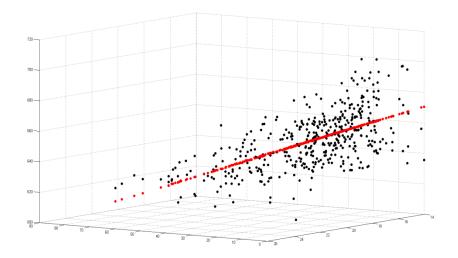
# EC 3303: Econometrics I

#### **Assessing Regression-Based Studies**



**Kelvin Seah** 

AY 2022/2023, Semester 2

### **Outline**

1. Framework for Assessing Regression Studies

2. Threats to Internal Validity

3. External Validity

## **Assessing Studies Based on Multiple Regression**

• What makes a study that uses multiple regression reliable or unreliable?

• Is there a systematic way to assess (critique) regression-based studies?

• Framework for assessing regression-based studies:

relies on the concepts of Internal & External Validity.

## **Internal & External Validity**

#### Internal Validity

- A study is internally valid if its statistical inferences about causal effects are valid for the population & setting studied.
  - where the "population studied" is the population of entities people, firms, school districts, etc from which the sample was drawn.
  - where "setting" refers to the institutional, social, economic environment.

#### External Validity

- A study is externally valid if its inferences can be generalised to other population & settings.

# Is there a systematic way to assess regression studies?

- Can assess a study by asking:
  - 1) Is it plausibly internally valid?
    - Yes: Why might it be internally valid?
    - No: Why might internal validity be threatened?

- 2) Can I generalise the inferences & conclusions from this study to other populations & settings?
  - Why or why not?

# **Regression Studies & Internal Validity**

Multiple regression has some key virtues:

- It provides an estimate of the effect on *Y* arising from a change in *X*.
- It resolves the problem of omitted variable bias, *if* omitted variable(s) can be measured & included.
- It can handle nonlinear relationships.

Still, OLS might yield a *biased* estimator of the true *causal* effect – that is, it might not yield internally valid inferences...

# **Internal Validity**

For a study to be internally valid, 2 conditions must be met:

The *estimator* of the causal effect of interest should be *unbiased* and *consistent*.

2) Hypothesis tests have the *correct significance level*; confidence intervals have the *correct confidence level* (i.e. standard errors are correctly estimated).

In practice, these requirements might not be met, and this constitutes a threat to internal validity.

# **Threats to Internal Validity**

- Omitted variable bias
- Wrong functional form
- Errors-in-variables bias
- Sample selection bias
- Simultaneous causality bias

All of these imply  $E(u_i|X_{1i}, X_{2i}, ..., X_{ki}) \neq 0$ 

#### 1. Omitted Variable Bias

Omitted variable bias arises if you omit from the regression a variable which is *both*:

- (i) a determinant of Y &
- (ii) correlated with at least one included regressor.

We first discussed omitted variable bias in regression with a single *X*, but OV bias can arise when there are multiple *X*'s as well.

What might we have omitted in testscore – class size regressions?

#### **Potential Solutions to Omitted Variable Bias**

#### If the omitted variable is observed

1. If you know what the omitted variable is, include it as an additional regressor in the multiple regression.

#### If the omitted variable is not observed

2. Use *panel data* to weed out the effects of unobserved omitted variables which do not change over time (EC3304).

#### If the omitted variable is not observed

- 3. Use *instrumental variables (IV)* regression (EC3304)
- 4. Use a randomized controlled experiment
  - if the treatment X is randomly assigned, then X necessarily will be distributed independently of u.
  - $\bullet \quad E(u_i|X_i=x)=0$

# **Project STAR**



#### 2. Incorrect Functional Form

• Bias can arise if the researcher wrongly specifies the functional form of the regression.

• e.g.: if the true regression function is nonlinear in *X* (cubic) but the researcher estimates a linear regression, then the OLS estimator of the effect of *X* will be biased.

