# EC2101: Microeconomic Analysis I

#### The Big Picture



$$\max_{x,y} U(x,y)$$
  
s.t.  $p_x x + p_y y = M$ 





Market Equilibrium

#### Supply

$$\min_{L,K} LRTC = wL + rK$$
s.t.  $f(L,K) = Q_0$ 

## Partial Equilibrium Analysis: Market Structure

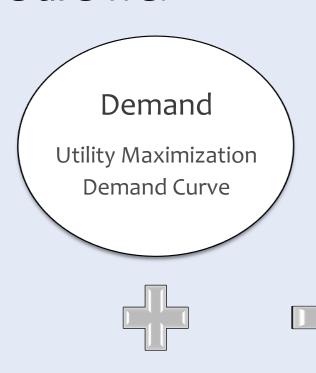
- Perfectly Competitive Markets
- Monopoly
- Monopolistic Competition
- Oligopoly

#### Lecture 10

#### **Perfect Competition**

- Accounting Profit vs. Economic Profit
- Perfect Competition in the Short Run
  - SR Profit-Maximizing Output Choice
  - SR Supply Curve
  - SR Market Equilibrium
  - Producer Surplus in the SR

#### Where are we?



Supply
Profit Maximization
Supply Curve

Competitive Market Equilibrium

#### Perfectly Competitive Markets

- The industry is fragmented.
  - Thus firms and consumers are price-takers.
- The product is homogeneous.
  - The products produced by different firms are identical.
- There is perfect information on prices.
  - Thus there is a single market price.
- Every firm has equal access to technology and inputs.
  - Thus the market is characterized by free entry (and exit).

#### Example: Catfish Farming Industry in the U.S.

- The industry is fragmented.
  - There are over 1,000 catfish farms.
- The product is homogeneous.
  - The catfish produced by different farms are indistinguishable.
- There is perfect information on prices.
  - All buyers and sellers know the prices charged by all sellers.
- Every firm has access to the same technology and inputs.
  - The production technology is well understood.

#### Short Run vs. Long Run

- In the short run:
  - At least one input is fixed.
  - Firms choose the level of output to maximize profit.
- In the long run:
  - All inputs are adjustable.
  - Firms choose the level of output to maximize profit.
  - Firms decide whether to enter or exit the market.

# Accounting Profit vs. Economic Profit

#### Accounting Profit vs. Economic Profit

- Accounting Profit
  - = Total Revenue Explicit Costs
- Economic Profit
  - = Total Revenue (Explicit Costs + Implicit Costs)

#### Accounting Profit vs. Economic Profit: Example

- Suppose you own and run a small software development firm.
- In 2020, your total revenue was \$400,000.
- You incurred explicit costs of \$250,000 for wages, supplies, rent, utilities, etc.
- Your accounting profit is:
  - -\$400,000 \$250,000 = \$150,000

#### Accounting Profit vs. Economic Profit: Example

- Your best alternative is to work for Google for an annual salary of \$150,000.
  - I.e., your implicit cost is \$150,000.
- Your economic cost / opportunity cost is:
  - **\$250,000 + \$150,000 = \$400,000**
- Your economic profit is:
  - -\$400,000 \$400,000 = \$0
- The money you make running your own firm is the same as the money you could have made working for Google.

#### **Economic Profit**

#### Zero economic profit

All resources (entrepreneur's time, assets, capital)
are getting returns that are equivalent to
the returns from the best alternative.

#### Positive economic profit

 The business is delivering returns that are higher than the returns from the best alternative.

#### Negative economic profit

 The resources could be used somewhere else to generate higher returns.

#### Exercise 10.1

#### Accounting Profit vs. Economic Profit

The rent on office space has just decreased by \$500 a month. How does accounting profit change? How does economic profit change?

- (a) You rent your office space.
- (b) You own your office space.

# Short-Run Profit-Maximizing Output Choice

#### Profit and Revenue

The firm chooses Q to maximize profit.

$$\pi(Q) = TR(Q) - TC(Q)$$

Total Revenue:

$$TR(Q) = P(Q) \cdot Q$$

Marginal Revenue:

$$MR(Q) = \frac{dTR(Q)}{dQ}$$

- The rate at which total revenue changes with output.
- The slope of the total revenue curve.

#### **Profit Maximization**

To maximize profit, we solve:

$$\max_{Q} \pi(Q) = TR(Q) - TC(Q)$$

First-order condition:

$$\pi'(Q) = 0$$

$$\frac{d\pi(Q)}{dQ} = 0$$

$$MR(Q) - MC(Q) = 0$$

Rearranging, we have:

$$MR(Q) = MC(Q)$$

## Profit-Maximizing Condition in a Perfectly Competitive Market

- Firms take the market price p as given.
- Total revenue is linear in output:

$$TR(Q) = pQ$$

- The firm can sell as many units as it wants at the market price.
  - Thus marginal revenue equals price:

$$MR(Q) = p$$

To maximize profit:

$$MR(Q) = MC(Q)$$

$$p = MC(Q)$$

#### Profit Maximization: Example

Suppose the firm's short-run total cost curve is:

$$SRTC(Q) = 25 + Q^2$$

Therefore, the short-run marginal cost is:

