

"Turbo HW5"  
 "Zhaoyi Jiang (.1364)"  
 "Problem 1"

"Given"

$$u = 250 \text{ [m/s]}$$

$$cz = 0.6 * u$$

$$R = 0.65$$

$$\alpha_2 = 55 \text{ [degree]}$$

"Normal stage"

$$\phi = cz/u$$

$$R = 1 - 0.5 * \phi * (\tan(\alpha_2) + \tan(\alpha_1))$$

$$\tan(\alpha_2) = (1 - R + \phi/2) / \phi$$

"Velocity triangles"

$$\tan(\beta_1) = -(R + \phi/2) / \phi$$

$$\tan(\beta_2) = -(R - \phi/2) / \phi$$

$$w_1 = cz / \cos(\beta_1)$$

$$w_2 = cz / \cos(\beta_2)$$

$$c_1 = cz / \cos(\alpha_1)$$

$$c_2 = cz / \cos(\alpha_2)$$

"Work"

$$W = u * (w_2 * \sin(\beta_2) - w_1 * \sin(\beta_1)) * \text{convert}(j, kJ)$$

SOLUTION

Unit Settings: SI C kPa kJ mass deg

$$\alpha_1 = -14.65 \text{ [degree]}$$

$$\beta_1 = -62.59 \text{ [degree]}$$

$$c_1 = 155 \text{ [m/s]}$$

$$cz = 150 \text{ [m/s]}$$

$$\psi = 1.014$$

$$u = 250 \text{ [m/s]}$$

$$w_1 = 325.8 \text{ [m/s]}$$

$$\alpha_2 = 55 \text{ [Degree]}$$

$$\beta_2 = -13.42 \text{ [degree]}$$

$$c_2 = 261.5 \text{ [m/s]}$$

$$\phi = 0.6$$

$$R = 0.65$$

$$W = 63.36 \text{ [kJ/kg]}$$

$$w_2 = 154.2 \text{ [m/s]}$$

No unit problems were detected.