. regress testscr avginc, robust

Linear regression

Number of obs = 420F( 1, 418) = 273.29Prob > F = 0.0000R-squared = 0.5076Root MSE = 13.387

testscr	Coef.	Robust Std. Err.	t	P> t	[95% Conf.	Interval]
avginc	1.87855	.1136349	16.53	0.000	1.655183	2.101917
_cons	625.3836	1.867872	334.81	0.000	621.712	629.0552

. regress testscr avginc avginc2 avginc3, robust

Linear regression

Number of obs = 420F( 3, 416) = 270.18Prob > F = 0.0000R-squared = 0.5584Root MSE = 12.707

testscr	Coef.	Robust Std. Err.	t	P> t	[95% Conf.	Interval]
avginc	5.018677	.7073505	7.10	0.000	3.62825	6.409104
avginc2	0958052	.0289537	-3.31	0.001	1527191	0388913
avginc3	.0006855	.0003471	1.98	0.049	3.27e-06	.0013677
_cons	600.079	5.102062	117.61	0.000	590.0499	610.108

How does an increase in district income from \$5,000 to \$6,000 affect testscore?

- Linear Specification: increase testscore by 1.9 points
- (True) Cubic Specification: increase testscore by 4.0 points

# Potential solutions to functional form misspecification

• use the "appropriate" nonlinear specifications (logarithms, polynomials, interactions)

#### 3. Errors-in-Variables Bias

we have assumed that X's are measured without error.

- In reality, economic data often have measurement error.
- Data entry errors in administrative data.
- Recollection errors in surveys (monthly salary during your first year of work?)
- Ambiguous question problems (income last year?)
- Intentionally false response problems (How often do you drink and drive?)

#### **Consequences of Measurement Error in a Regressor**

Suppose we have a single regressor  $X_i$  (say, actual earnings):

- $X_i$  is measured with error, as  $\tilde{X}_i$  (respondent's reported earnings).
- because we observe  $\tilde{X}_i$  (not  $X_i$ ), the regression equation actually estimated will be the one based on  $\tilde{X}_i$ .

Suppose true model is:

$$Y_i = \beta_0 + \beta_1 X_i + u_i \quad (1)$$

and that  $E(u_i|X_i) = 0$ 

Written in terms of  $\tilde{X}_i$ , (1) is

$$Y_i = \beta_0 + \beta_1 \tilde{X}_i + \left[\beta_1 \left(X_i - \tilde{X}_i\right) + u_i\right]$$
$$= \beta_0 + \beta_1 \tilde{X}_i + v_i \tag{2}$$

where 
$$v_i = \beta_1 (X_i - \tilde{X}_i) + u_i$$

$$Y_i = \beta_0 + \beta_1 \tilde{X}_i + \left[\beta_1 (X_i - \tilde{X}_i) + u_i\right]$$

$$v_i$$

- measurement error is  $X_i \tilde{X}_i$ .
- If the measurement error  $(X_i \tilde{X}_i)$  is correlated with the measured value  $\tilde{X}_i$ , then  $\tilde{X}_i$  will be correlated with the error term  $v_i$ , and  $\hat{\beta}_1$  will be biased and inconsistent.
- The size & direction of the bias in  $\hat{\beta}_1$  depends on the nature of the correlation between  $\tilde{X}_i$  & the measurement error.

What would happen, if instead, *Y* is measured with some random error?

• Not much... $Var(\hat{\beta}_1)$  would be larger than if Y was not measured with error, but **no bias** would be induced in  $\hat{\beta}_1$ 

true model:

$$Y_i = \beta_0 + \beta_1 X_i + u_i \quad (1)$$

Written in terms of the incorrectly measured variable,  $\tilde{Y}_i$ , (1) is

$$\tilde{Y}_i = \beta_0 + \beta_1 X_i + u_i + w_i \quad (3)$$

where  $w_i$  represents random measurement error.

$$\tilde{Y}_i = \beta_0 + \beta_1 X_i + u_i + w_i \quad (3)$$

$$v_i$$

$$\tilde{Y}_i = \beta_0 + \beta_1 X_i + \nu_i \qquad (4)$$

If the measurement error in Y,  $w_i$ , is random, then  $w_i$  is independently distributed of  $X_i$ .

- So  $E(w_i|X_i) = 0$ , and in which case,  $E(v_i|X_i) = 0$ .
- $\hat{\beta}_1$  is unbiased.

#### Potential Solutions to Errors-in-Variables Bias

1) Obtain better data; get more accurate measures of *X*.

- 2) Use instrumental variables regression (EC3304)
  - Involves searching for a variable ("instrumental" variable) that is correlated with the actual value  $X_i$  but is uncorrelated with the measurement error.

# 4. Sample Selection Bias

• So far, we have assumed simple random sampling of the population.

• In some cases, simple random sampling is thwarted because the dependent variable is observed only for a restricted (non-random) sample.

## **Example: Returns to Education**

What is the return to an additional year of education?