$$SRMC(Q) = 2Q$$

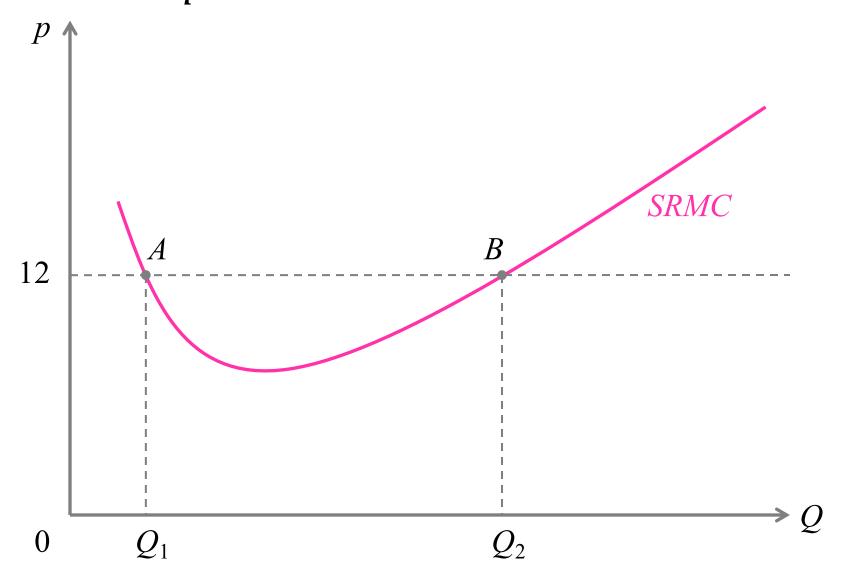
To maximize profit,

$$p = SRMC(Q)$$
$$p = 2Q$$

• If p = 12, the profit-maximizing Q is:

$$12 = 2Q$$
$$Q = 6$$

There may be more than one output level at which p = SRMC



#### Second-Order Condition

 To ensure that we are indeed maximizing profit, we need the second-order condition:

$$\frac{d\left(\frac{d\pi(Q)}{dQ}\right)}{dQ} \le 0$$

$$\frac{d\left(MR(Q) - MC(Q)\right)}{dQ} \le 0$$

$$\frac{dMR(Q) - dMC(Q)}{dQ} \le 0$$

#### Second-Order Condition

Second-order condition:

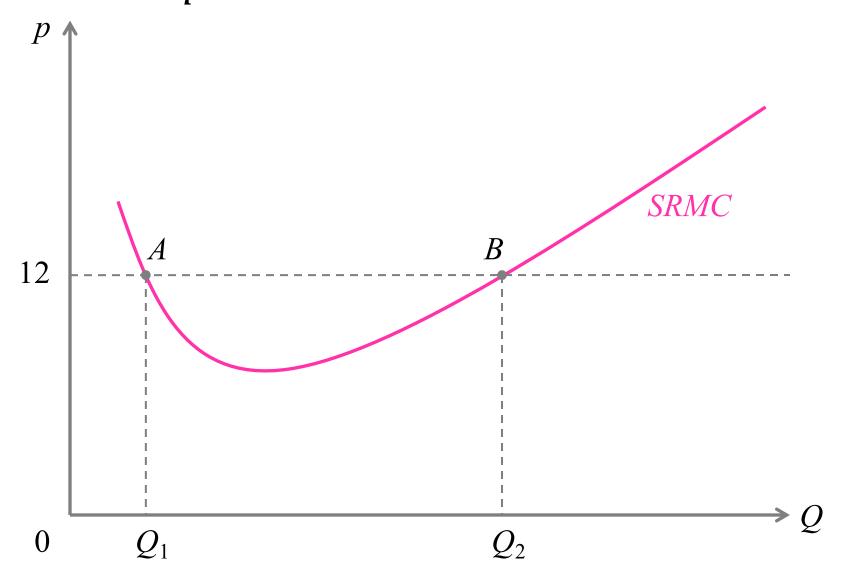
$$\frac{dMR(Q)}{dQ} - \frac{dMC(Q)}{dQ} \le 0$$

• Since 
$$MR(Q) = p$$
, 
$$\frac{dMR(Q)}{dO} = 0$$

Therefore,

$$\frac{dMC(Q)}{dQ} \ge 0$$

There may be more than one output level at which p = SRMC



#### Profit Maximization: When p > SRMC

- Suppose p = 12, and the firm produces Q = 2.
- MR = p = 12
  - If the firm increases the production level,
     total revenue increases at a rate of 12.
- $SRMC = 2Q = 2 \cdot 2 = 4$ 
  - If the firm increases the production level,
     total cost increases at a rate of 4.
- When p > SRMC,
   total revenue increases faster than total cost
   as the production level increases.

#### Profit Maximization: When p < SRMC

- Suppose p = 12, and the firm produces Q = 8.
- MR = p = 12
  - If the firm decreases the production level,
     total revenue decreases at a rate of 12.
- $SRMC = 2Q = 2 \cdot 8 = 16$ 
  - If the firm decreases the production level,
     total cost decreases at a rate of 16.
- When p < SRMC, total revenue decreases slower than total cost as the production level decreases.

#### **Profit Maximization**

- If the firm can increase profit by either:
  - producing more when p > SRMC or
  - producing less when p < SRMC
  - Then the firm must be maximizing profit when producing at an output level such that p = SRMC.

#### Short-Run Profit-Maximizing Output Choice

Suppose a firm in a perfectly competitive market has a short-run total cost curve of  $SRTC(Q) = \frac{1}{2}Q^2 - 10Q + 800$ . The market price of the output is p = 20.

