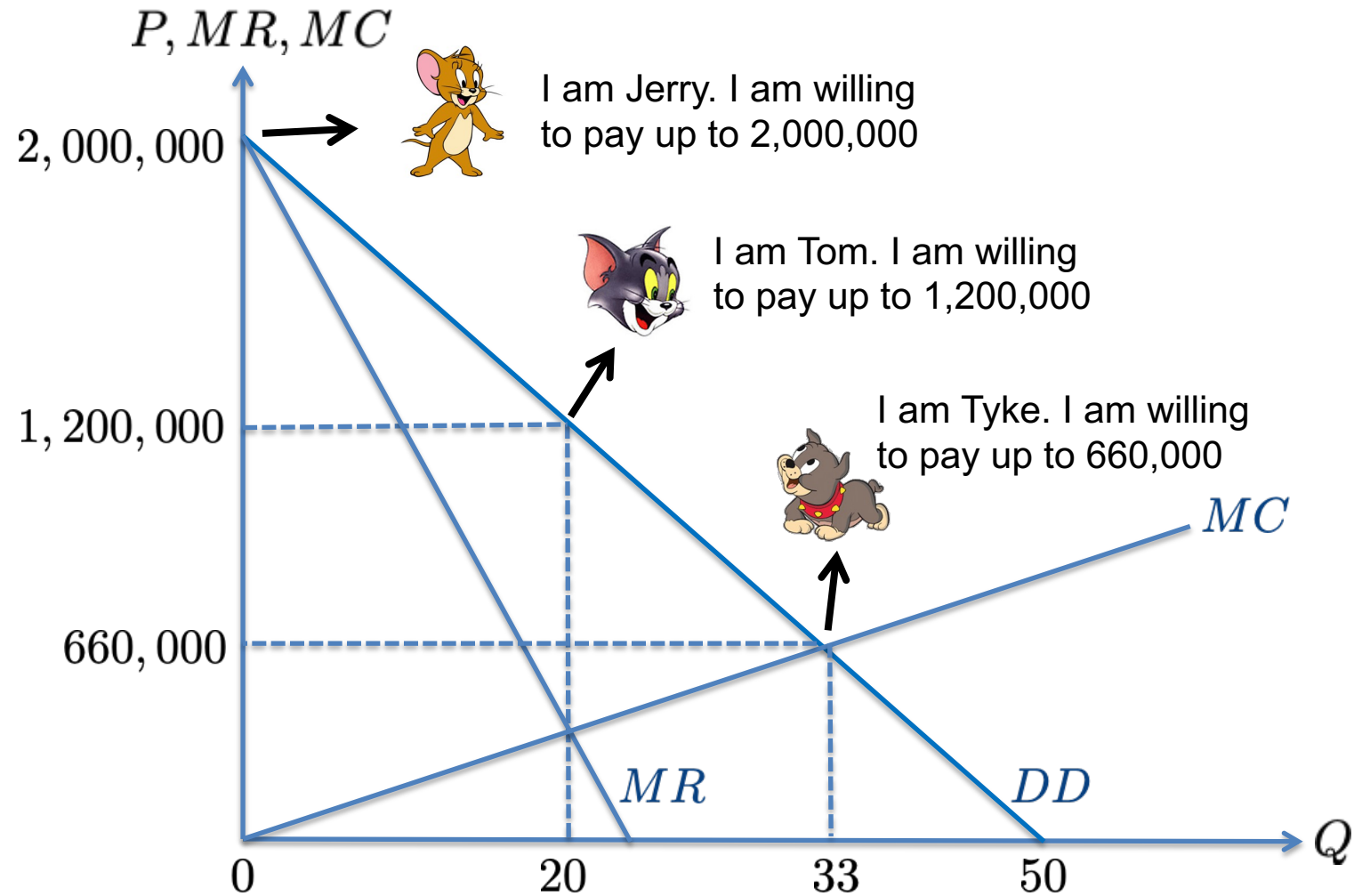
- Being a dominant player is fine
- Anti-competitive activities that protects/enhances one's dominant position are illegal
 - deter other competitors from entering the market
 - intend to drive competitors out of the market
- Examples
 - Exclusive dealing
 - Aggressive pricing

Price Discrimination

(Firm may increase its profit further by charging different prices for its good)