#### Empirical strategy:

- Sampling scheme: simple random sample of employed workers (employed, so we have wage data).
- Data: earnings & years of education.
- regress ln(earnings) on years\_education.
- Ignoring issues of omitted variable bias and measurement error for now – is there bias?

$$ln(Earnings_i) = \beta_0 + \beta_1 Years\_Educ_i + u_i$$

- We want to know how an additional year of schooling affects earnings for the *population of workers*.
- However, (positive) earnings are only observed for employed workers.
- If we only sample employed workers and run the regression on this sample,  $\hat{\beta}_1$  will be biased.
- because the effect on earnings of an additional year of schooling for employed workers does not give a reliable estimate of what the effect of an additional year of schooling would have been for unemployed workers had they been employed.

$$ln(Earnings_i) = \beta_0 + \beta_1 Years\_Educ_i + u_i$$

- Being in the sample means that you are employed.
- But employed and unemployed are likely to be different.
- Effect of an additional year of schooling for those employed might not represent the effect of an additional year of schooling for workers in general.

# **Potential Solution to Sample Selection Bias**

• Collect the sample in a way that avoids non-random sample selection:

• Returns to education example: random sample of all workers (including the unemployed).

# 5. Simultaneous Causality Bias

- we have assumed that *X* causes *Y*.
- but what if **Y** causes **X**, too?
- If so, there is *simultaneous causality* & the OLS estimator will be picking up *both effects*.
  - OLS estimator will be biased & inconsistent.

#### Example: Class size effect

- Low *STR* results in higher test scores.
- But, suppose that as a result of a political process: districts with low test scores are given extra resources to lower *STR* 
  - then low test scores would result in low *STR*
- What does this mean for a regression of *TestScore* on *STR*?

(a) Causal effect of *X* on *Y*:

$$Y_i = \beta_0 + \beta_1 X_i + u_i$$

(b) Causal effect of *Y* on *X* :

$$X_i = \gamma_0 + \gamma_1 Y_i + \nu_i$$

- fall in  $u_i$  means fall in  $Y_i$ ,
  - if  $\gamma_1 > 0$ , this *implies* fall in  $X_i$ .
- So  $Corr(u_i, X_i) \neq 0...$
- ...and  $\hat{\beta}_1$  is biased and inconsistent.

$$Y_i = \beta_0 + \beta_1 X_i + u_i$$

$$X_i = \gamma_0 + \gamma_1 Y_i + \nu i$$

- What is the sign of  $Corr(u_i, X_i)$  here?
- a. +
- b.

## **Potential Solutions to Simultaneous Causality Bias**

• Randomized controlled experiment:

- negates feedback from Y to X.
- Use instrumental variables regression

#### **Back to our Assessment**

# Kids with tuition fare worse

Analysis of Pisa data throws up surprising results for S'pore parents paying high tuition rates to help their children do well at school

rates tend to be high in countries where high-stakes exams prevail because parents see a need to prepare their children adequately for these assessments.

Because performance in exams such as the Primary School Leaving Examination, O and A levels plays an important role in determining admissions to selective schools and universities, it is not surprising that parents in Singapore focus a lot of attention on programmes they perceive will ensure their children's academic success.

So the growing prevalence of

- Does having tuition cause kids to do worse?
- Y: TestScore
- X: tuition dummy, age, gender, home language, nativity, number of people at home, parents' education, parents' employment status

 Could there still be omitted variables that could result in OVB?

Back in the 1990s, when I was a secondary school student, only a few of my friends had access to private tuition. Today, however, it is not uncommon for the majority of one's classmates to have this. Some may even have tuition in several subjects.

#### **Back to our Assessment**

# Kids with tuition fare worse

- Reverse Causality?
- Could test scores affect whether one enrolls in tuition?

Analysis of Pisa data throws up surprising results for S'pore parents paying high tuition rates to help their children do well at school

rates tend to be high in countries where high-stakes exams prevail because parents see a need to prepare their children adequately for these assessments.

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# **Regression Studies & External Validity**

- Whether one can generalise the results found in a study to other population & settings depends on how similar the populations and settings are.
- Can we generalise the class size results from California elementary school districts (in 1999) to:
  - Massachusetts elementary school districts in 1999?
  - Californian elementary school districts in 2015?
  - Californian universities in 1999?
  - Singapore elementary schools in 2015?