- (a) Write down the firm's profit-maximization problem.
- (b) What is the firm's optimal level of output?
- (c) Verify that your answer in (b) is indeed profit maximizing.
- (d) Calculate the firm's profit.

#### Short-Run Profit-Maximizing Output Choice

# Short-Run Supply Curve

#### Non-Sunk Cost vs. Sunk Cost

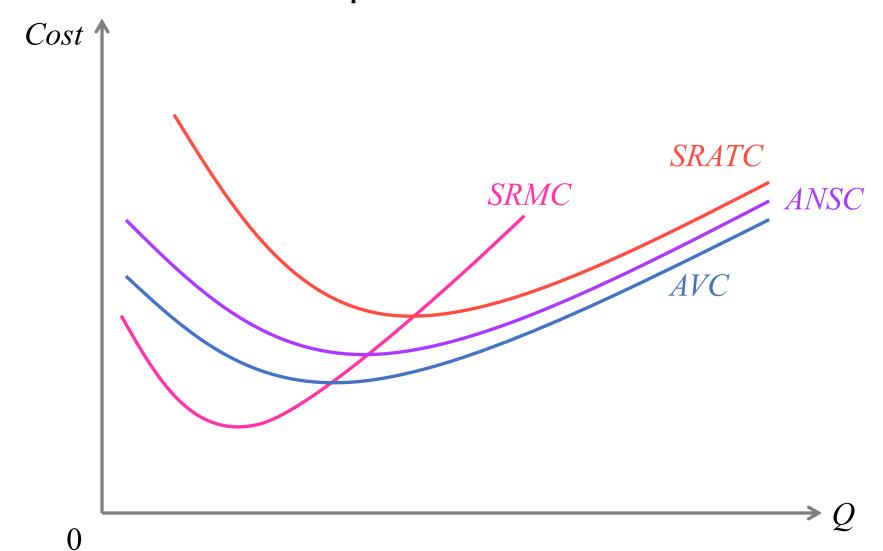
- The fixed cost may or may not be sunk.
- Total Non-Sunk Cost (TNSC):
  - Variable Cost + Non-Sunk Fixed Cost
- Total Sunk Cost (TSC):
  - Sunk Fixed Cost
- If all of the fixed cost is non-sunk,