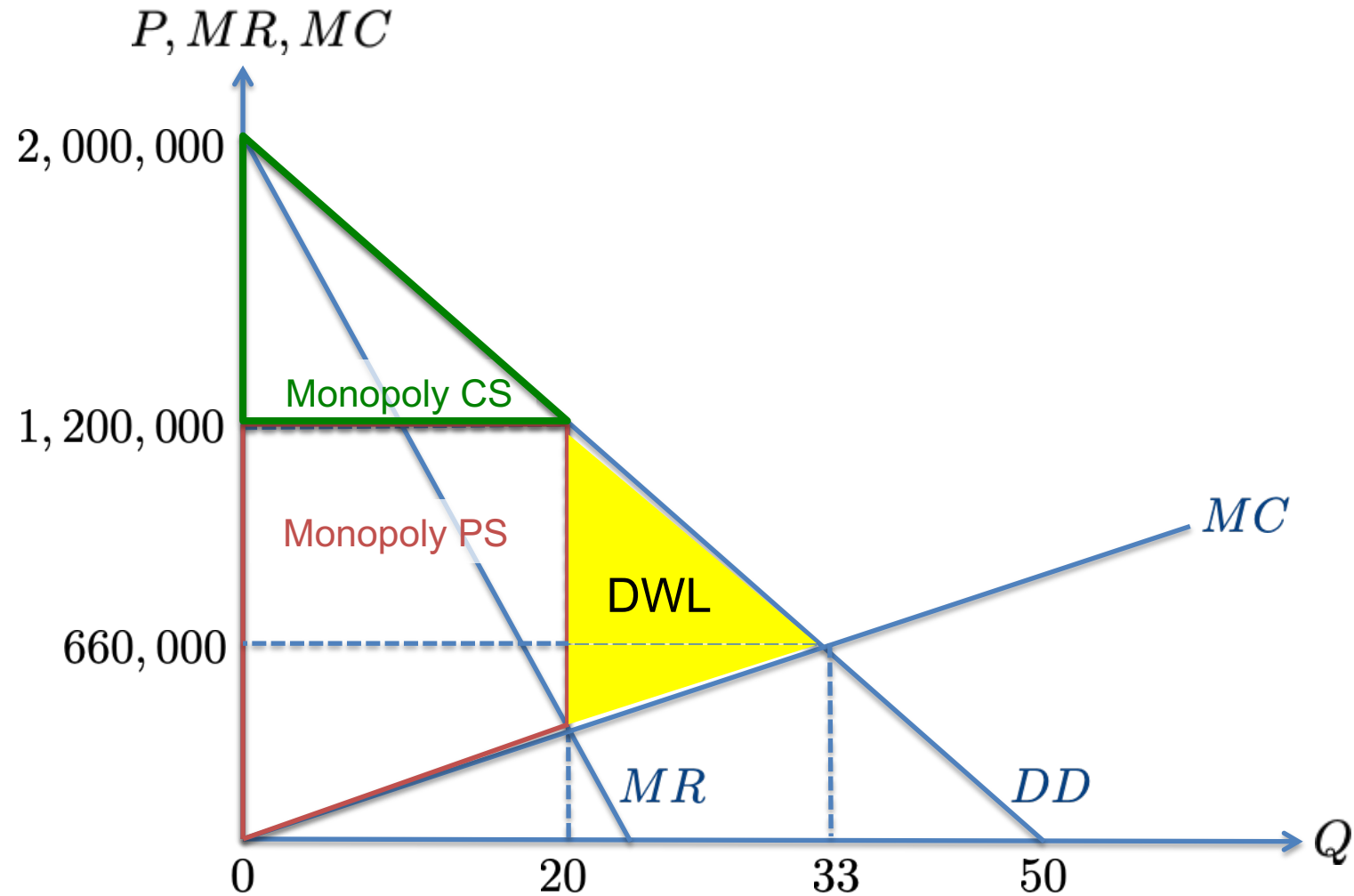
- 1st-degree
 - Each output unit is sold at a different price
 - Prices differ across buyers
- 2nd-degree
 - Price paid by a buyer varies with quantity purchased
 - All buyers face the same price schedule
 - Example: bulk discount
- 3rd-degree
 - Firm offers different prices to different groups
 - All buyers in the same group face the same price schedule
 - Example: senior citizen/student discounts

