PSTAT131 Final Project

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Introduction

This research question is which factor has positive or negative impacts to housing price and which prediction model will show future the housing prices based on the historical dataset appropriately? This is important for regional economic analysis to predict the future values of housings and real estates. We know the price is based on the size of the house, number of bathrooms and bedrooms, how much the house is closed to transportations, location and etc, but we need to be more specific during the analysis.

Data

This dataset contains records of apartments for sale and for rent in the city of São Paulo, Brazil. The dataset consists of 16 different variables (5 numeric variables, 6 logistic variables, 5 categorial variables) and about 13,000 records of apartment sales and rents advertised in April, 2019 from multiple websites.

Data Structure:

Price: Final price advertised (R\$ Brazilian Real)

Condo: Condominium expenses (unknown values are marked as zero)

Size: The property size in Square Meters m² (private areas only)

Rooms: Number of bedrooms

Toilets: Number of toilets (all toilets)

Suites: Number of bedrooms with a private bathroom (en suite)

Parking: Number of parking spots

Elevator: Binary value: 1 if there is elevator in the building, 0 otherwise

Furnished: Binary value: 1 if the property is funished, 0 otherwise

Swimming Pool: Binary value: 1 if the property has swimming pool, 0 otherwise

New: Binary value: 1 if the property is very recent, 0 otherwise

District: The neighborhood and city where the property is located.

Negotiation Type: Sale or Rent

Property Type: The property type

Latitude: Geographic location Longitude: Geographic location

References

https://www.kaggle.com/argonalyst/sao-paulo-real-estate-sale-rent-april-2019

Methods

Analysis Plan

- Data processing, filtering, clustering if necessary.
- Summary and plots(Scatter plot, boxplot, ...)
- 1. Logistic Regression
- 2. Decision Tree
- 3. Random Forest
- 4. Model Decision and Conclusion

Warning: package 'knitr' was built under R version 3.6.2

Data processing and filtering

```
#read data from Excel file.
saodata <- read.csv("C:/Users/Inwoong/Downloads/sao-paulo-properties-april-2019.csv")
#overview
dim(saodata)</pre>
```