$$TNSC = VC + FC = SRTC$$

If all of the fixed cost is sunk,

$$TNSC = VC$$

## SRMC intersects ANSC at the minimum point of ANSC



#### Should the firm produce at all?

If the firm does not produce any output,

$$\pi(Q=0)=0-TSC$$

If the firm produces output,

$$\pi(Q > 0) = TR(Q) - TNSC(Q) - TSC$$

The firm produces output only if

$$TR(Q) - TNSC(Q) - TSC \ge -TSC$$

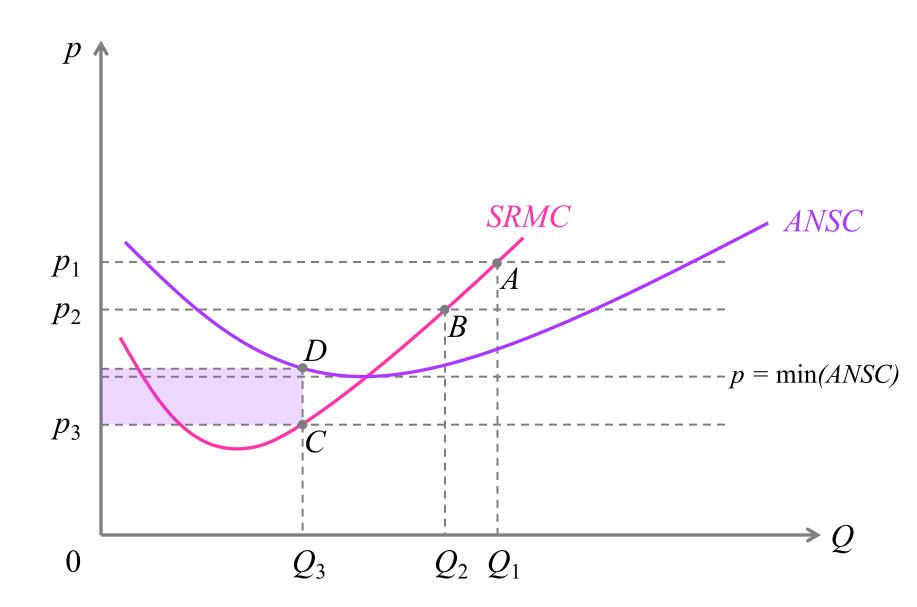
$$TR(Q) \ge TNSC(Q)$$

#### Should the firm produce at all?

- Recall that:
  - TR(Q) = pQ
  - $TNSC(Q) = ANSC(Q) \times Q$
- The firm produces output only if

```
TR(Q) \ge TNSC(Q)
pQ \ge ANSC(Q) \times Q
p \ge ANSC(Q)
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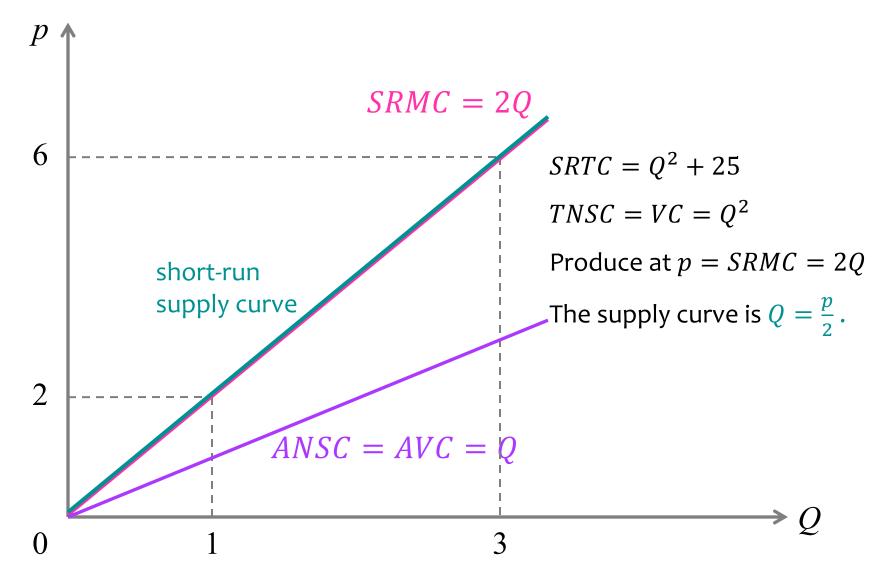
#### When should the firm stop producing?



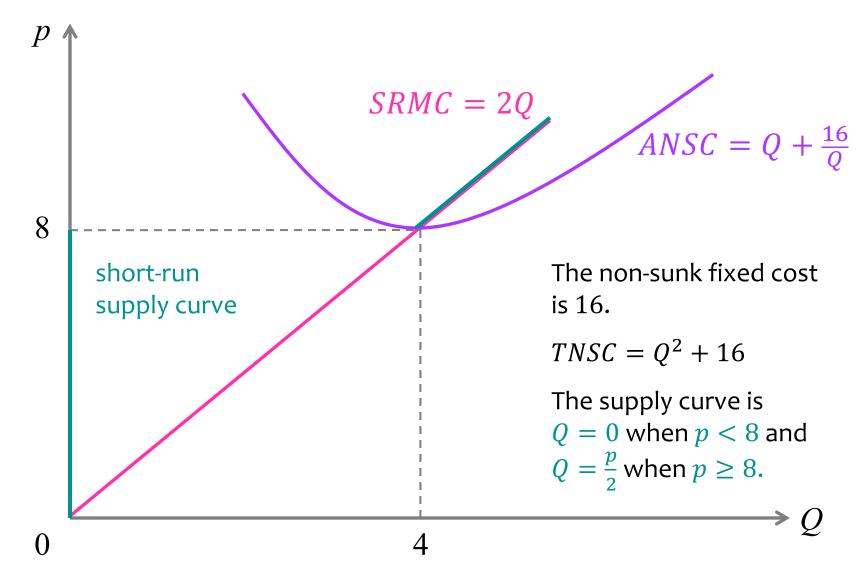
#### Profit-Maximizing Conditions in the Short Run

- When  $p \ge \min(ANSC)$ , the firm should choose Q such that:
  - At that output level, p = SRMC(Q).
  - SRMC is non-decreasing in Q.
- When  $p < \min(ANSC)$ , the firm should choose Q = 0.

### The Firm's Supply Curve when All of the Fixed Cost is Sunk



# The Firm's Supply Curve when Part of the Fixed Cost is Non-Sunk



# Deriving ANSC(Q) and Finding the Minimum

Refer to the graph on the previous slide. The short-run total cost curve is  $SRTC(Q) = Q^2 + 25$  and the non-sunk fixed cost is 16.

(a) Verify that 
$$ANSC(Q) = Q + \frac{16}{Q}$$
.

(b) Verify that at the minimum of ANSC(Q), Q = 4 and ANSC = 8.

Exercise 10.3

Deriving ANSC(Q) and Finding the Minimum

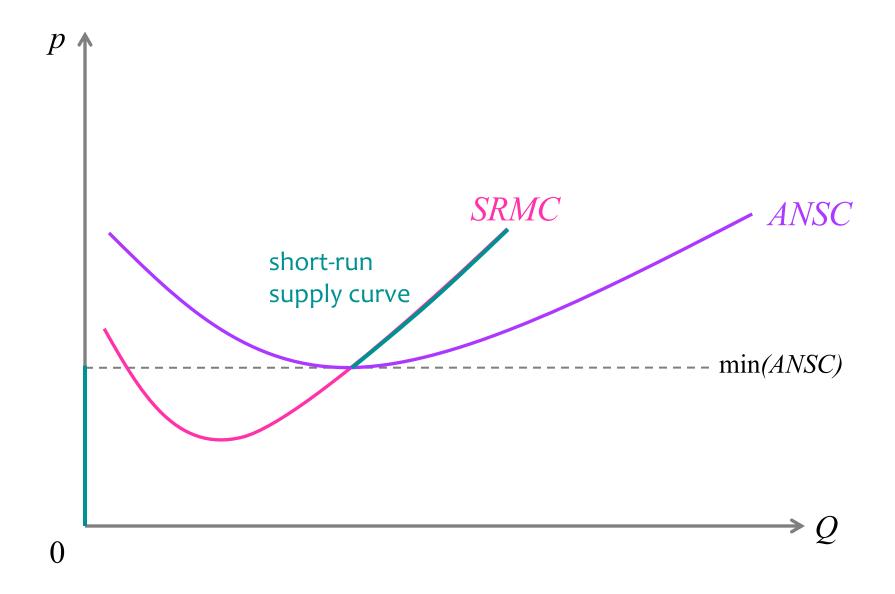
# The Individual Firm's Supply Curve

 The short-run supply curve for an individual firm is the profit-maximizing quantity for the firm as a function of the market price.