Uniform Pricing

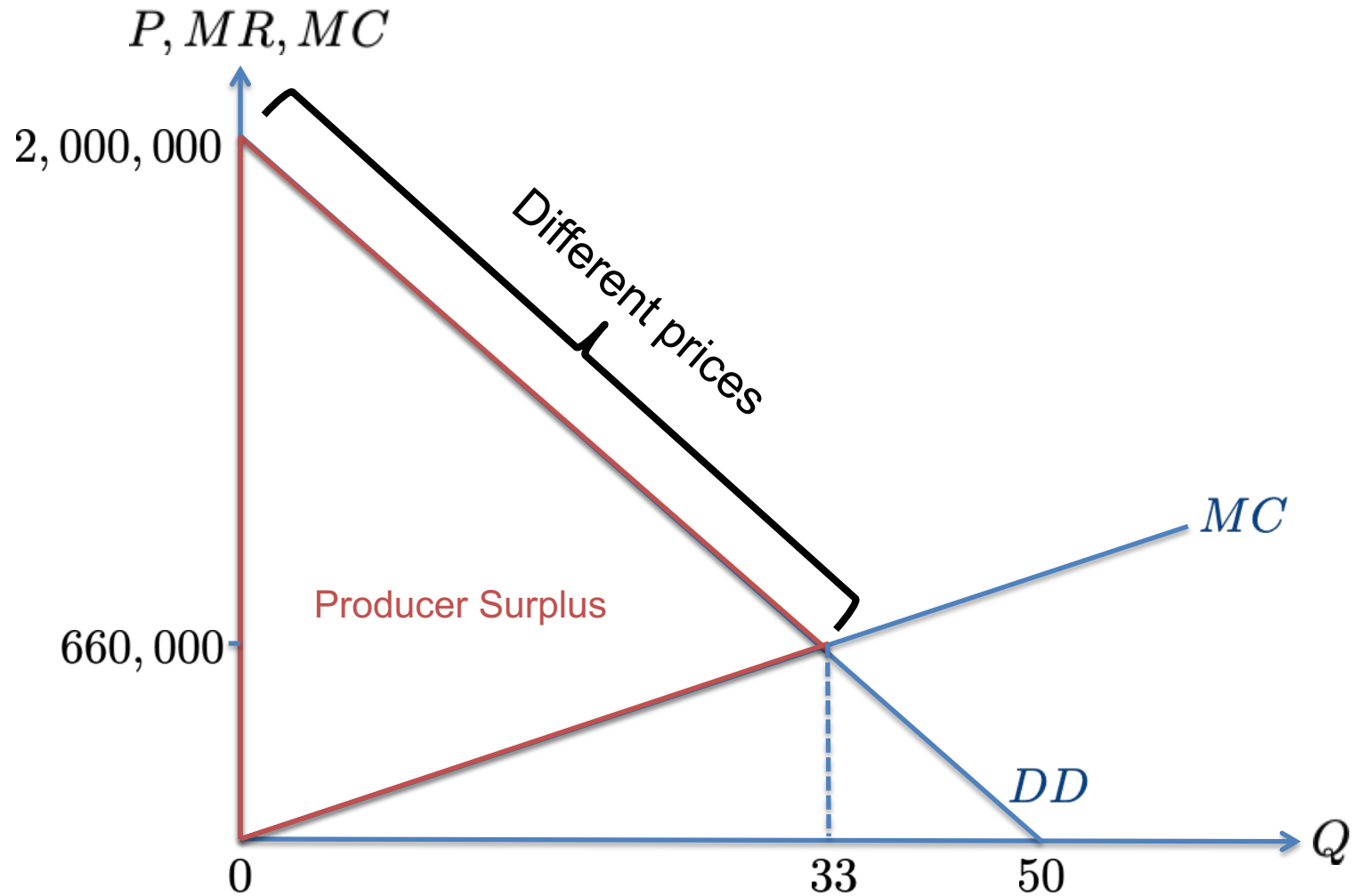


Under uniform pricing, Tyke will not consume

Welfare Under Uniform Pricing



First-Degree Price Discrimination