[1] 13640 16

summary(saodata)

```
##
        Price
                            Condo
                                              Size
                                                              Rooms
##
                  480
                                :
                                                : 30.0
                                                         Min.
                                                                : 1.00
    Min.
                        Min.
                                        Min.
    1st Qu.:
                 1859
                        1st Qu.: 290
                                        1st Qu.: 50.0
                                                          1st Qu.: 2.00
##
##
    Median:
                 8100
                        Median: 500
                                        Median: 65.0
                                                         Median: 2.00
              287738
                                : 690
                                                : 84.4
                                                                 : 2.31
    Mean
            :
                        Mean
                                        Mean
                                                         Mean
              360000
                                                          3rd Qu.: 3.00
    3rd Qu.:
                        3rd Qu.: 835
                                        3rd Qu.: 94.0
##
##
    Max.
            :10000000
                        Max.
                                :9500
                                        Max.
                                                :880.0
                                                         Max.
                                                                 :10.00
##
##
       Toilets
                        Suites
                                        Parking
                                                        Elevator
                                                                        Furnished
##
    Min.
           :1.00
                    Min.
                            :0.000
                                     Min.
                                             :0.00
                                                     Min.
                                                             :0.000
                                                                      Min.
                                                                              :0.000
##
    1st Qu.:2.00
                    1st Qu.:1.000
                                     1st Qu.:1.00
                                                     1st Qu.:0.000
                                                                      1st Qu.:0.000
##
   Median:2.00
                    Median :1.000
                                     Median:1.00
                                                     Median : 0.000
                                                                      Median : 0.000
##
    Mean
           :2.07
                    Mean
                            :0.981
                                     Mean
                                             :1.39
                                                     Mean
                                                             :0.354
                                                                      Mean
                                                                              :0.147
                    3rd Qu.:1.000
    3rd Qu.:2.00
                                     3rd Qu.:2.00
##
                                                     3rd Qu.:1.000
                                                                      3rd Qu.:0.000
##
    Max.
            :8.00
                            :6.000
                                     Max.
                                             :9.00
                                                             :1.000
                    Max.
                                                     Max.
                                                                      Max.
                                                                              :1.000
##
##
                                                          District
    Swimming.Pool
                          New
##
    Min.
            :0.000
                             :0.0000
                                       Moema/S o Paulo
                                                               293
                     Min.
                                       Mooca/S o Paulo
##
    1st Qu.:0.000
                     1st Qu.:0.0000
                                                               288
    Median :1.000
                     Median :0.0000
                                       Br s/S o Paulo
                                       Bela Vista/S o Paulo:
##
    Mean
            :0.512
                     Mean
                             :0.0156
##
    3rd Qu.:1.000
                     3rd Qu.:0.0000
                                       Brooklin/S o Paulo :
                                                               250
##
    Max.
           :1.000
                     Max.
                             :1.0000
                                       Pinheiros/S o Paulo: 249
##
                                        (Other)
                                                              :12055
##
    Negotiation.Type
                        Property.Type
                                                            Longitude
                                             Latitude
```

```
## rent:7228
                    apartment: 13640
                                     Min. :-46.7
                                                     Min.
                                                            :-58.4
##
   sale:6412
                                     1st Qu.:-23.6
                                                    1st Qu.:-46.7
                                     Median :-23.6
##
                                                    Median :-46.6
##
                                           :-22.1
                                     Mean
                                                     Mean
                                                           :-43.6
##
                                     3rd Qu.:-23.5
                                                     3rd Qu.:-46.6
##
                                     Max. : 0.0
                                                     Max. : 0.0
##
str(saodata)
                  13640 obs. of 16 variables:
## 'data.frame':
## $ Price
                    : int 930 1000 1000 1000 1300 1170 1000 900 1000 1000 ...
## $ Condo
                            220 148 100 200 410 0 180 150 0 0 ...
## $ Size
                    : int 47 45 48 48 55 50 52 40 65 100 ...
                            2 2 2 2 2 2 1 2 2 2 ...
## $ Rooms
                    : int
## $ Toilets
                    : int
                            2 2 2 2 2 2 2 2 2 2 . . .
## $ Suites
                     : int 1 1 1 1 1 1 1 1 1 ...
                    : int 1 1 1 1 1 1 1 1 1 1 ...
## $ Parking
## $ Elevator
                    : int 0000101000...
                    : int 00000000000...
## $ Furnished
## $ Swimming.Pool : int 0 0 0 0 0 0 0 0 0 ...
## $ New
                    : int 0000000000...
                    : Factor w/ 96 levels "Alto de Pinheiros/S o Paulo",..: 4 4 4 4 4 4 4 4 4 ...
## $ District
## $ Negotiation.Type: Factor w/ 2 levels "rent", "sale": 1 1 1 1 1 1 1 1 1 1 ...
## $ Property.Type : Factor w/ 1 level "apartment": 1 1 1 1 1 1 1 1 1 1 ...
## $ Latitude
                   : num -23.5 -23.6 -23.5 -23.5 -23.5 ...
## $ Longitude
                    : num -46.5 -46.5 -46.5 -46.5 ...
#check missingness in dataset
apply(is.na(saodata), 2, sum)
##
             Price
                              Condo
                                               Size
                                                               Rooms
##
                                                  0
##
           Toilets
                             Suites
                                            Parking
                                                           Elevator
##
                 0
                                                  0
##
         Furnished
                      Swimming.Pool
                                                            District
                                                New
                                                  Λ
##
                 0
                      Property.Type
## Negotiation.Type
                                           Latitude
                                                           Longitude
                                                  0
##
                 0
# Select parameters in the dataset.
## New, Property. Type is out of the model because they have only one type.
## District is related to the location(Latitude and Longitude). I therefore remove this variable from m
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
```

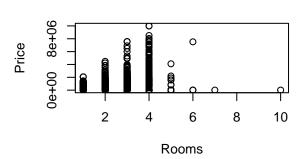
```
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
saodata <- dplyr::select(saodata, -c(New, Property.Type, District))</pre>
head(saodata)
    Price Condo Size Rooms Toilets Suites Parking Elevator Furnished
## 1
                   47
                          2
                                  2
       930
             220
                                          1
                                                  1
## 2 1000
                                  2
                                                           0
             148
                   45
                          2
                                          1
                                                  1
                                                                     0
## 3 1000
             100
                   48
                          2
                                  2
                                          1
                                                  1
                                                           0
                                                                     0
                          2
                                  2
                                                           0
                                                                     0
## 4 1000
             200
                   48
                                          1
                                                  1
                          2
                                  2
## 5 1300
             410
                   55
                                          1
                                                  1
                                                           1
                                                                     0
## 6 1170
               0
                   50
                          2
                                  2
                                          1
                                                           0
                                                                     0
                                                  1
     Swimming.Pool Negotiation.Type Latitude Longitude
                               rent -23.5431 -46.4795
## 1
                 0
## 2
                 0
                               rent -23.5502 -46.4807
## 3
                 0
                               rent -23.5428 -46.4857
## 4
                 0
                               rent -23.5472 -46.4830
## 5
                 0
                               rent -23.5250 -46.4824
## 6
                 0
                               rent -23.5488 -46.4772
#plots(Price vs other parameters)
library(scatterplot3d)
par(mfrow=c(2,2))
plot(saodata$Condo, saodata$Price, main = "Condo vs Price", xlab = "Condo", ylab = "Price")
plot(saodata$Size, saodata$Price, main = "Size vs Price", xlab = "Size", ylab = "Price")
plot(saodata$Rooms, saodata$Price, main = "Rooms vs Price", xlab = "Rooms", ylab = "Price")
plot(saodata$Toilets, saodata$Price, main = "Toilets vs Price", xlab = "Toilets", ylab = "Price")
```