```
Q_f(p)
```

- When  $p < \min(ANSC)$ :
  - The firm chooses Q = 0.
  - The supply curve is the vertical axis.
- When  $p \ge \min(ANSC)$ :
  - The firm chooses Q such that p = SRMC(Q).
  - The supply curve is the marginal cost curve.

# The Firm's Short-Run Supply Curve in General



# Short-Run Market Supply Curve

- The short-run market supply curve is the horizontal sum of all individual firms' supply curves.
- Suppose there are 100 identical firms in the market.
- Assuming all of the fixed cost is sunk, each firm has a supply curve:

$$Q_f = \frac{p}{2}$$

The market supply curve is:

$$S(p) = 100 \times \frac{p}{2} = 50p$$

# Short-Run Market Equilibrium

# Short-Run Market Equilibrium

- At the short-run market equilibrium price:
  - Total quantity demanded equals total quantity supplied.
  - Each firm produces at the profit-maximizing output level given the equilibrium market price.
  - Each consumer buys the utility-maximizing quantity given the equilibrium market price.

# Short-Run Market Equilibrium: Example

- Recall that each firm's supply curve is  $Q_f = \frac{p}{2}$  and that the market supply curve is S(p) = 50p.
- Suppose the market demand curve is:

$$D(p) = 560 - 20p$$

Therefore, the short-run equilibrium price is:

$$S(p) = D(p)$$

$$50p = 560 - 20p$$

$$p = 8$$