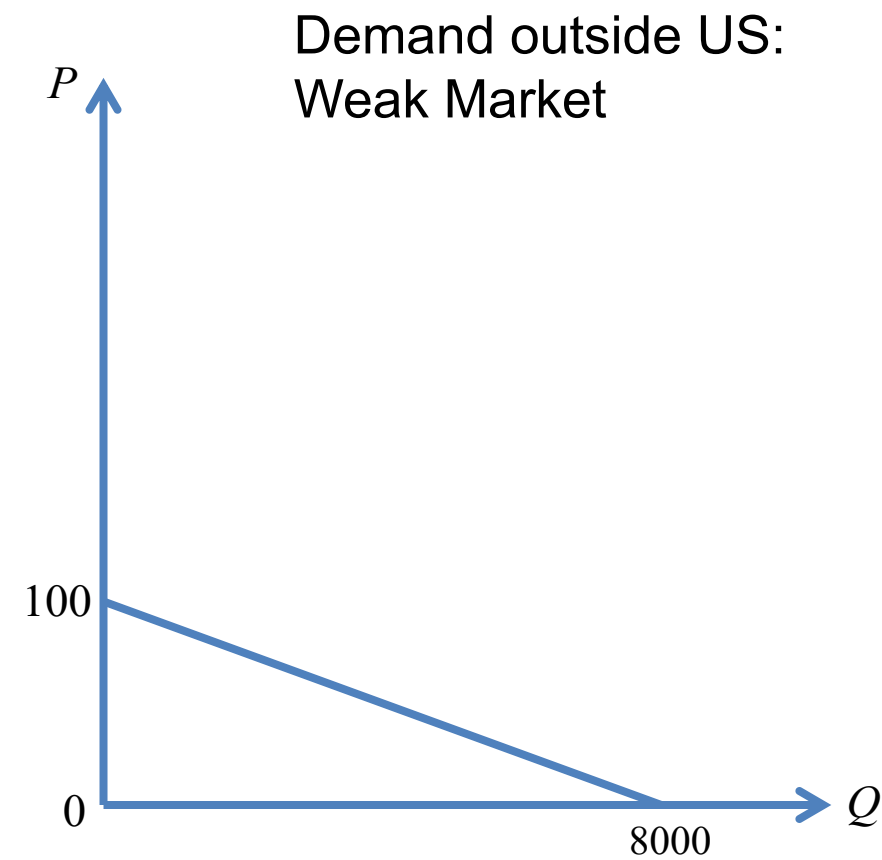
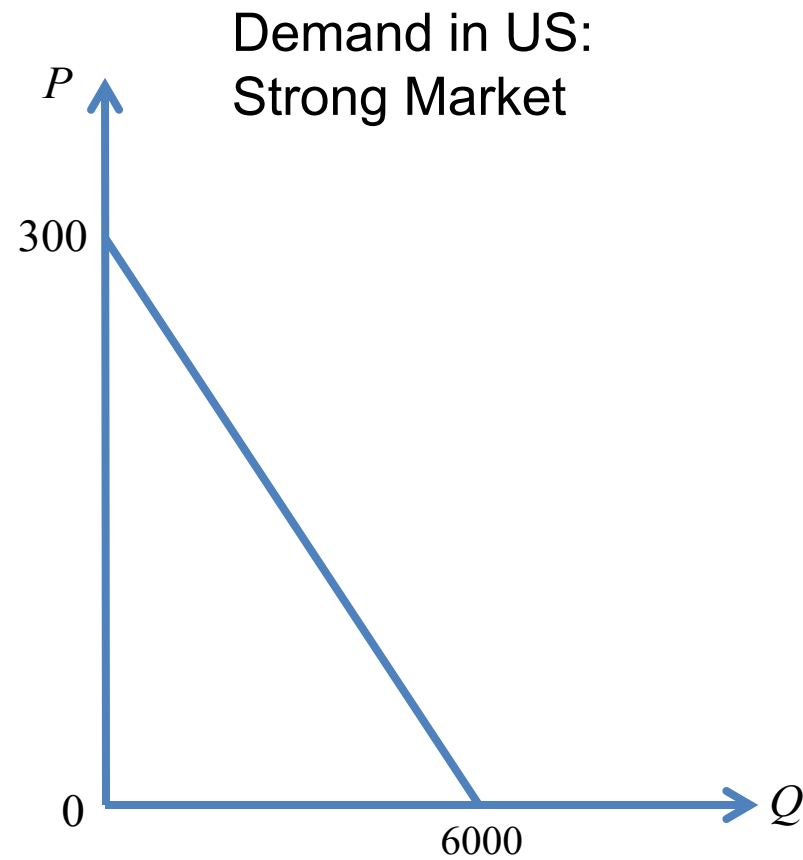


- Firm sells 33 units (at different prices) in total, instead of 20
- Tyke will consume