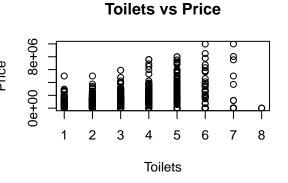
90+98 - 0 2000 4000 6000 8000 Condo

Condo vs Price

Rooms vs Price

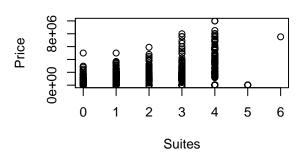




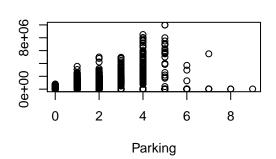


```
par(mfrow=c(2,2))
plot(saodata$Suites, saodata$Price, main = "Suites vs Price", xlab = "Suites", ylab = "Price")
plot(saodata$Parking, saodata$Price, main = "Parking vs Price", xlab = "Parking", ylab = "Price")
plot(saodata$Latitude, saodata$Price, main = "Latitude vs Price", xlab = "Latitude", ylab = "Price")
plot(saodata$Longitude, saodata$Price, main = "Longitude vs Price", xlab = "Longitude", ylab = "Price")
```

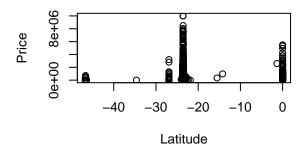
Suites vs Price



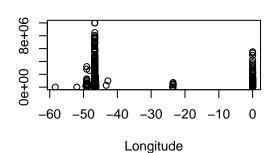
Parking vs Price



Latitude vs Price



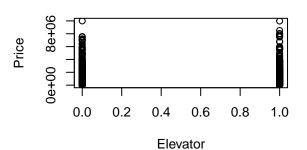
Longitude vs Price



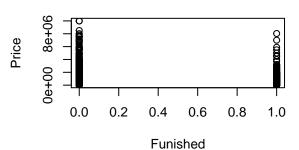
par(mfrow=c(2,2))
plot(saodata\$Elevator, saodata\$Price, main = "Elevator vs Price", xlab = "Elevator", ylab = "Price")
plot(saodata\$Furnished, saodata\$Price, main = "Funished vs Price", xlab = "Funished", ylab = "Price")
plot(saodata\$Swimming.Pool, saodata\$Price, main = "Swimming Pool vs Price", xlab = "Swining Pool", ylab
plot(saodata\$Negotiation.Type, saodata\$Price, main = "Negotiation Type vs Price", xlab = "Negotiation Type")

Price

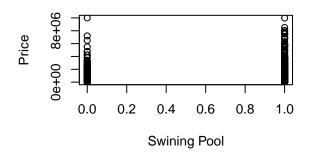
Elevator vs Price



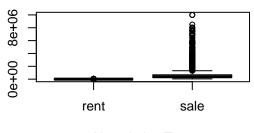
Funished vs Price



Swimming Pool vs Price



Negotiation Type vs Price



Negotiation Type

```
# Split the data
set.seed(20200305)
train <- sample(1:dim(saodata)[1], dim(saodata)[1]*0.75, rep=FALSE)
test <- -train
training_data<- saodata[train, ]
testing_data= saodata[test, ]
dim(training_data)</pre>
```

[1] 10230 13

dim(testing_data)

[1] 3410 13

Logistic Regression

```
logistic_train <- training_data
logistic_test <- testing_data
#get the number of average price of all housing.
mean_log <- mean(logistic_train$Price)
#If the price is over the average, Price is 1. If not, the price is 0.
logistic_train$Price <- ifelse(logistic_train$Price <= mean_log , 0, 1)
logistic_test$Price <- ifelse(logistic_test$Price <= mean_log , 0, 1)
#Build logistic model</pre>
```

```
#glm.fit <- glm(Price~., data=logistic_train, family=binomial)</pre>
glm.fit <- glm(Price~Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished+Swimming.Pool+Negotiat
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
summary(glm.fit)
##
## Call:
  glm(formula = Price ~ Condo + Size + Rooms + Toilets + Suites +
##
       Parking + Elevator + Furnished + Swimming.Pool + Negotiation.Type +
##
       Latitude + Longitude, family = binomial, data = logistic_train)
##
## Deviance Residuals:
##
      Min
               10 Median
                               30
                                      Max
                    0.000
  -3.608
            0.000
                            0.005
                                    2.983
##
## Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                        -1.61e+04
                                    9.11e+05
                                                -0.02
                                                        0.9859
## Condo
                                                11.47
                         2.57e-03
                                    2.24e-04
                                                       < 2e-16 ***
## Size
                         1.49e-01
                                    6.51e-03
                                               22.86
                                                      < 2e-16 ***
## Rooms
                        -1.20e+00
                                    1.14e-01
                                              -10.46 < 2e-16 ***
## Toilets
                         7.60e-01
                                    3.94e-01
                                                 1.93
                                                        0.0537 .
## Suites
                        -9.51e-01
                                    3.89e-01
                                                -2.45
                                                        0.0144 *
## Parking
                         9.02e-01
                                    1.78e-01
                                                5.08 3.7e-07 ***
## Elevator
                         1.95e-01
                                    1.03e-01
                                                1.90
                                                        0.0572 .
                                                        0.0065 **
## Furnished
                                                2.72
                         4.50e-01
                                    1.65e-01
## Swimming.Pool
                         1.50e+00
                                    9.75e-02
                                                15.40
                                                       < 2e-16 ***
## Negotiation.Typesale 1.61e+04
                                    9.11e+05
                                                0.02
                                                        0.9859
## Latitude
                        -3.08e-02
                                    4.36e-02
                                                -0.71
                                                        0.4798
                         5.62e-03
## Longitude
                                    2.22e-02
                                                0.25
                                                        0.7997
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 12724.9
                               on 10229
                                         degrees of freedom
## Residual deviance: 2929.8
                               on 10217
                                         degrees of freedom
## AIC: 2956
##
## Number of Fisher Scoring iterations: 14
```