# Are Results of Fertility Studies done on the Nordic Countries Generalisable to Singapore?

- Experiences of Nordic countries show that pro-parenthood measures (financial support, leave provisions) lead to increases in fertility rates.
- Why aren't pro-parenthood policies working in Singapore?
- Differences in settings? Cultural norms?

#### **Class Size Effect**

Long history of conflicting findings.

**ASK: NUS Economists** 

# Reducing class size is good, but mind the costs

#### Kelvin Seah Kah Cheng

For The Straits Times

**Q** Does class size matter? **A** Earlier this year, the issue of whether to implement smaller class sizes in Singapore schools was hotly debated in Parliament.

the data collected by researchers for this purpose is problematic because it is based on observations. In such settings, students are not randomly assigned to different classes. So students from larger classes and those from smaller ones tend to be dissimilar.

For instance, in Singapore schools, less able students may be assigned to smaller classes (students enrolled in learning support programmes, for instance) while more able students are assigned to the regular larger.

Other scholars later found that Mr Hanushek's conclusions might have been misguided because not all the estimates included in his meta-analysis were equally reliable. Many of the estimates were based on research designs – like regressions – which would not have allowed for credible estimation of the class size effect.

More recent reviews of the literature, conducted for instance, by Northwestern University's Professor Diane Schanzenbach, focused on studies based on Joshua Angrist and co-researcher Victor Lavy.

Both studies show that smaller classes are effective in raising student achievement, and that the benefits of attending a smaller class are greater for students from low-income families.

Even though reducing class size may improve student learning, it does not mean that Singapore should necessarily go ahead with it.Reducing class size comes at a substantial cost. More teachers

#### California Class Size Effect

 We found evidence that reductions in class size improve test scores in California.

• i.e. class size has a *statistically significant* effect on test scores

• But does class size have a *practically important* effect on test scores?

# For simplicity, consider estimates from linear regressions again...

TABLE 7.1  Results of Regressions of Test Scores on the Student–Teacher Ratio and Student Characteristic Control Variables Using California Elementary School Districts								
Dependent variable: average test score in the	he district.		$\bigcap$					
Regressor	(1)	(2)	(3)	(4)	(5)			
Student–teacher ratio $(X_1)$	-2.28** (0.52)	-1.10* (0.43)	-1.00** (0.27)	-1.31** (0.34)	-1.01** (0.27)			
Percent English learners $(X_2)$		-0.650** (0.031)	-0.122** (0.033)	-0.488** (0.030)	-0.130** (0.036)			
Percent eligible for subsidized lunch $(X_3)$			-0.547** (0.024)		-0.529** (0.038)			
Percent on public income assistance $(X_4)$				-0.790** (0.068)	0.048 (0.059)			
Intercept	698.9** (10.4)	686.0** (8.7)	700.2** (5.6)	698.0** (6.9)	700.4** (5.5)			
Summary Statistics								
SER	18.58	14.46	9.08	11.65	9.08			
$\overline{R}^2$	0.049	0.424	0.773	0.626	0.773			
n	420	420	420	420	420			

These regressions were estimated using the data on K-8 school districts in California, described in Appendix 4.1. Standard errors are given in parentheses under coefficients. The individual coefficient is statistically significant at the \*5% level or \*\*1% significance level using a two-sided test.

#### . summarize str, detail

	_	-
•		r

1%	Percentiles 15.13898	Smallest 14		
5%	16.41658	14.20176		
			Ola a	420
10%	17.34573	14.54214	Obs	420
25%	18.58179	14.70588	Sum of Wgt.	420
			_	
50%	19.72321		Mean	19.64043
3070	13.72321	Largest	Std. Dev.	1.891812
7.50/	20 07102		Sta. Dev.	1.091012
75%	20.87183	24.95		
90%	21.87561	25.05263	Variance	3.578952
95%	22.64514	25.78512	Skewness	0253655
99%	24.88889	25.8	Kurtosis	3.609597

#### . summarize testscr, detail

#### testscr

1% 5% 10% 25%	Percentiles 612.65 623.15 630.375 640	Smallest 605.55 606.75 609 612.5	Obs Sum of Wgt.	420 420
50%	654.45	Lawract	Mean	654.1565
75%	666.675	Largest 699.1	Std. Dev.	19.05335
90%	679.1	700.3	Variance	363.0301
95%	685.5	704.3	Skewness	.0916151
99%	698.45	706.75	Kurtosis	2.745712

#### The End?

The module may be over, but there are still important issues to be addressed:

- How to handle (i) omitted variables that are not observable, (ii) measurement errors, (iii) simultaneous causality? (IV estimation, panel data)
- What if my dependent variable is binary? (logit/probit regression)
- How do I forecast inflation, interest rates etc.? (time series analysis)
- Answering the above questions requires further modification of regression techniques tune in to Econometrics II and III to find out how!