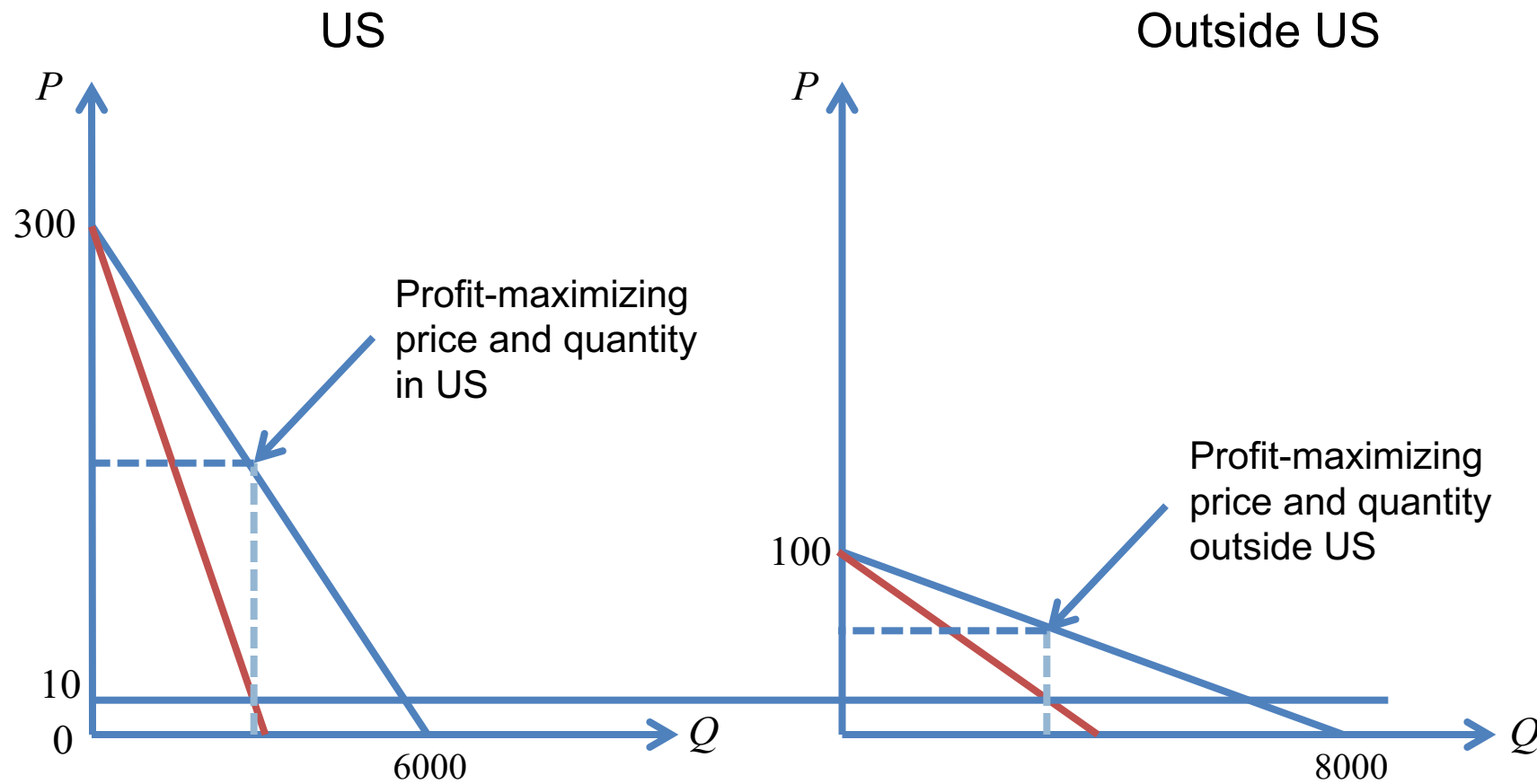
Third-Degree Price Discrimination

- Suppose Wiley sells textbook *Microeconomics* in two markets, US and Outside US
- Demand
 - Demand in US is $Q=6000-20P$
 - Demand outside US is $Q=8000-80P$
- Cost
 - Wiley's marginal cost is $MC=10$ in both markets
 - No fixed cost