Interpretation of the logistic regression model

The variable Condo has a coefficient 2.569e-03. For every one unit change in Condo, the log odds of getting higher price than average increases by 2.569e-03, holding other variables fixed.

The variable Size has a coefficient 1.487e-01. For a one unit increase in Size, the log odds of getting higher price than average increases by 1.487e-01, holding other variables fixed.

The variable Rooms has a coefficient -1.195e+00. For a one unit increase in Rooms, the log odds of getting higher price than average decreases by 1.195e+00, holding other variables fixed.

The variable Toilets has a coefficient 7.601e-01. For a one unit increase in Toilets, the log odds of getting higher price than average increases by 7.601e-01, holding other variables fixed.

The variable Suites has a coefficient -9.512e-01. For a one unit increase in Suites, the log odds of getting higher price than average decreases by 9.512e-01, holding other variables fixed.

The variable Parking has a coefficient 9.024e-01. For a one unit increase in Parking, the log odds of getting higher price than average increases by 9.024e-01, holding other variables fixed.

The variable Furnished has a coefficient 4.504e-01, meaning that the indicator function of 1 has a regression coefficient 4.504e-01. That being said, furnished room changes the log odds of getting higher price than average to increase by 4.504e-01.

The variable Swimming.Pool has a coefficient 1.502e+00, meaning that the indicator function of 1 has a regression coefficient 1.502e+00. That being said, existence of a swimming pool changes the log odds of getting higher price than average to increase by 1.502e+00.

The variable Negotiation. Type has a coefficient 1.610e+04, meaning that the indicator function of Sale has a regression coefficient 1.610e+04. That being said, Sale type verses Rent changes the log odds of getting higher price than average to increase by 1.610e+04.

The variable Latitude has a coefficient -3.079e-02. For a one unit increase in Latitude, the log odds of getting higher price than average decreases by 3.079e-02, holding other variables fixed.

The variable Longitude has a coefficient 5.625e-03. For a one unit increase in Longitude, the log odds of getting higher price than average increases by 5.625e-03, holding other variables fixed.

```
# Model selection
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
full.model <- glm(Price~Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished, data=logistic_train
summary(full.model)
##
## Call:
## glm(formula = Price ~ Condo + Size + Rooms + Toilets + Suites +
##
       Parking + Elevator + Furnished, family = binomial, data = logistic_train)
##
## Deviance Residuals:
##
               10
                  Median
                               3Q
                                       Max
## -3.055 -0.874
                   -0.735
                                     2.584
                            1.261
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -2.37e+00
                           8.99e-02 -26.37
                                             < 2e-16 ***
               -5.10e-04
                           4.86e-05
                                     -10.50
                                              < 2e-16 ***
## Condo
## Size
                3.83e-03
                           7.64e-04
                                       5.01 5.3e-07 ***
```

10.43 < 2e-16 *** 5.14 2.8e-07 ***

Rooms

Toilets

4.21e-01

2.83e-01

4.03e-02

5.51e-02

```
-3.67e-01 6.40e-02 -5.73 1.0e-08 ***
## Suites
              1.26e-01 4.45e-02 2.83 0.0047 **
## Parking
## Elevator
              5.62e-01 4.63e-02 12.16 < 2e-16 ***
## Furnished -1.78e-02 6.40e-02 -0.28 0.7808
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 12725 on 10229 degrees of freedom
## Residual deviance: 12127 on 10221 degrees of freedom
## AIC: 12145
##
## Number of Fisher Scoring iterations: 4
When the logistic regression model has all preditors, the model has the smallest AIC, which means the full
model is the most significant model.
phat <- predict(glm.fit, type = 'response')</pre>
yhat <- phat > 0.5
#Confusion matrix table
ct <- table(obs=logistic_train$Price,pred=yhat)</pre>
##
     pred
## obs FALSE TRUE
##
    0 6695 327
##
       329 2879
\#TPR
tpr \leftarrow ct[2,2]/(ct[2,1]+ct[2,2])
tpr
## [1] 0.897444
#FPR
fpr \leftarrow ct[1,2]/(ct[1,1]+ct[1,2])
fpr
## [1] 0.0465679
#Misclassification rate
mean(yhat != logistic_train$Price)
## [1] 0.0641251
# install.packages("ROCR")
library(ROCR)
```

