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Zhaoyi Jiang	
CESG504 HW1	

HW1 P2d

```
figure(1)
A=3;
E=10000000;
hold on
fplot(@(x) (34400*x-x^5/2000)/(A*E))
xlim([0 60])
ylim([0 0.06])
fem3=[0 0.02288 0.04416 0.05584];
sp3=[0 20 40 60];
fem4=[0 0.01719 0.03399 0.04852 0.05584];
sp4=[0 15 30 45 60];
plot(sp3,fem3,'-r*',sp4,fem4,'-k*')
title('HW1 P2d u(x)')
xlabel('Length')
ylabel('u(x)')
legend({'Exact','3 Elements','4 Elements'},'Location','northwest')
hold off
figure(2)
A=3;
E=10000;
hold on
fplot(@(x) (34400-x^4/400)/3000)
xlim([0 60])
ylim([0 14])
sigma3=[0.001145*E 0.001064*E 0.000584*E 0.000584*E];
sp3=[0 20 40 60];
sigma4=[0.001146*E 0.00112*E 0.000969*E 0.000488*E 0.000488*E];
sp4=[0 15 30 45 60];
stairs(sp3,sigma3,'-r')
stairs(sp4,sigma4,'-k')
title('HW1 P2d Sigma')
xlabel('Length')
```

```
ylabel('Sigma')
legend('Exact','3 Elements','4 Elements')
hold off
```

Warning: Function behaves unexpectedly on array inputs. To improve performance,

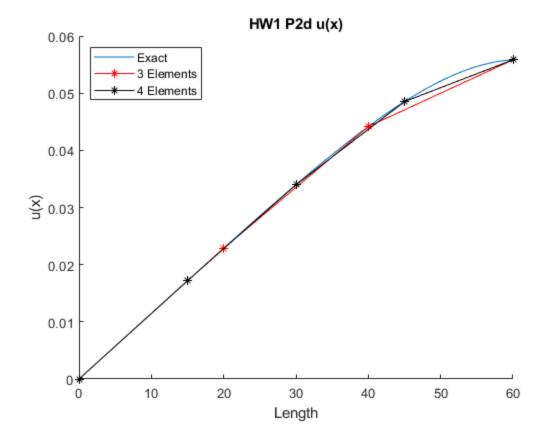
properly vectorize your function to return an output with the same size and

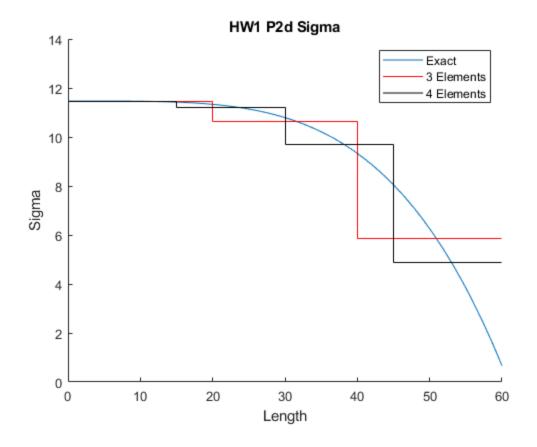
shape as the input arguments.

Warning: Function behaves unexpectedly on array inputs. To improve performance,

properly vectorize your function to return an output with the same size and

shape as the input arguments.