# **Consultations plus Additional Consultations**

- Please do approach me if you have any queries on the class material.
- My Friday (4pm-6pm) consultation sessions for this week remain unchanged.
- However, for next week, consultations will be held on 20 April (Thursday), 4pm-6pm instead of the usual Friday slot because of the end-of-semester Economics
  Department meeting will be held at that time.
- To better support you for your final exam revisions, I will also be setting up an additional consultation session on 26 April (Wednesday), 4pm-6pm.
- Consultations will be done through Zoom through the usual link:

https://nus-sg.zoom.us/j/83502944248?pwd=K2c1WENobVBXV0YrcEliUlh4Z2s5dz09

Meeting ID: 835 0294 4248

Passcode: 714459

#### **Reminder: Homework 2**

- 11 Apr (12pm) 14 Apr (7pm)
- Done through the "Canvas Quiz" Platform
- To access Homework 2, log on to Canvas
- Then on the left panel, click on "Quizzes" and you will be able to access the Homework.
- 20 MCQ questions

#### **Final Exam**

#### April 27<sup>th</sup>, Thursday, 5pm-7pm (2hrs)

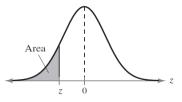
- Multi-part Short Answer Questions
- Closed book
- Coverage: All lectures
- Have a calculator with you
- Have your matric card with you
- Normal and F Tables can soon be found in Canvas under "Files" → "Supporting Materials for Final Exam (27 Apr, 5pm-7pm)"
- Venue: See next slide

Date	Topic	Chapters
		(Stock and Watson)
Week 1	Introduction and Overview	SW: Ch. 1
Week 2	Bivariate Linear Regression (I)	SW: Ch. 4
Week 3	Bivariate Linear Regression (II)	SW: Ch. 4,5
Week 4	Bivariate Linear Regression (III)	SW: Ch. 5
Week 5	Multiple Regression (I)	SW: Ch. 6
Week 6	Multiple Regression (II)	SW: Ch. 6,7
Week 7	Multiple Regression (III)	SW: Ch. 7
Week 8	Midterm Test: (No lecture this week)	
Week 9	Nonlinear Regression Functions (I)	SW: Ch. 8
Week 10	Nonlinear Regression Functions (II)	SW: Ch. 8
Week 11	Fixed Effects Regression	SW: Ch. 10
Week 12	Instrumental Variables Regression	SW: Ch. 12
Week 13	Assessment of Regression-based Studies and Conclusion	SW: Ch. 9

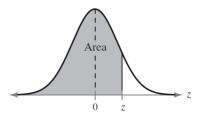
#### Venue for EC3303 final exam

- Students will soon be able to check the venue at Education Records System (EduRec)
- My Homepage > Academics > Examinations
- Click 'View Exam Schedule' and select '2022/2023 Semester 2'