Warning: package 'ROCR' was built under R version 3.6.3

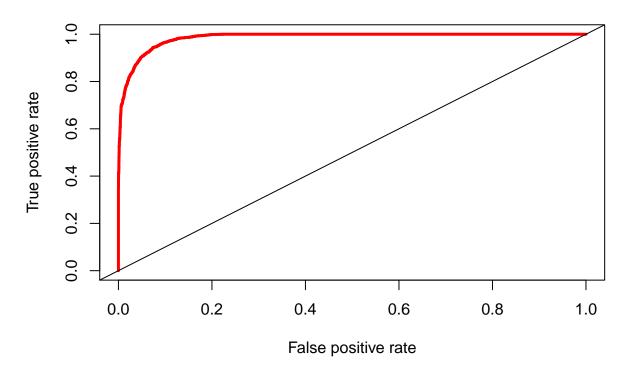
```
## Loading required package: gplots
## Warning: package 'gplots' was built under R version 3.6.3

##
## Attaching package: 'gplots'

## The following object is masked from 'package:stats':
##
## lowess

# First arument is the logistic_train, second is true labels
pred = prediction(phat, logistic_train$Price)
perf = performance(pred, measure = "tpr", x.measure = "fpr")
# plot ROC curve
plot(perf, col=2, lwd=3, main="ROC curve")
abline(0,1)
```

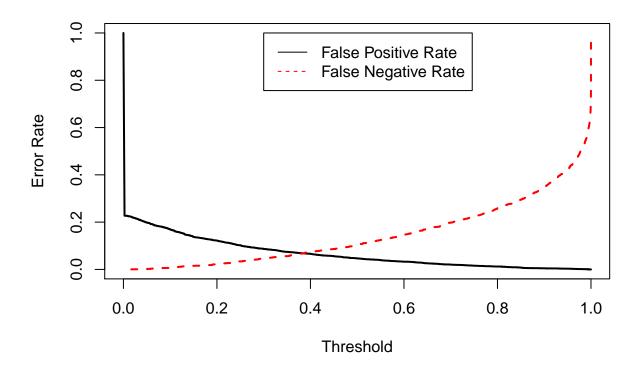
ROC curve



```
# Calculate AUC
auc = performance(pred, "auc")@y.values
auc
```

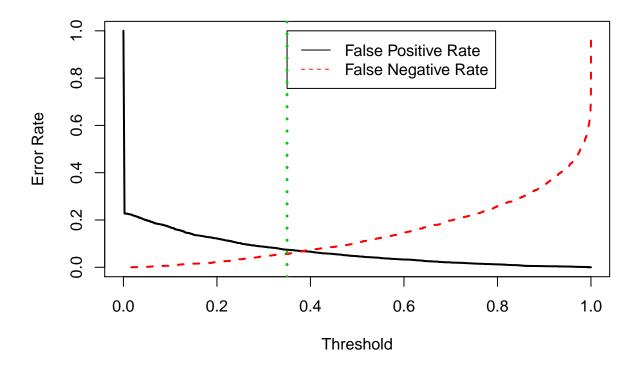
```
## [[1]]
## [1] 0.985185
```

```
#Obtain FPR and FNR from performance() output:
# FPR
fpr = performance(pred, "fpr")@y.values[[1]]
cutoff = performance(pred, "fpr")@x.values[[1]]
# FNR
fnr = performance(pred, "fnr")@y.values[[1]]
# Plot FPR and FNR versus threshold values using matplot():
# Plot
matplot(cutoff, cbind(fpr,fnr), type="l",lwd=2, xlab="Threshold",ylab="Error Rate")
# Add legend to the plot
legend(0.3, 1, legend=c("False Positive Rate","False Negative Rate"),
col=c(1,2), lty=c(1,2))
```



```
# Calculate the euclidean distance between (FPR,FNR) and (0,0)
rate = as.data.frame(cbind(Cutoff=cutoff, FPR=fpr, FNR=fnr))
rate$distance = sqrt((rate[,2])^2+(rate[,3])^2)
# Select the probability threshold with the smallest euclidean distance
index = which.min(rate$distance)
best = rate$Cutoff[index]
best
```

```
# Plot
matplot(cutoff, cbind(fpr,fnr), type="l",lwd=2, xlab="Threshold",ylab="Error Rate")
# Add legend to the plot
legend(0.35, 1, legend=c("False Positive Rate","False Negative Rate"),
col=c(1,2), lty=c(1,2))
# Add the best value
abline(v=best, col=3, lty=3, lwd=3)
```



