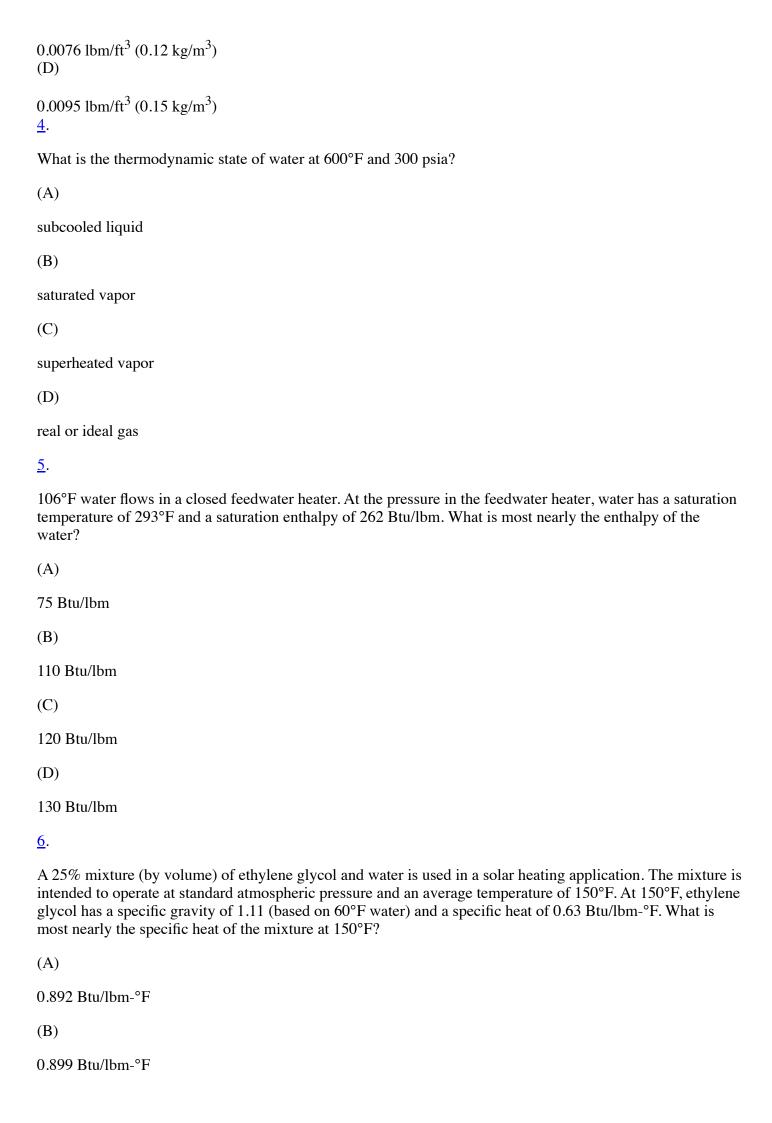
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<u>Chapter 10. Thermodynamic Properties of Substances</u>

Practice Problems <u>1</u>. The molar enthalpy of 250°F (120°C) steam with a quality of 92% is most nearly (A) 16,000 Btu/lbmol (37 MJ/kmol) (B) 18,000 Btu/lbmol (41 MJ/kmol) (C) 20,000 Btu/lbmol (46 MJ/kmol) (D) 22,000 Btu/lbmol (51 MJ/kmol) <u>2</u>. The ratio of specific heats for air at 600°F (300°C) is most nearly (A) 1.33 (B) 1.38 (C) 1.41 (D) 1.67 <u>3</u>. The density of helium at 600°F (300°C) and one standard atmosphere is most nearly (A) $0.0052 \text{ lbm/ft}^3 (0.085 \text{ kg/m}^3)$ (B) $0.0061 \text{ lbm/ft}^3 (0.098 \text{ kg/m}^3)$

(C)



(C)

0.908 Btu/lbm-°F

(D)

0.913 Btu/lbm-°F

Solutions

<u>1</u>.

Customary U.S. Solution

From appendixMERM24A (also *NCEES Handbook*: Properties of Saturated Steam (U.S. Customary Units)), for 250°F steam, the enthalpy of saturated liquid, h_f , is 218.6 Btu/lbm. The heat of vaporization, h_{fg} , is 945.4 Btu/lbm. The enthalpy is given by equationMERM24040 (also *NCEES Handbook*: Properties for Two-Phase (Vapor-Liquid) Systems).

$$h = h_f + x h_{fg} = 218.6 \ rac{
m Btu}{
m lbm} + (0.92) \left(945.4 \ rac{
m Btu}{
m lbm}
ight) \ = 1088.4 \
m Btu/lbm$$

As in *NCEES Handbook* table "Temperature-Independent Properties of Liquids and Gases (U.S. Units)," the molecular weight of water is 18 lbm/lbmol. The molar enthalpy is given by equationMERM24014.

$$H = (MW)h = \left(18 \frac{\text{lbm}}{\text{lbmol}}\right) \left(1088.4 \frac{\text{Btu}}{\text{lbm}}\right)$$

= 19,591 Btu/lbmol (20,000 Btu/lbmol)

The answer is (C).