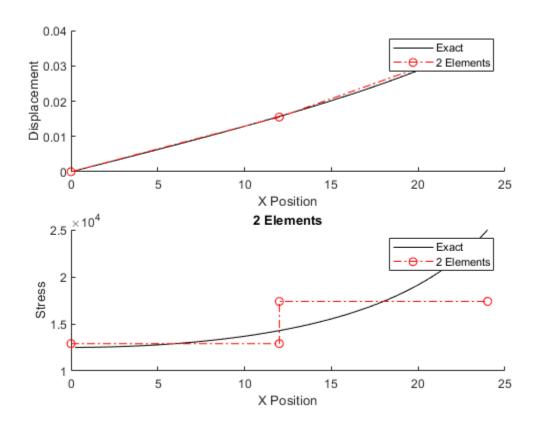
HW1 P4 2elements

```
E=10000000; %Pa
2 2
%%%%%%%% nodal information matrix %%%%%%%%%
응 응
    % x location | fixity (1=fixed, 0=free)
n info=
      [ 0
             1;
      L/2
             0;8 %
            01;
              응 응
%%%%%%% element information matrix %%%%%%%%%
% i node, j node, E
e_info=[1,
        2,
            Ε;
        3,
            E];
               응 응
numelem=size(e info,1); %number of elements
응 응
P=50000; %Applied Load
b=0; %m/s^2
P_loaded_Node=numelem+1; %<- in this case, the point load is applied
at the end of the rod
                %
응 응
%%%%% EXACT SOLUTION for displacement (used for plotting) %%%%%
               응 응
syms u(x) x
               왕 왕
% u(x)=?; %<- exact solution (Change this using your acquired solution
to problem 2a)
```

```
u(x) = (P*L/(E*(A0*(A1-A0))^0.5))*atan((x/L)*(1/sqrt(A0))*sqrt(A1-A0))
 %(exact soln - problem 4) % %
응
%END
                ____user
                                    input
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% DO NOT MODIFY BELOW, UNLESS YOU
SAVED
888888888888888888888888888888885555
% initializing arrays for Stiffness Matrix and FVector = fixed end
forces + applied loads
Kglob=zeros(nnodes,nnodes);
Fglob=zeros(nnodes,1);
uFE_soln=zeros(length(Fglob),1);
endNodesLocList=[]; %< used for plotting only</pre>
for i=1:size(e info,1);
   currentElemCenterXloc=(n_info(e_info(i,1),1) +
n_{info}(e_{info}(i,2),1))/2; %element center=(x location of i node + x
location of j node)/2
   L_elem(i) = (n_info(e_info(i,2),1) - n_info(e_info(i,1),1)); %<-
determining the length of the current element
   qetArea %< getting element x-sec area by calling subroutine (EDIT
THIS FOR NONPRISMATIC SECTION)
       %< getting element stiffness by calling subroutine (also
included at end as a comment)
   KeLinear1DRoddivA(i,:,:)=KeLinear1DRod./ElA;
   % Global Stiffness Matrix assembly
   curr doflist=[e info(i,1),e info(i,2)];
   Fe=[(b*L elem/2);(b*L elem/2)];
   for j=1:length(curr doflist);
      for jj=1:length(curr_doflist);
Kglob(curr_doflist(j),curr_doflist(jj))=Kglob(curr_doflist(j),curr_doflist(jj))+K
      Fglob(curr_doflist(j))=Fglob(curr_doflist(j)) + Fe(j);
   end
```

```
endNodesLocList=[endNodesLocList,n_info(e_info(i,1),1),n_info(e_info(i,2),1)];
  %< used for plotting only
end
xExact=L.*[1:100]./100;
uExact=u(xExact); %<- exact solution for the displacement
du=symfun(diff(u(x),x),x);
sExact=E*du(xExact);
constlin=find(n info(:,2));
Kglob(constlin,:)=[];
Kglob(:,constlin)=[];
Fglob(P_loaded_Node)=Fglob(P_loaded_Node)+P;
Fqlob(constlin,:)=[];
ulin=Kglob\Fglob; %<- solving the system of equations
uFE_soln(setdiff(1:end,constlin),:)=ulin;
eFE_soln=uFE_soln./L_elem;
for ijk=1:numelem;
    jkl=ijk+1;
Stress_FE(ijk,:) = abs(reshape(KeLinear1DRoddivA(ijk,:,:),[2
 2])*(uFE_soln(jkl-1:jkl)-uFE_soln(jkl-1)));
end
Stress FE=reshape(Stress FE',[numelem*2,1]);
if flag==1;
figure;
subplot(2,1,1)
hold on;
plot(xExact, uExact, 'k');
plot(n_info(:,1),uFE_soln,['-.or']);
leg(:,end+1)={string(size(e_info,1))+' Elements'};
xlabel('X Position')
ylabel('Displacement');
subplot(2,1,2)
hold on;
plot(xExact,sExact,'k');
plot(endNodesLocList,Stress_FE,['-.or']);
xlabel('X Position')
ylabel('Stress');
flag=0;
```

```
else
subplot(2,1,1)
hold on;
plot(n_info(:,1),uFE_soln,['-.or']);
leg(:,end+1)={string(size(e_info,1))+' Elements'};
subplot(2,1,2)
hold on;
plot(endNodesLocList,Stress_FE,['-.or']);
end
title('2 Elements')
subplot(2,1,1)
legend(leg)
subplot(2,1,2)
legend(leg)
u(x) =
-(2^{(1/2)*}atan((2^{(1/2)*}x*1i)/48)*3i)/100
```