#Therefore, our best cutoff value is 0.34998. That means, probabilities for higher price is less than 0

Decision Tree

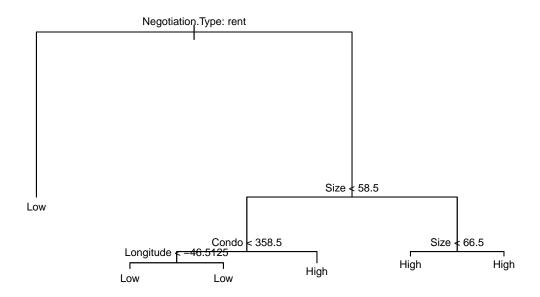
```
library(tree)
```

Warning: package 'tree' was built under R version 3.6.2

```
logistic_train_class <- training_data
logistic_test_class <- testing_data
logistic_train_class$Price <- as.factor(ifelse(logistic_train_class$Price <= mean_log , "Low", "High"))
logistic_test_class$Price <- as.factor(ifelse(logistic_test_class$Price <= mean_log , "Low", "High"))
#classification tree with class
fit <- tree(Price ~ Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished+Swimming.Pool+Negotiations
summary(fit)</pre>
```

```
##
## Classification tree:
## tree(formula = Price ~ Condo + Size + Rooms + Toilets + Suites +
## Parking + Elevator + Furnished + Swimming.Pool + Negotiation.Type +
## Latitude + Longitude, data = logistic_train_class)
## Variables actually used in tree construction:
## [1] "Negotiation.Type" "Size" "Condo" "Longitude"
## Number of terminal nodes: 6
## Residual mean deviance: 0.3 = 3070 / 10200
## Misclassification error rate: 0.0656 = 671 / 10230

plot(fit)
text(fit, pretty = 0, cex = .7)
```

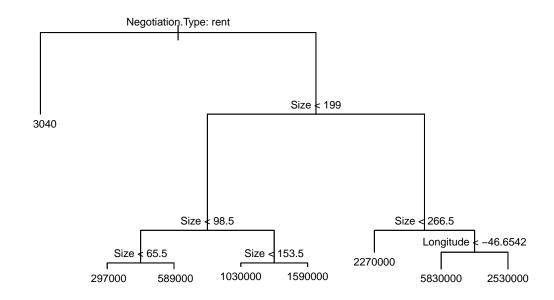


```
#classification tree without class
fit2<- tree(Price ~ Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished+Swimming.Pool+Negotiation
summary(fit2)</pre>
```

```
##
## Regression tree:
## tree(formula = Price ~ Condo + Size + Rooms + Toilets + Suites +
## Parking + Elevator + Furnished + Swimming.Pool + Negotiation.Type +
## Latitude + Longitude, data = training_data)
## Variables actually used in tree construction:
## [1] "Negotiation.Type" "Size" "Longitude"
```

```
## Number of terminal nodes: 8
## Residual mean deviance: 5.79e+10 = 5.92e+14 / 10200
## Distribution of residuals:
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -3720000 -18000 -1240 0 2960 4170000

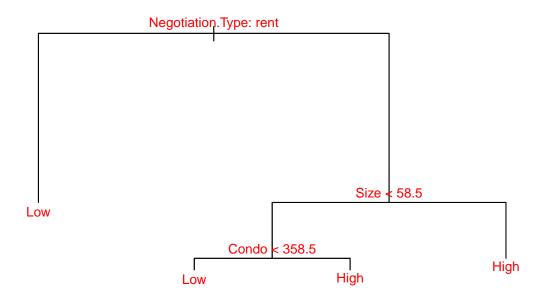
plot(fit2)
text(fit2, pretty = 0, cex = .7)
```



```
# Test error rate (Classification Error)
1-sum(diag(error))/sum(error)
## [1] 0.0683284
yhat.testset2 <- predict(fit2, testing_data)</pre>
y.testset2 <- testing_data$Price</pre>
error <- table(yhat.testset2, y.testset2)</pre>
# Test accuracy rate
sum(diag(error))/sum(error)
## [1] 0.000293255
# Test error rate (Classification Error)
1-sum(diag(error))/sum(error)
## [1] 0.999707
Since the test error rate of the classification tree model with class is much lower than classification tree model
without class, the classification model with class is significant.
Pruned Tree
prune <- prune.tree(fit, k = 0:50, method = "misclass")</pre>
# Best size
best.prune <- prune$size[which.min(prune$dev)]</pre>
best.prune
## [1] 4
#From the output, the 'best' size is 4 since this number of terminal nodes corresponds to the smallest.
set.seed(3)
cv <- cv.tree(fit, FUN=prune.misclass, K=50)</pre>
# Print out cv
## $size
## [1] 6 4 3 2 1
##
## $dev
## [1] 725 725 879 1596 3208
##
## $k
## [1] -Inf
                0 204 720 1613
##
## $method
## [1] "misclass"
##
## attr(,"class")
## [1] "prune"
                         "tree.sequence"
```

```
# Prune tree
pt.prune <- prune.misclass (fit, best=best.prune)
# Plot pruned tree
plot(pt.prune)
text(pt.prune, pretty=0, col = "red", cex = .8)
title("Pruned tree of size 4")</pre>
```

