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Algorithm 8.1. Modified Gram-Schmidt

for $i = 1$ to n $v_i = a_i$ for $i = 1$ to n $r_{ii} = \|v_i\|$ $q_i = v_i / r_{ii}$ for $j = i + 1$ to n $r_{ij} = q_i^T v_j$ $v_j = v_j - r_{ij} q_i$ mult: m add: $m-1$ div: m mult: m add: $m-1$ sub: m mult: m

$$\therefore \text{add} \quad (m-1) \times n + \sum_{i=1}^n (m-1) \left(\frac{n(n+1)}{2} - \frac{i(i+1)}{2} \right)$$

$$\text{sub} \quad m \sum_{i=1}^m \left(\frac{n(n+1)}{2} - \frac{i(i+1)}{2} \right)$$

$$\text{div} \quad mn$$

$$\text{mult} \quad mn + m \sum_{i=1}^n (n(n+1) - i(i+1))$$

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$$R_i = \begin{bmatrix} I & 0 & \dots & 0 \\ 0 & 1 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & 1 \end{bmatrix}$$

Handwritten annotations for the matrix structure:

- Red bracket above the first row: $(i-1)$
- Red bracket to the left of the first column: $(i-1)$
- Red bracket to the left of the first column: $(n-i+1)$
- Red bracket below the first column: $(n-i+1)$
- Red bracket below the first column: $(n-i+1)$