HW1 P4 8elements

clc

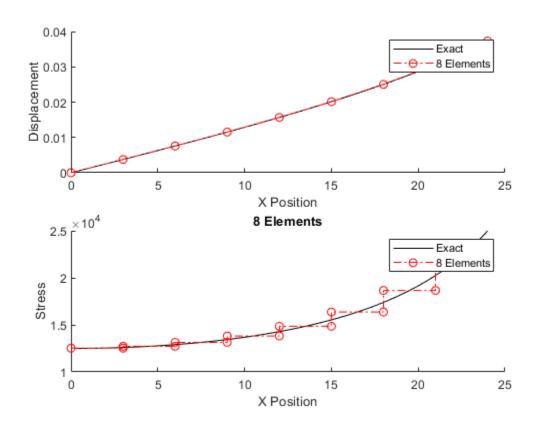
```
clear all
close all
% NOTE: YOU WILL HAVE TO EDIT THE FUNCTION getArea.m
                  % TO ENSURE THAT THE A(x) FUNCTION MATCHES WHAT IS SPECIFIED IN
PROBLEM 4 %
leg={'Exact'};
flag=1;
                  ____user input
%BEGIN _
                        % %
                 응 응
A0=4; %in^2 <- area at LHS of rod
                  응 응
A1=2; %in^2 <- area at RHS of rod
L=24; %m
                   % %
E=10000000; %Pa
%%%%%%% nodal information matrix %%%%%%%%%
% %
     % x location | fixity (1=fixed, 0=free)
n info=
       [ 0
                1;
        L/8
                0;
                0;
        L*2/8
        L*3/8
                0;
        L*4/8
                0;
        L*5/8
                 0;
        L*6/8
                0;
        L*7/8
                0;8 %
              0];
%%%%%%% element information matrix %%%%%%%%%
% i node, j node, E
e_info=[1, 2, 2, 2, 3,
              E;
              Ε
```

8

```
3,
      4,
      5,
    4,
   5,
          E
       6,
   6,
      7,
          E
   7,
       8,
   8,
       9,
          E];
응 응
numelem=size(e_info,1); %number of elements
             응 응
8 8
P=50000; %Applied Load
b=0; %m/s^2
            응 응
P_loaded_Node=numelem+1; %<- in this case, the point load is applied
at the end of the rod % %
응 응
%%%%% EXACT SOLUTION for displacement (used for plotting) %%%%%%
syms u(x) x
% u(x)=?; %<- exact solution (Change this using your acquired solution
to problem 2a)
            응 응
            응 응
u(x) = (P*L/(E*(A0*(A1-A0))^0.5))*atan((x/L)*(1/sqrt(A0))*sqrt(A1-A0))
 %(exact soln - problem 4) % %
$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$$
           ____user
                      input
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% DO NOT MODIFY BELOW, UNLESS YOU
SAVED
```

```
% initializing arrays for Stiffness Matrix and FVector = fixed end
 forces + applied loads
Kglob=zeros(nnodes,nnodes);
Fglob=zeros(nnodes,1);
uFE_soln=zeros(length(Fglob),1);
endNodesLocList=[]; %< used for plotting only</pre>
for i=1:size(e_info,1);
    currentElemCenterXloc=(n_info(e_info(i,1),1) +
 n info(e info(i,2),1))/2; %element center=(x location of i node + x
 location of j node)/2
    L_elem(i) = (n_info(e_info(i,2),1) - n_info(e_info(i,1),1)); %<-
 determining the length of the current element
    getArea %< getting element x-sec area by calling subroutine (EDIT
 THIS FOR NONPRISMATIC SECTION)
          %< getting element stiffness by calling subroutine (also
 included at end as a comment)
    KeLinear1DRoddivA(i,:,:)=KeLinear1DRod./ElA;
    % Global Stiffness Matrix assembly
    curr doflist=[e info(i,1),e info(i,2)];
    Fe=[(b*L_elem/2);(b*L_elem/2)];
    for j=1:length(curr_doflist);
        for jj=1:length(curr_doflist);
 Kglob(curr_doflist(j),curr_doflist(jj))=Kglob(curr_doflist(j),curr_doflist(jj))+K
        end
        Fglob(curr_doflist(j))=Fglob(curr_doflist(j)) + Fe(j);
    end
 endNodesLocList=[endNodesLocList,n_info(e_info(i,1),1),n_info(e_info(i,2),1)];
  %< used for plotting only
end
xExact=L.*[1:100]./100;
uExact=u(xExact); %<- exact solution for the displacement</pre>
du=symfun(diff(u(x),x),x);
sExact=E*du(xExact);
constlin=find(n_info(:,2));
Kglob(constlin,:)=[];
Kglob(:,constlin)=[];
```

```
Fglob(P loaded Node)=Fglob(P loaded Node)+P;
Fglob(constlin,:)=[];
ulin=Kglob\Fglob; %<- solving the system of equations</pre>
uFE soln(setdiff(1:end,constlin),:)=ulin;
eFE_soln=uFE_soln./L_elem;
for ijk=1:numelem;
    jkl=ijk+1;
Stress_FE(ijk,:)=abs(reshape(KeLinear1DRoddivA(ijk,:,:),[2
 2])*(uFE soln(jkl-1:jkl)-uFE soln(jkl-1)));
end
Stress_FE=reshape(Stress_FE',[numelem*2,1]);
if flag==1;
figure;
subplot(2,1,1)
hold on;
plot(xExact, uExact, 'k');
plot(n_info(:,1),uFE_soln,['-.or']);
leg(:,end+1)={string(size(e info,1))+' Elements'};
xlabel('X Position')
ylabel('Displacement');
subplot(2,1,2)
hold on;
plot(xExact, sExact, 'k');
plot(endNodesLocList,Stress_FE,['-.or']);
xlabel('X Position')
ylabel('Stress');
flag=0;
else
subplot(2,1,1)
hold on;
plot(n_info(:,1),uFE_soln,['-.or']);
leg(:,end+1)={string(size(e_info,1))+' Elements'};
subplot(2,1,2)
hold on;
plot(endNodesLocList,Stress_FE,['-.or']);
end
title('8 Elements')
subplot(2,1,1)
legend(leg)
subplot(2,1,2)
legend(leg)
u(x) =
```