Pruned tree of size 4



```
# Predict on test set
pred.pt.prune <- predict(pt.prune, logistic_test_class, type="class")
# Obtain confusion matrix
err.pt.prune <- table(pred.pt.prune, y.testset)
err.pt.prune

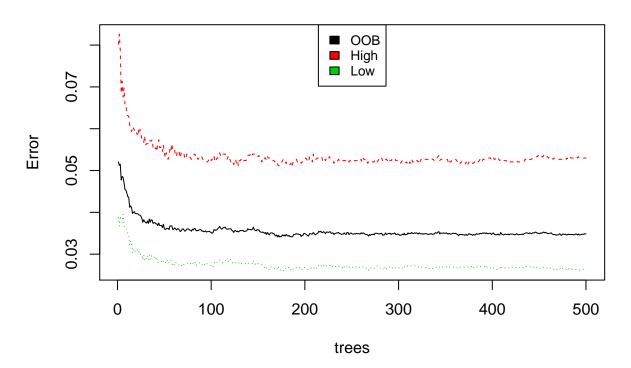
## y.testset
## pred.pt.prune High Low
## High 1010 154
## Low 79 2167

# Test accuracy rate
sum(diag(err.pt.prune))/sum(err.pt.prune)</pre>
```

[1] 0.931672

```
# Test error rate (Classification Error)
1-sum(diag(err.pt.prune))/sum(err.pt.prune)
## [1] 0.0683284
Even if I applied pruned tree to get better model, the test error rate remains same.
Bagging Tree and Random Forest model
library(dplyr)
library(randomForest)
## Warning: package 'randomForest' was built under R version 3.6.2
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
       combine
library(tree)
#Bagging Tree
bag <- randomForest(Price~Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished+Swimming.Pool+Nego
bag
##
## Call:
                                                                          Suites + Parking + Elevator + 1
## randomForest(formula = Price ~ Condo + Size + Rooms + Toilets +
##
                  Type of random forest: classification
                        Number of trees: 500
##
## No. of variables tried at each split: 12
##
##
           OOB estimate of error rate: 3.48%
## Confusion matrix:
       High Low class.error
## High 3038 170 0.0529925
        186 6836 0.0264882
## Low
plot(bag)
legend("top", colnames(bag$err.rate),col=1:4,cex=0.8,fill=1:4)
```

bag



```
#confusion matrix
yhat.bag = predict(bag, newdata = logistic_test_class)
bag.err = table(pred = yhat.bag, truth = logistic_test_class$Price)
test.bag.err = 1 - sum(diag(bag.err))/sum(bag.err)
test.bag.err
```

[1] 0.0316716

High 3044 164

183 6839

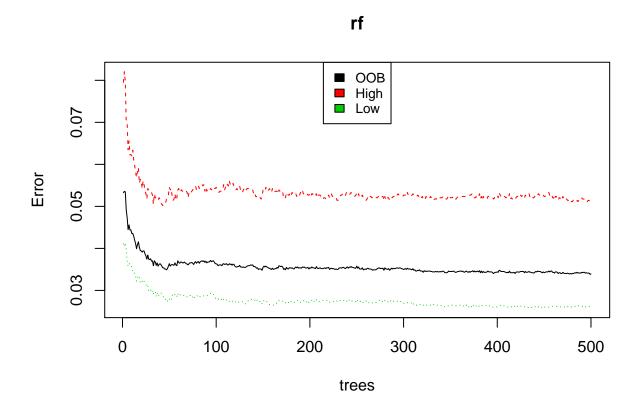
Low

The test set error rate associated with the bagged classification tree is 0.0316

0.0511222 0.0260610

```
#Random Forest
rf <- randomForest(Price~Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished+Swimming.Pool+Negot
##
## Call:
    randomForest(formula = Price ~ Condo + Size + Rooms + Toilets +
##
                                                                         Suites + Parking + Elevator +
##
                  Type of random forest: classification
                        Number of trees: 500
## No. of variables tried at each split: 12
##
           OOB estimate of error rate: 3.39%
##
## Confusion matrix:
##
        High Low class.error
```

```
plot(rf)
legend("top", colnames(rf$err.rate),col=1:4,cex=0.8,fill=1:4)
```



```
yhat.rf = predict (rf, newdata = logistic_test_class)
# Confusion matrix
rf.err = table(pred = yhat.rf, truth = logistic_test_class$Price)
test.rf.err = 1 - sum(diag(rf.err))/sum(rf.err)
# Test error rate
test.rf.err
```