# Short-Run Market Equilibrium: Example

- Recall that each firm's supply curve is  $Q_f = \frac{p}{2}$  and that the market supply curve is S(p) = 50p.
- The short-run equilibrium price is p = 8.
- In equilibrium, the total quantity of output produced is:

$$S = 50p = 50 \cdot 8 = 400$$

Each firm produces:

$$Q_f = \frac{p}{2} = \frac{8}{2} = 4$$

# Relationship between Profit and SRATC

- Suppose the market price is p, and at this price, the firm's optimal output level is  $Q_f$ .
- The firm's profit is:

$$TR - SRTC = pQ_f - (SRATC(Q_f) \times Q_f)$$
$$= (p - SRATC(Q_f))Q_f$$

- If p > SRATC(Q):
  - The firm's profit is positive at the output level  $Q_f$ .
- If p < SRATC(Q):
  - The firm's profit is negative at the output level  $Q_f$ .

# Profit in the Short-Run Market Equilibrium

- Recall that:
  - The short-run equilibrium price is p = 8.
  - Each firm produces  $Q_f = 4$ .
  - Each firm's short-run total cost is  $SRTC(Q_f) = 25 + (Q_f)^2$ .
- Each firm's profit is:

$$TR - SRTC = pQ_f - SRTC(Q_f)$$
$$= 8 \cdot 4 - (25 + 4^2)$$
$$= -9$$

# Profit in the Short-Run Market Equilibrium

Each firm's short-run average total cost is:

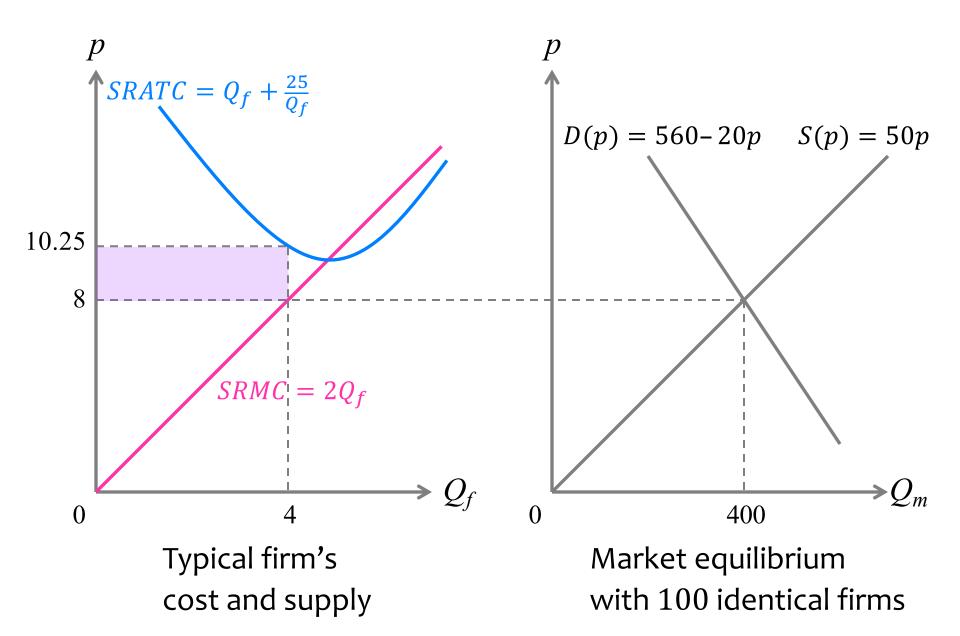
$$SRATC(Q_f) = \frac{SRTC(Q_f)}{Q} = \frac{25 + (Q_f)^2}{Q}$$

• At  $Q_f = 4$ :

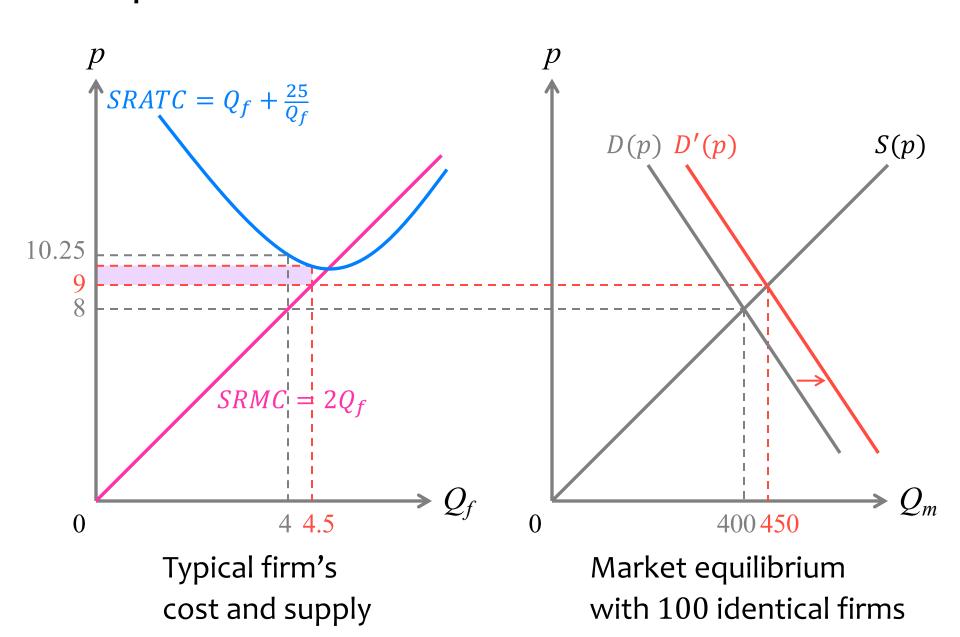
$$SRATC(4) = \frac{25 + 4^2}{4} = 10.25$$

- Negative profit is possible in the short-run market equilibrium.