## **Normal Table**

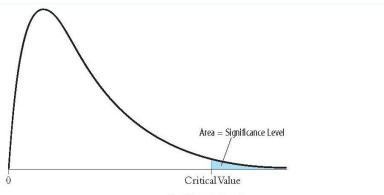


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-3.4	.0002	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003
-3.3	.0003	.0004	.0004	.0004	.0004	.0004	.0004	.0005	.0005	.0005
-3.2	.0005	.0005	.0005	.0006	.0006	.0006	.0006	.0006	.0007	.0007
-3.1	.0007	.0007	.0008	.0008	.0008	.0008	.0009	.0009	.0009	.0010
-3.0	.0010	.0010	.0011	.0011	.0011	.0012	.0012	.0013	.0013	.0013
-2.9	.0014	.0014	.0015	.0015	.0016	.0016	.0017	.0017	.0018	.0019
<b>-2.8</b>	.0019	.0020	.0021	.0021	.0022	.0023	.0023	.0024	.0025	.0026
-2.7	.0026	.0027	.0028	.0029	.0030	.0031	.0032	.0033	.0034	.0035
<b>-2.6</b>	.0036	.0037	.0038	.0039	.0040	.0041	.0043	.0044	.0045	.0047
-2.5	.0048	.0049	.0051	.0052	.0054	.0055	.0057	.0059	.0060	.0062
-2.4	.0064	.0066	.0068	.0069	.0071	.0073	.0075	.0078	.0080	.0082
-2.3	.0084	.0087	.0089	.0091	.0094	.0096	.0099	.0102	.0104	.0107
-2.2	.0110	.0113	.0116	.0119	.0122	.0125	.0129	.0132	.0136	.0139
-2.1	.0143	.0146	.0150	.0154	.0158	.0162	.0166	.0170	.0174	.0179
-2.0	.0183	.0188	.0192	.0197	.0202	.0207	.0212	.0217	.0222	.0228
-1.9	.0233	.0239	.0244	.0250	.0256	.0262	.0268	.0274	.0281	.0287
-1.8	.0294	.0301	.0307	.0314	.0322	.0329	.0336	.0344	.0352	.0359
-1.7	.0367	.0375	.0384	.0392	.0401	.0409	.0418	.0427	.0436	.0446
-1.6	.0455	.0465	.0475	.0485	.0495	.0505	.0516	.0526	.0537	.0548
-1.5	.0559	.0571	.0582	.0594	.0606	.0618	.0630	.0643	.0655	.0668
-1.4	.0681	.0694	.0708	.0722	.0735	.0749	.0764	.0778	.0793	.0808
-1.3	.0823	.0838	.0853	.0869	.0885	.0901	.0918	.0934	.0951	.0968
-1.2	.0985	.1003	.1020	.1038	.1056	.1075	.1093	.1112	.1131	.1151
-1.1	.1170	.1190	.1210	.1230	.1251	.1271	.1292	.1314	.1335	.1357
-1.0	.1379	.1401	.1423	.1446	.1469	.1492	.1515	.1539	.1562	.1587
-0.9	.1611	.1635	.1660	.1685	.1711	.1736	.1762	.1788	.1814	.1841
-0.8	.1867	.1894	.1922	.1949	.1977	.2005	.2033	.2061	.2090	.2119
-0.7	.2148	.2177	.2206	.2236	.2266	.2296	.2327	.2358	.2389	.2420
-0.6	.2451	.2483	.2514	.2546	.2578	.2611	.2643	.2676	.2709	.2743
-0.5	.2776	.2810	.2843	.2877	.2912	.2946	.2981	.3015	.3050	.3085
-0.4	.3121	.3156	.3192	.3228	.3264	.3300	.3336	.3372	.3409	.3446
-0.3	.3483	.3520	.3557	.3594	.3632	.3669	.3707	.3745	.3783	.3821
-0.2	.3859	.3897	.3936	.3974	.4013	.4052	.4090	.4129	.4168	.4207
-0.1	.4247	.4286	.4325	.4364	.4404	.4443	.4483	.4522	.4562	.4602
-0.0	.4641	.4681	.4721	.4761	.4801	.4840	.4880	.4920	.4960	.5000



z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9278	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

## **F** Table



#### Significance Level

Degrees of Freedom	10%	5%	1%
1	2.71	3.84	6.63
2	2.30	3.00	4.61
3	2.08	2.60	3.78
2 3 4 5	1.94	2.37	3.32
5	1.85	2.21	3.02
6	1.77	2.10	2.80
7	1.72	2.01	2.64
8	1.67	1.94	2.51
9	1.63	1.88	2.41
10	1.60	1.83	2.32
11	1.57	1.79	2.25
12	1.55	1.75	2.18
13	1.52	1.72	2.13
14	1.50	1.69	2.08
15	1.49	1.67	2.04
16	1.47	1.64	2.00
17	1.46	1.62	1.97
18	1.44	1.60	1.93
19	1.43	1.59	1.90
20	1.42	1.57	1.88
21	1.41	1.56	1.85
22	1.40	1.54	1.83
23	1.39	1.53	1.81
24	1.38	1.52	1.79
25	1.38	1.51	1.77
26	1.37	1.50	1.76
27	1.36	1.49	1.74
28	1.35	1.48	1.72
29	1.35	1.47	1.71
30	1.34	1.46	1.70

This table contains the  $90^{\text{th}}$ ,  $95^{\text{th}}$ , and  $99^{\text{th}}$  percentiles of the  $F_{m,\infty}$  distribution. These serve as critical values for tests with significance levels of 10%, 5%, and 1%.

#### How to prepare for Final Exam?

- Read lecture notes carefully
  - Only material covered in lecture will be tested
- Practice HW and tutorial questions
- No need to memorize STATA commands, apart from those covered in the *Lecture*