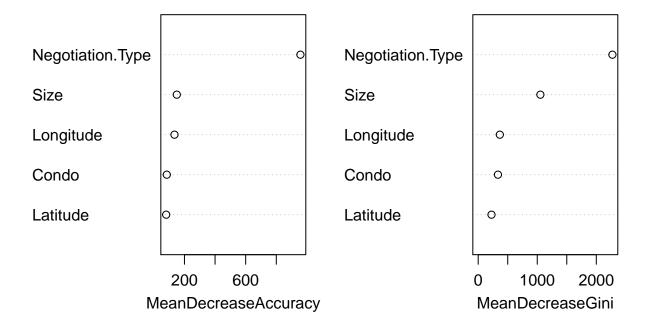
importance(rf)

```
##
                                    Low MeanDecreaseAccuracy MeanDecreaseGini
                         High
## Condo
                      5.98763 81.77486
                                                      84.5799
                                                                      334.4486
## Size
                     73.40752 119.29500
                                                     150.0157
                                                                      1052.8905
## Rooms
                     26.78820 22.38165
                                                      35.5415
                                                                       29.0150
## Toilets
                      5.99065
                                9.61840
                                                      11.2781
                                                                       11.7216
## Suites
                     15.28685
                                7.60921
                                                      16.8849
                                                                       10.8644
## Parking
                     11.90394 13.10237
                                                      18.3228
                                                                       15.8911
## Elevator
                      7.30762 18.94925
                                                      20.4841
                                                                       16.0372
## Furnished
                      7.21419 21.77851
                                                      22.0330
                                                                       14.9544
## Swimming.Pool
                     34.62240 40.71451
                                                      50.8982
                                                                       53.7812
```

```
## Negotiation.Type 812.10487 764.64823 957.7058 2273.0749
## Latitude 59.90652 52.10808 80.6961 225.3113
## Longitude 73.54912 115.19641 134.8107 366.5115

varImpPlot(rf, sort=T, main="Variable Importance for rf", n.var=5)
```

Variable Importance for rf



The results indicate that across all of the trees considered in the random forest, the Negotiation. Type is by far the most important variable in terms of Model Accuracy and Size is the secondary most important variable.

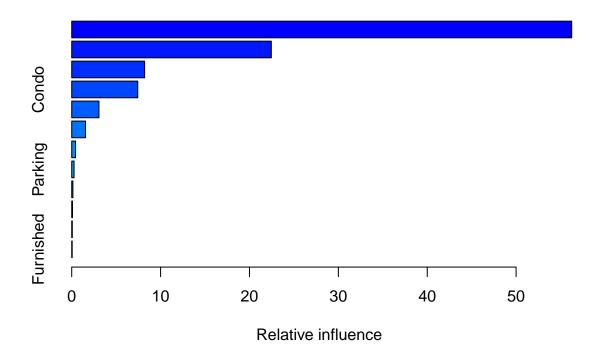
Boosting

```
library(gbm)

## Warning: package 'gbm' was built under R version 3.6.2

## Loaded gbm 2.1.5

set.seed(1)
boost <- gbm(ifelse(Price=="High",1,0)~Condo+Size+Rooms+Toilets+Suites+Parking+Elevator+Furnished+Swimm summary(boost)</pre>
```



```
##
                                         rel.inf
                                  var
## Negotiation.Type Negotiation.Type 56.2521617
## Size
                                 Size 22.4572285
## Longitude
                           Longitude
                                      8.2025809
## Condo
                                Condo
                                       7.4298397
## Latitude
                             Latitude 3.0638884
## Swimming.Pool
                       Swimming.Pool
                                      1.5546862
## Rooms
                                Rooms 0.4318611
## Parking
                              Parking 0.2658957
## Toilets
                              Toilets 0.1332400
## Elevator
                             Elevator 0.0900062
## Suites
                               Suites 0.0666510
## Furnished
                            Furnished 0.0519606
yhat.boost <- predict(boost, newdata = logistic_test_class, n.trees=500)</pre>
# Confusion matrix
boost.err <- table(pred = yhat.boost, truth = logistic_test_class$Price)</pre>
test.boost.err <-1-sum(diag(boost.err))/sum(boost.err)</pre>
test.boost.err
```

Testing error seems not okay with boosting model because it is over 0.9.

Conclusion

According to all of tests, Randomforest model has the lowest test error rate, which means the most significant model. All predictors excluding New, District, Property. Type are included because the model has the lowest AIC when it has all of the predictors. This study has some limitation because the dataset has information of very narrow area. It might have different results if the dataset includes information from other areas in Brazil. Also, this study is not effectively explained due to lack of other predictors such as existence of transfortation, number of criminal cases near the area, etc. This study will result in having different conclusion if the dataset is expanded.