Demand in US vs. outside US



Profit-Maximizing Price in Each Market



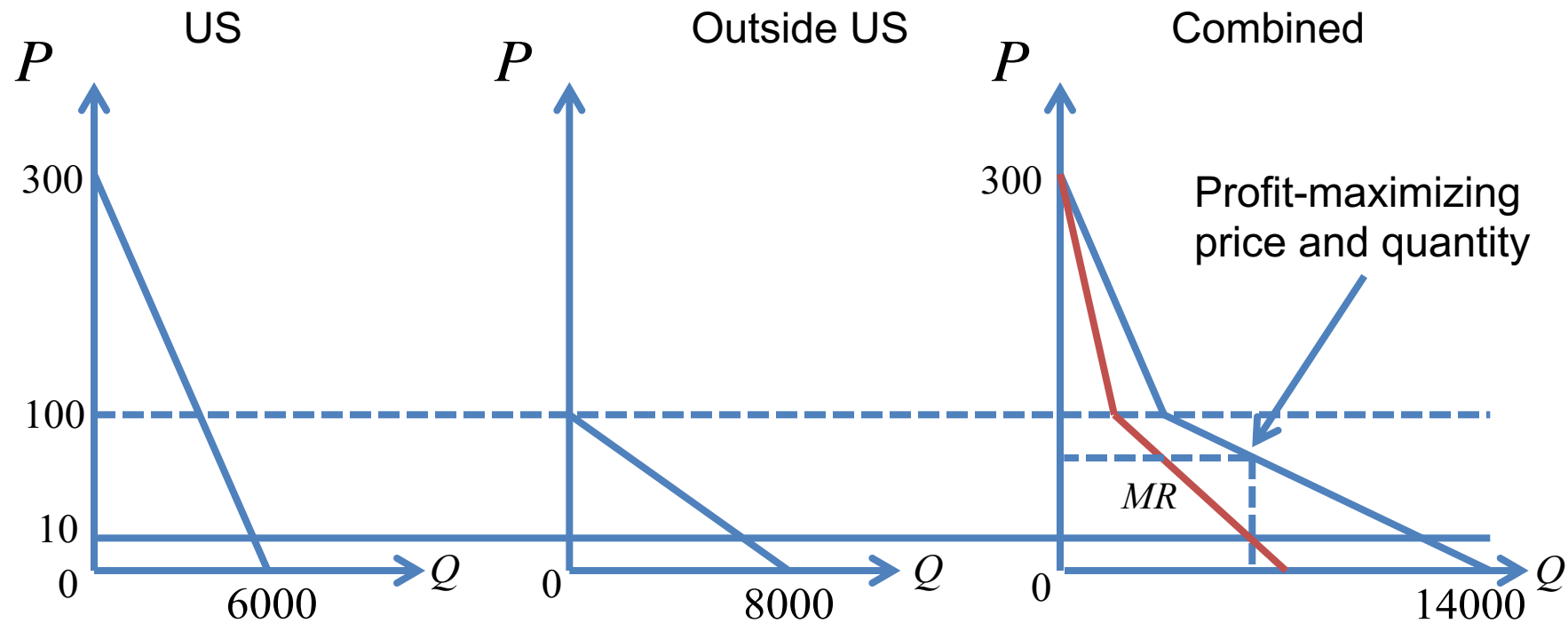
Profit-Maximizing Price in US

- In US, $MR = 300 - Q/10$
- Setting $MR=MC$, $300 - Q/10 = 10 \Rightarrow Q = 2900$
- Profit-maximizing price $P = 300 - 2900/20 = 155$
- Profit in US $TR - TC = 155 \times 2900 - 10 \times 2900 = 420,500$

Profit-Maximizing Price outside US

- Outside US, $MR = 100 - Q/40$
- Setting $MR=MC$, $100 - Q/40 = 10 \Rightarrow Q = 3600$
- Profit-maximizing price $P = 100 - 3600/80 = 55$
- Profit outside US $TR - TC = 55 \times 3600 - 10 \times 3600 = 162,000$

What if Wiley can only charge one price?



$$\begin{aligned}
 Q &= Q_{US} + Q_{exUS} \implies Q = (6000 - 20P) + (8000 - 80P) \\
 &\implies P = 140 - \frac{Q}{100}
 \end{aligned}$$

Profit-maximizing Uniform Price

- Wiley sets $MR=MC$, $140 - Q/50 = 10 \Rightarrow Q = 6,500$
- The profit-maximizing uniform price is $P = 140 - 6500/100 = 75$
- Wiley's profit is $TR - TC = 75 \times 6500 - 10 \times 6500 = 422,500$
- US consumers buy $6000 - 20 \times 75 = 4500$
- International consumers buy $8000 - 80 \times 75 = 2000$

Comparison

	Uniform Pricing	Third-Degree Price Discrimination
Optimal price	75	155 (US) 55 (Outside US)
Profit	422,500	582,500
Quantity sold in US	4500	2900
Quantity sold outside US	2000	3600