## grover

## May 28, 2022

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[]: #initialization
     import matplotlib.pyplot as plt
     import numpy as np
     import math
     # importing Qiskit
     from qiskit import IBMQ, Aer, assemble, transpile
     from qiskit import QuantumCircuit, ClassicalRegister, QuantumRegister
     from qiskit.providers.ibmq import least_busy
     # import basic plot tools
     from qiskit.visualization import plot_histogram
     from qiskit_textbook.tools import vector2latex
[ ]: | n = 4 
[]: def apply_oracle(qc):
         # Oracle
         qc.h([2,3])
         qc.ccx(0,1,2)
         qc.h(2)
         qc.x(2)
         qc.x([1,3])
         qc.ccx(0,2,3)
         qc.x(2)
         qc.h(3)
         qc.x([1,3])
         qc.h(2)
         qc.mct([0,1,3],2)
         qc.x([1,3])
         qc.h(2)
         qc.x(2)
         return qc
[]: def diffuser(nqubits):
         qc = QuantumCircuit(nqubits)
         # Apply transformation |s\rangle \rightarrow |00..0\rangle (H-gates)
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for qubit in range(nqubits):
             qc.h(qubit)
         # Apply transformation |00..0> -> |11..1> (X-gates)
         for qubit in range(nqubits):
             qc.x(qubit)
         # Do multi-controlled-Z gate
         qc.h(nqubits-1)
         qc.mct(list(range(nqubits-1)), nqubits-1) # multi-controlled-toffoli
         qc.h(nqubits-1)
         # Apply transformation | 11..1> -> | 00..0>
         for qubit in range(nqubits):
             qc.x(qubit)
         # Apply transformation | 100..0> -> |s>
         for qubit in range(nqubits):
             qc.h(qubit)
         # We will return the diffuser as a gate
         U_s = qc.to_gate()
         U_s.name = "U_s_s"
         return U_s
[]: def initialize_s(qc, qubits):
         """Apply a H-gate to 'qubits' in qc"""
         for q in qubits:
             qc.h(q)
         return qc
[]: grover_circuit = QuantumCircuit(n)
     all_qubits = list(range(n))
     grover_circuit = initialize_s(grover_circuit,all_qubits)
     grover_circuit = apply_oracle(grover_circuit)
     grover_circuit.append(diffuser(n), all_qubits)
     grover_circuit.measure_all()
     grover_circuit.draw()
[]:
                                             0
                                                        M ≫
        q_0:
              Η
                            X
                                           Х
              Η
                        X
                                                 1
        q_1:
                                               U$_s$
                               Х
        q_2:
                       Х
                           Η
                                      Х
                                          Η
                                              Х
                                                  Η
                                                       X
        q_3:
              Η
                  Η
                       Х
                                Х
                                    Η
                                         Х
                                               Х
                                                      3
    meas: 4/
                                                    >>
                                                                                    0 >>
        q_0:
```

```
«
     «
         q_1: M
     «
         q_2:
                Μ
     «
     «
         q_3:
                  Μ
     «meas: 4/
               1 2 3
[ ]: aer_sim = Aer.get_backend('aer_simulator')
     transpiled_grover_circuit = transpile(grover_circuit, aer_sim)
     qobj = assemble(transpiled_grover_circuit)
     results = aer_sim.run(qobj).result()
     counts = results.get_counts()
     print(counts)
     plot_histogram(counts)
    {'0110': 3, '0111': 2, '0010': 3, '1001': 4, '0000': 5, '0101': 5, '0001': 3,
    '0011': 2, '1101': 7, '1111': 3, '0100': 3, '1100': 175, '1000': 190, '1110':
    197, '1010': 208, '1011': 214}
[]:
             0.24
                                                          0.203
                                                                         0.192
                                                   0.186
                                                                  0.171
             0.18
         Probabilities
             0.12
```

0.06

0.00

 $0.\underline{00}$  50.0030.0030.0020.0030.0050.0030.002

0.007

0.003

0.004

0001 0010 0100 0101 0110 1001 1100 1100 1110