HW1 P4 20elements

```
clc
clear all
close all
% NOTE: YOU WILL HAVE TO EDIT THE FUNCTION getArea.m
% TO ENSURE THAT THE A(x) FUNCTION MATCHES WHAT IS SPECIFIED IN
PROBLEM 4
leg={'Exact'};
flag=1;
%BEGIN _
                                  _ user
                                              input
                         응
                            응
                          %
A0=4; %in^2 <- area at LHS of rod
                         응 응
A1=2; %in^2 <- area at RHS of rod
```

```
L=24; %m
                     응 응
E=10000000; %Pa
                   응 응
% %
%%%%%%%% nodal information matrix %%%%%%%%%
% %
      % x location | fixity (1=fixed, 0=free)
                     응 응
n info=
        [ 0
                  1;
        L*1/20
                    0;
         L*2/20
                    0;
         L*3/20
                    0;
         L*4/20
                    0;
         L*5/20
                    0;
         L*6/20
                    0;
         L*7/20
                    0;
         L*8/20
                    0;
        L*9/20
                    0;
                    0;
         L*10/20
         L*11/20
                     0;
        L*12/20
                     0;
         L*13/20
                     0;
         L*14/20
                     0;
         L*15/20
                     0;
         L*16/20
                     0;
         L*17/20
                     0;
         L*18/20
         L*19/20
                     0;
                0;];
응 응
%%%%%%% element information matrix %%%%%%%%%
                     응 응
% i node, j node, E
                     응 응
e_info=[1,
           2,
                E;
      2,
           3,
                Ε
                Е
      3,
           4,
      4,
                Ε
           5,
      5,
           6,
                Ε
                Е
      6,
           7,
      7,
                Ε
           8,
      8,
           9,
      9,
           10,
                Ε
      10,
           11,
               E
```