  - Firms do not consider sunk cost when deciding how many units of output to produce.

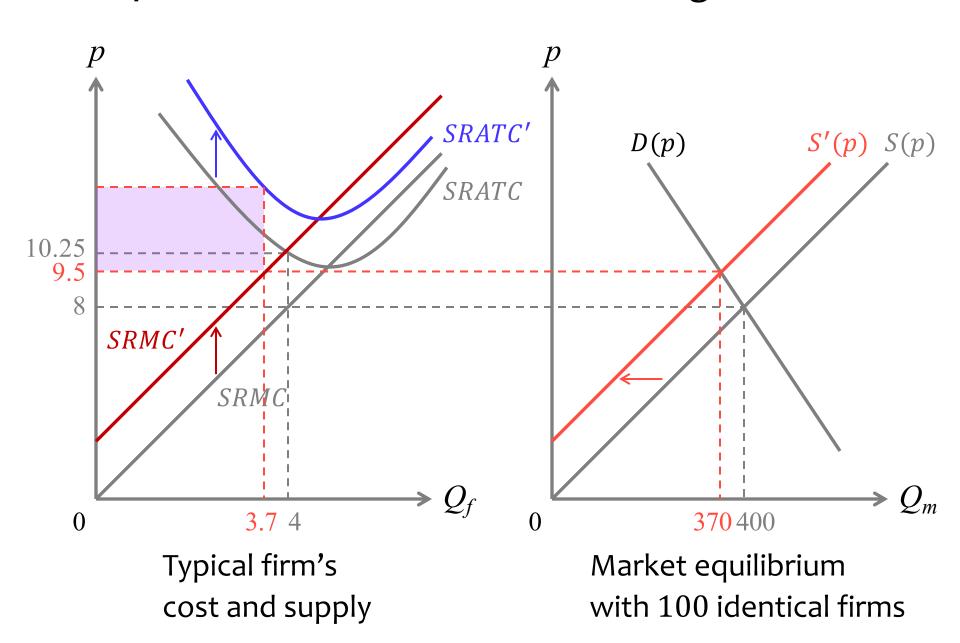
# Short-Run Equilibrium



# Comparative Statics: Increase in Demand



# Comparative Statics: Increase in Wage



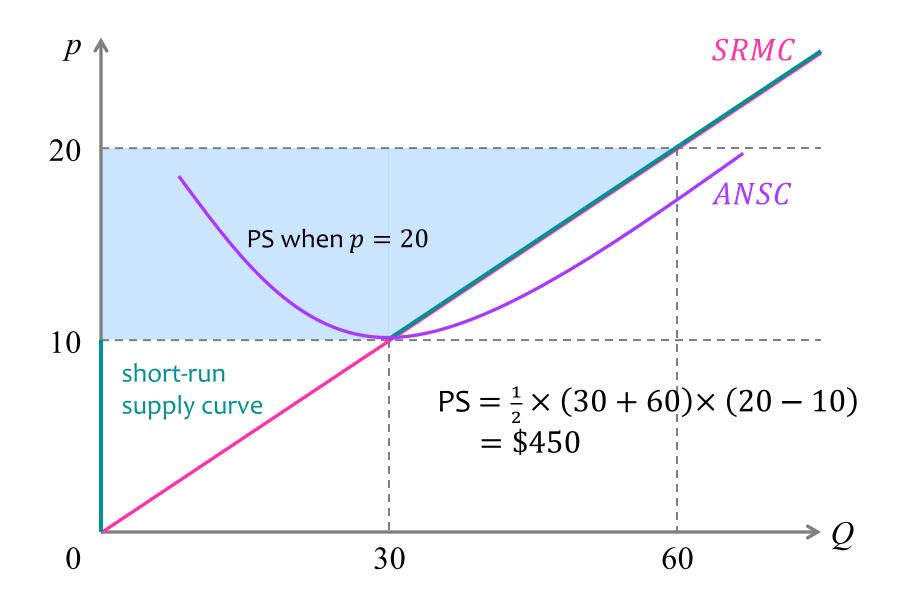
# Summary SRATC, SRMC, ANSC

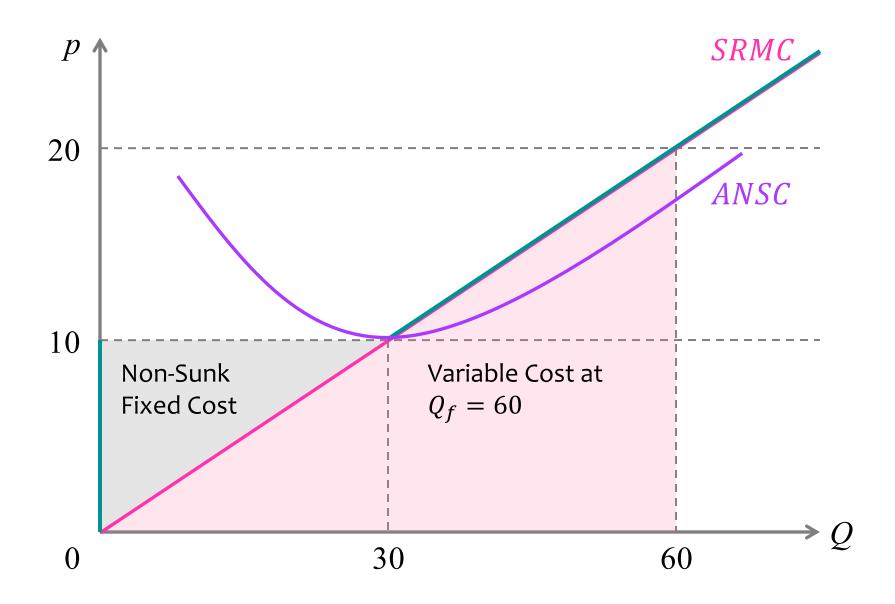
#### When does the firm consider:

- short-run average total cost (SRATC)
- short-run marginal cost (SRMC)
- average non-sunk cost (ANSC)

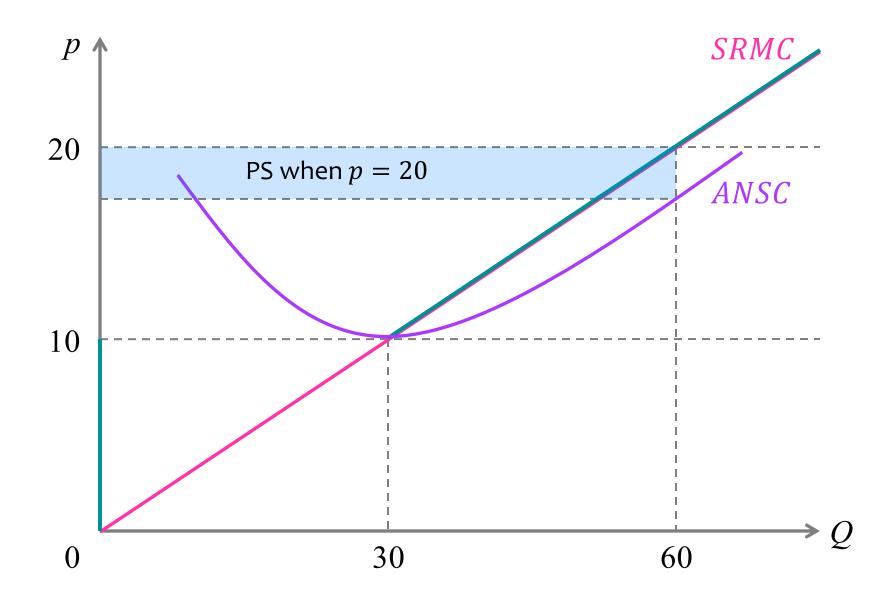
# Producer Surplus in the Short Run

- Producer Surplus (PS) individual firm:
  - The difference between
     the amount that the firm receives
     for producing a certain quantity of output and
     the amount the firm has to receive
     in order to produce that quantity of output.
  - PS = Total Revenue Total Non-Sunk Cost
  - Graphically, the area below the price and above the supply curve.
- Producer Surplus (PS) market:
  - The sum of all individual firms' producer surplus.





- Total Revenue  $(TR) = 20 \cdot 60 = 1,200$
- Total Non-Sunk Cost (TNSC):
  - *VC* when  $Q_f = 60$  is  $\frac{1}{2} \cdot 60 \cdot 20 = 600$ .
    - *VC* is the area below the *SRMC* curve.
  - Non-Sunk Fixed Cost is 150.
    - *TNSC* for the first 30 units is  $ANSC(30) \cdot 30 = 10 \cdot 30 = 300$ .