SI Solution

From appendixMERM24N (also *NCEES Handbook:* Saturated Steam (SI Units), for 120°C steam, the enthalpy of saturated liquid, h_f , is 503.81 kJ/kg. The heat of vaporization, h_{fg} , is 2202.1 kJ/kg. The enthalpy is given by equationMERM24040 (also *NCEES Handbook:* Properties for Two-Phase (Vapor-Liquid) Systems).

$$h = h_f + x h_{fg} = 503.81 \; rac{ ext{kJ}}{ ext{kg}} + (0.92) \left(2202.1 \; rac{ ext{kJ}}{ ext{kg}}
ight) \ = 2529.7 \; ext{kJ/kg}$$

As in *NCEES Handbook* table "Temperature-Independent Properties of Liquids and Gases (SI Units)," the molecular weight of water is 18 kg/kmol. Molar enthalpy is given by equationMERM24014.

$$H = ext{MW} imes h = \left(18 \ rac{ ext{kg}}{ ext{kmol}}
ight) \left(2529.7 \ rac{ ext{kJ}}{ ext{kg}}
ight)$$
 $= 45535 \ ext{kJ/kmol} \quad (46 \ ext{MJ/kmol})$

The answer is (C).

<u>2</u>.

Customary U.S. Solution

As in NCEES Handbook: Temperature, the absolute temperature is

$$600^{\circ} \text{F} + 460^{\circ} = 1060^{\circ} \text{R}$$

From tableCERM24001 (also *NCEES Handbook:* Temperature-Dependent Properties of Air (U.S. Customary Units)), the specific heat at constant pressure for air at 1060°R is

$$c_p = 0.250 \, rac{
m Btu}{
m lbm-{}^\circ R}$$

From equationMERM24095(b) (also *NCEES Handbook*: Ideal Gas Law),

$$egin{array}{ll} c_v &= c_p - rac{R}{J} \ &= 0.250 \; rac{
m Btu}{
m lbm^{\circ} R} - rac{1545.35 \; rac{
m ft ext{-} lbf}{
m lbmol^{\circ} R}}{\left(778 \; rac{
m ft ext{-} lbf}{
m Btu}
ight) \left(28.967 \; rac{
m lbm}{
m lbmol}
ight)} \ &= 0.1814 \;
m Btu/lbm^{\circ} R \end{array}$$

The ratio of specific heats is given by equationMERM24028.

$$k = rac{c_p}{c_v} = rac{0.250 rac{
m Btu}{
m lbm-{}^{\circ}R}}{0.1814 rac{
m Btu}{
m lbm-{}^{\circ}R}} = 1.378 \quad (1.38)$$

The answer is (B).

SI Solution

From tableCERM24001 (also *NCEES Handbook:* Temperature-Dependent Properties of Air (SI Units)), the specific heat at constant pressure for air is

$$c_p = 1.047 \text{ kJ/kg} \cdot \text{K}$$

From equationMERM24095(a) (also NCEES Handbook: Ideal Gas Law),

$$egin{aligned} c_v &= c_p - rac{R}{J} \ &= \left(1.047 rac{ ext{kJ}}{ ext{kg·K}}
ight) \left(1000 rac{ ext{J}}{ ext{kJ}}
ight) - rac{8.3145}{0.0289} rac{ ext{J}}{rac{ ext{mol·K}}{ ext{mol}}} \ &= 760 ext{ J/kg·K} \end{aligned}$$

The ratio of specific heats is given by equationMERM24028.

$$k = \frac{c_p}{c_v} = \frac{\left(1.047 \frac{\mathrm{kJ}}{\mathrm{kg \cdot K}}\right) \left(1000 \frac{\mathrm{J}}{\mathrm{kJ}}\right)}{760 \frac{\mathrm{J}}{\mathrm{kg \cdot K}}}$$

$$= 1.377 \quad (1.38)$$

The answer is (B). 3.

Customary U.S. Solution

As in NCEES Handbook: Temperature, the absolute temperature is

$$600\degree F + 460\degree = 1060\degree R$$

From equationMERM24050 (also NCEES Handbook: Ideal Gas Law), the density of helium is

$$\rho = \frac{p}{RT} = \frac{\left(14.7 \frac{\text{lbf}}{\text{in}^2}\right) \left(12 \frac{\text{in}}{\text{ft}}\right)^2 \left(4 \frac{\text{lbm}}{\text{lbmol}}\right)}{\left(1545.35 \frac{\text{ft-lbf}}{\text{lbmol-'R}}\right) (1060 \text{ R})}$$
$$= 0.00517 \text{ lbm/ft}^3 \quad \left(0.0052 \text{ lbm/ft}^3\right)$$

The answer is (A).