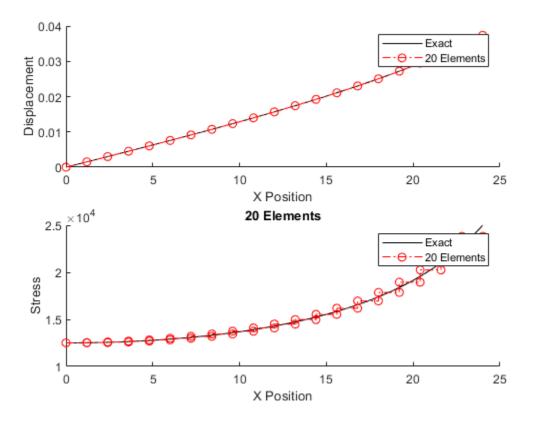
```
11,
        12,
            Ε
    12,
        13,
             \mathbf{E}
    13,
        14,
             Ε
    14,
        15,
             Ε
    15,
        16,
            E
    16,
        17,
             Ε
    17,
        18,
            E
        19,
    18,
            E
            E
    19,
        20,
            E];
    20,
        21,
                %
numelem=size(e_info,1); %number of elements
              응 응
              응 응
응 응
왕 왕
P=50000; %Applied Load
b=0; %m/s^2
               %
P loaded Node=numelem+1; %<- in this case, the point load is applied
at the end of the rod % %
응 응
%%%%% EXACT SOLUTION for displacement (used for plotting) %%%%%
syms u(x) x
               % %
% u(x)=?; %<- exact solution (Change this using your acquired solution
to problem 2a) % %
              응 응
u(x) = (P*L/(E*(A0*(A1-A0))^0.5))*atan((x/L)*(1/sqrt(A0))*sqrt(A1-A0))
 %(exact soln - problem 4) % %
응 응
____user input
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% DO NOT MODIFY BELOW, UNLESS YOU
SAVED
```

```
nnodes=numelem+1;
                     %number of nodes in the linear element system
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%5555
% initializing arrays for Stiffness Matrix and FVector = fixed end
forces + applied loads
Kglob=zeros(nnodes,nnodes);
Fglob=zeros(nnodes,1);
uFE_soln=zeros(length(Fglob),1);
endNodesLocList=[]; %< used for plotting only
for i=1:size(e info,1);
    currentElemCenterXloc=(n_info(e_info(i,1),1) +
n_{info}(e_{info}(i,2),1))/2; %element center=(x location of i node + x
 location of j node)/2
    L_elem(i) = (n_info(e_info(i,2),1) - n_info(e_info(i,1),1)); %<-
determining the length of the current element
    getArea %< getting element x-sec area by calling subroutine (EDIT
THIS FOR NONPRISMATIC SECTION)
          %< getting element stiffness by calling subroutine (also</pre>
 included at end as a comment)
   KeLinear1DRoddivA(i,:,:)=KeLinear1DRod./ElA;
    % Global Stiffness Matrix assembly
    curr doflist=[e info(i,1),e info(i,2)];
    Fe=[(b*L_elem/2);(b*L_elem/2)];
    for j=1:length(curr_doflist);
        for jj=1:length(curr_doflist);
 Kqlob(curr doflist(j),curr doflist(jj))=Kqlob(curr doflist(j),curr doflist(jj))+K
       Fglob(curr_doflist(j))=Fglob(curr_doflist(j)) + Fe(j);
    end
endNodesLocList=[endNodesLocList,n_info(e_info(i,1),1),n_info(e_info(i,2),1)];
  %< used for plotting only
end
xExact=L.*[1:100]./100;
uExact=u(xExact); %<- exact solution for the displacement</pre>
du=symfun(diff(u(x),x),x);
sExact=E*du(xExact);
```

```
constlin=find(n_info(:,2));
Kglob(constlin,:)=[];
Kglob(:,constlin)=[];
Fglob(P_loaded_Node)=Fglob(P_loaded_Node)+P;
Fqlob(constlin,:)=[];
ulin=Kglob\Fglob; %<- solving the system of equations
uFE_soln(setdiff(1:end,constlin),:)=ulin;
eFE soln=uFE soln./L elem;
for ijk=1:numelem;
    jkl=ijk+1;
Stress_FE(ijk,:)=abs(reshape(KeLinear1DRoddivA(ijk,:,:),[2
 2])*(uFE_soln(jkl-1:jkl)-uFE_soln(jkl-1)));
end
Stress_FE=reshape(Stress_FE',[numelem*2,1]);
if flag==1;
figure;
subplot(2,1,1)
hold on;
plot(xExact, uExact, 'k');
plot(n_info(:,1),uFE_soln,['-.or']);
leg(:,end+1)={string(size(e_info,1))+' Elements'};
xlabel('X Position')
ylabel('Displacement');
subplot(2,1,2)
hold on;
plot(xExact,sExact,'k');
plot(endNodesLocList,Stress FE,['-.or']);
xlabel('X Position')
ylabel('Stress');
flag=0;
else
subplot(2,1,1)
hold on;
plot(n_info(:,1),uFE_soln,['-.or']);
leg(:,end+1)={string(size(e_info,1))+' Elements'};
subplot(2,1,2)
hold on;
plot(endNodesLocList,Stress_FE,['-.or']);
title('20 Elements')
subplot(2,1,1)
legend(leg)
subplot(2,1,2)
legend(leg)
```

$$u(x) =$$

$$-(2^{(1/2)*}atan((2^{(1/2)*}x*1i)/48)*3i)/100$$



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