    - But VC for the first 30 units is  $\frac{1}{2} \cdot 30 \cdot 10 = 150$ .
  - Therefore TNSC = 600 + 150 = 750
- PS = TR TNSC = 1,200 750 = 450
  - The area below the price and above the supply curve.

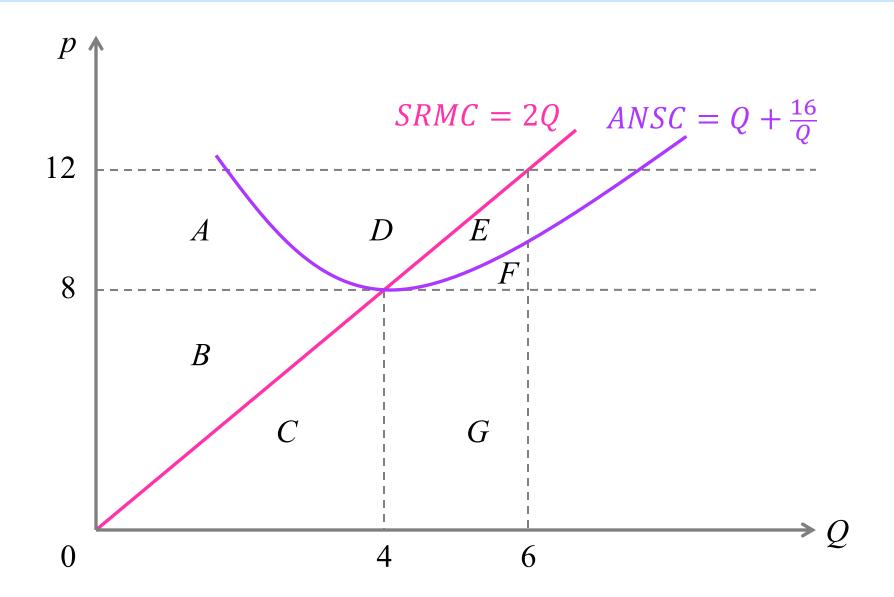


# Part of the Fixed Cost is Non-Sunk (ANSC)

Refer to the graph on the next slide. The short-run total cost curve is  $SRTC = Q^2 + 25$ . Part of the fixed cost is non-sunk. Suppose p = 12.

- (a) Indicate the variable cost (VC) on the graph. Calculate VC.
- (b) Indicate the non-sunk fixed cost (*NSFC*) on the graph. Calculate *NSFC*.
- (c) Indicate the sunk fixed cost (SFC) on the graph. Calculate SFC.

# Part of the Fixed Cost is Non-Sunk (ANSC)

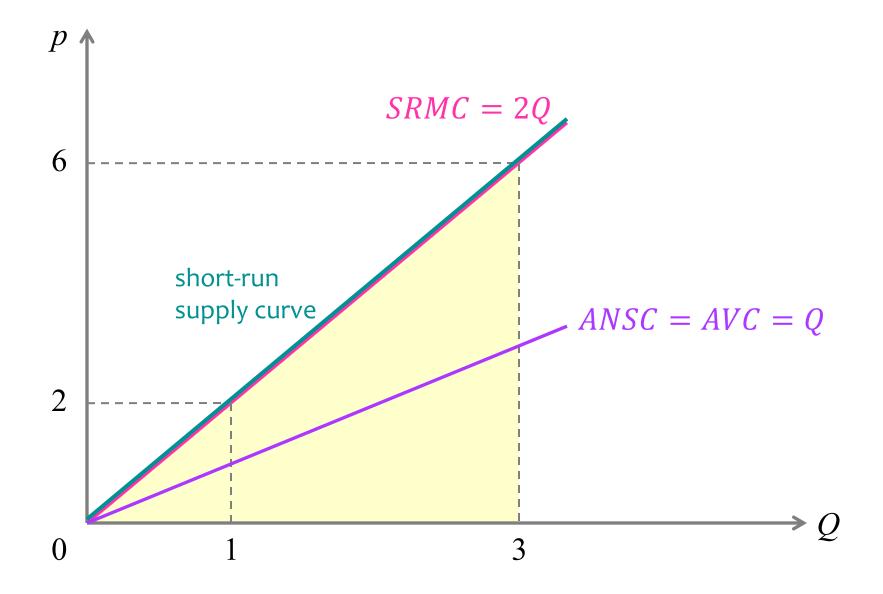


# All of the Fixed Cost is Sunk (ANSC)

Refer to the graph on the next slide. The short-run total cost curve is  $SRTC = Q^2 + 25$ . All of the fixed cost is sunk. Suppose p = 6.

- (a) Show that the short-run supply curve is Q = p/2.
- (b) What is the shaded area?

# All of the Fixed Cost is Sunk (ANSC)



#### Exercise 10.6

# All of the Fixed Cost is Sunk (SRATC)

Refer to the graph on the next slide. The short-run total cost curve is  $SRTC = Q^2 + 25$ . All of the fixed cost is sunk. The short-run supply curve is Q = p/2.

What is the shaded area?

# All of the Fixed Cost is Sunk (SRATC)