As in NCEES Handbook: Temperature, the absolute temperature is

$$300^{\circ}\text{C} + 273^{\circ} = 573\text{K}$$

From equationMERM24050 (also NCEES Handbook: Ideal Gas Law), the density of helium is

$$ho = rac{p}{RT} = rac{(101\,300\ ext{Pa}) \left(4\ rac{ ext{g}}{ ext{mol}}
ight)}{\left(8314.5\ rac{ ext{J}}{ ext{kmol}\cdot ext{K}}
ight) (573 ext{K})} = 0.085\ ext{kg/m}^3$$

The answer is (A).

<u>4</u>.

As in *NCEES Handbook* table "Superheated Steam (U.S. Units)" the saturation temperature for 300 psia steam is 417°F, so since the water's temperature is higher than this, the water is either a superheated vapor or a gas. The critical temperature for water is 705°F, so the water can't be considered a gas. Therefore, it is a superheated vapor.

The answer is (C).

<u>5</u>.

Since the pressure of the water in the feedwater heater is not given, a subcooled liquid table can't be used directly. (The saturation temperature could be used to find the pressure, however, if this approach was taken.) As in *NCEES Handbook* table "Physical Properties of Liquid Water (U.S. Units)" the specific heat of liquid water is approximately 1 Btu/lbm-°F, which is the reason that saturated liquid enthalpy and saturation temperature have essentially the same numerical values. Calculate the subcooled enthalpy by subtracting the sensible heat from 106°F to 293°F.

$$egin{aligned} h_{106\,^{\circ}\mathrm{F}} &= h_{\mathrm{saturation}} - c_p \left(T_{\mathrm{saturation}} - T
ight) \ &= 262 \, rac{\mathrm{Btu}}{\mathrm{lbm}} - \left(1 \, rac{\mathrm{Btu}}{\mathrm{lbm}\text{-}^{\circ}\mathrm{F}}
ight) (293\,^{\circ}\mathrm{F} - 106\,^{\circ}\mathrm{F}) \ &= 75 \, \mathrm{Btu/lbm} \end{aligned}$$

The answer is (A).

<u>6</u>.

Use a saturated steam table, such as appendixMERM24A (also *NCEES Handbook* table "Properties of Saturated Steam (U.S. Units)—Temperature Table") to get the properties of 150°F water. The specific volume is the reciprocal of the density. Since $\Delta h = c_p \Delta T$, the specific heat can be found from the change in enthalpy over a known temperature range. Use the saturation enthalpies at 140°F and 160°F.

$$\begin{split} \rho &= \frac{1}{v_f} \\ &= \frac{1}{0.01634 \, \frac{\text{ft}^3}{\text{lbm}}} \\ &= 61.20 \, \text{lbm/ft}^3 \\ c_{p,\text{water}} &= \frac{h_{\text{sat},T_2} - h_{\text{sat},T_1}}{T_2 - T_1} \\ &= \frac{128.00 \, \frac{\text{Btu}}{\text{lbm}} - 107.99 \, \frac{\text{Btu}}{\text{lbm}}}{160\, ^{\circ}\text{F} - 140\, ^{\circ}\text{F}} \\ &= 1.00 \, \text{Btu/lbm-} ^{\circ}\text{F} \end{split}$$

Specific heats of liquid mixtures are gravimetrically weighted.

Consider 1 ft³ of mixture, containing 0.25 ft³ of ethylene glycol and 1 - 0.25 ft³ = 0.75 ft³ water. The gravimetric fraction of ethylene glycol, $G_{\rm glycol}$, in the mixture is

$$egin{align*} G_{
m glycol} &= rac{m_{
m glycol}}{m_{
m glycol} + m_{
m water}} \ &= rac{{
m SG}_{
m glycol}
ho_{
m water, 60\,^{\circ}F} V_{
m glycol}}{{
m SG}_{
m glycol}
ho_{
m water, 60\,^{\circ}F} V_{
m glycol} +
ho_{
m water, 150\,^{\circ}F} V_{
m water}} \ &= rac{\left(1.11
ight) \left(62.4 rac{
m lbm}{
m ft^3}
ight) \left(0.25
m ft^3
ight)}{\left(1.11
ight) \left(62.4 rac{
m lbm}{
m ft^3}
ight) \left(0.25
m ft^3
ight)} \ &+ \left(61.2 rac{
m lbm}{
m ft^3}
ight) \left(0.75
m ft^3
ight)} \ &= 0.274 \end{gathered}$$

The gravimetric fraction of water in the mixture is

$$G_{
m water} = 1 - G_{
m glycol} = 1 - 0.274 = 0.726$$

The specific heat of the mixture is

$$egin{aligned} c_{p, ext{mixture}} &= G_{ ext{glycol}} c_{p, ext{ glycol}} + G_{ ext{water}} c_{p, ext{water}} \ &= (0.274) \left(0.63 \, rac{ ext{Btu}}{ ext{lbm-}\,^{\circ} ext{F}}
ight) \ &+ (0.726) \left(1.00 \, rac{ ext{Btu}}{ ext{lbm-}\,^{\circ} ext{F}}
ight) \ &= 0.899 \, ext{Btu/lbm-}\,^{\circ} ext{F} \end{aligned}$$

The answer is (B).