Fitting Models to Data in Ecology and Evolution

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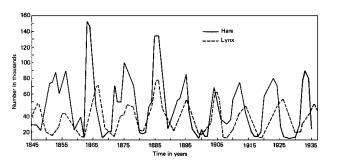
MECHANISTIC VS. PHENOMENOLOGICAL MODELS

What does "modelling data" mean to you?

MECHANISTIC VS. PHENOMENOLOGICAL MODELS

- Mechanistic models aim to explain the PROCESSES or MECHANISMS underlying PATTERNS or PHENOMENA in empirical data
 - These models have a THEORETICAL BASIS
- Empirical/Phenomenological models establish the existence of STATISTICALLY SIGNIFICANT, NON-RANDOM PATTERNS or PHENOMENA in empirical data
 - They make no assumptions about the processes or mechanisms that generate the patterns
 - That is, these models lack a THEORETICAL BASIS

MECHANISTIC VS. PHENOMENOLOGICAL MODEL FITTING



source: https://www.cds.caltech.edu/~murray/amwiki/images/8/8f/LHgraph.gif

- Mechanistic model: The Lynx-Hare Cycle is driven by density-dependent population growth in hares
- Phenomenological model: The Lynx and Hare Cycles have a significant asynchrony (period shift) of x years

MECHANISTIC VS. PHENOMENOLOGICAL MODEL FITTING

- It's not really one vs. the other, Both types of models play a role in science (and Biology)
- Phenomenological model-fitting reveals patterns in data that generate HYPOTHESES
 - These can be tested using further model fitting
 - Example: Whether climatic temperature affects the Lynx-Hare cycle (using Generalized Linear Model-fitting)
- Mechanistic model-fitting tries to validate a mechanistic model that can explain the observed phenomenological pattern and generate MORE ACCURATE, MECHANISTIC HYPOTHESES
 - Example: How climatic temperature drives the Lynx-Hare cycle
- Ultimately, successful, EMPIRICALLY-GROUNDED mechanistic models are the best path towards a THEORY in any scientific discipline (including ecology and evolution)

MECHANISTIC VS. PHENOMENOLOGICAL MODEL FITTING

Individuals

Mechanisms ⇒
Metabolic rate,
Temperature response,
Growth rate



Interactions

Mechanisms ⇒
Consumer-resource
interactions, Competition,
Density dependence



Communities

Mechanisms ⇒
Trophic cascades,
Bottom-up & Top-down
regulation



MECHANISTIC MODELS IN ECOLOGY AND EVOLUTION?

- Do most ecological studies perform phenomenological or mechanistic modelling (or model-fitting)?
- The answer is mostly Phenomenological Why?
 - Partly because we are still establishing the existence of GENERAL PATTERNS/PHENOMENA,
 - ... and partly because we are (or are forced to be) interested in FORECASTING rather than EXPLAINING.
- So the big question is, can we FORECAST WITHOUT EXPLAINING?
 - For example, disease outbreaks: Do we really need to care about the underlying mechanisms if we can predict a future event using phenomenological modelling (e.g., Machine-learning of time series patterns)?

WHAT ARE MECHANISMS?

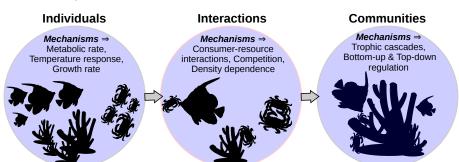
- Somewhat subjective!
- For example, the Ricker model can be thought of as mechanistic:

$$N_{t+1} = N_t e^{r\left(1 - \frac{N_t}{k}\right)}$$

- What is the mechanism? Density dependence through scramble competition (Brannstrom & Sumpter 2005)
- If the Ricker model and another model with contest competition were compared with data — some would call it mechanistic modelling because one is trying to get at the underlying mechanism, scramble or contest competition
- But is this REALLY mechanistic? What are r and k really?

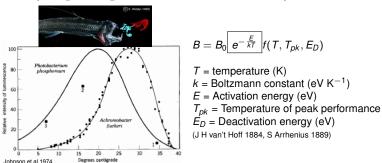
EXAMPLE OF A FUNDAMENTAL MECHANISM: METABOLIC RATE

 Proponents of Ecological Metabolic Theory (AKA "Metabolic Theory of Ecology") argue that we have not progressed far enough towards mechanistic modelling because metabolism has been ignored



EXAMPLE OF A FUNDAMENTAL MECHANISM: METABOLIC RATE

 The mechanistic basis of thermal performance curves (https://youtu.be/6n8fCuDwn74)



- Surely there is more to thermal responses?
- What about alternative models?

MODELLING, AND FITTING MODELS TO DATA: WHAT'S THE BIG IDEA?

- If possible, use biological knowledge to construct models
- See if the models "agree well" with data
- Whichever model "agrees best" is most likely to have the right mechanisms
- That's the one that's best for predictions (e.g. population cycles), estimating rates (e.g. population or individual growth rates), etc
- Don't use models you already know have the wrong mechanisms just because they are popular!
- Phenomenological/statistical models often perform better than mechanistic ones. Why? — because they have lest restrictive assumptions

MODELS: HOW TO BUILD THEM?

- It's an art, takes practice (Levins' paper on the strategy of model building in biology)
- Build models one mechanism at a time in biology, it means start at the right level of organization!
- Always consider an alternative that is more parsimonious, even if it is phenomenological!
- For example, the Boltzmann-Arrhenius model is a good first try describe and uncover mechanisms underlying individual level "traits" that are rates (e.g., fecundity or development rate)
- The next step would be to include species interactions with temperature dependence of individuals (or go in an evolutionary direction)

FITTING MODELS TO DATA

Multiple ways to do it:

- Least Squares methods
 - Linear
 - Non-linear
- Likelihood-based methods
 - Maximum Likelihood Estimation (MLE)
 - Bayesian
- Artificial intelligence and Machine learning
 - Focus in on maximizing ability to discover pattern and predict at the cost of mechanistic insights

METHODS YOU CAN USE

- Least squares: along with Linear Model fitting, Non-linear Least Squares (NLLS) fitting is a particularly versatile and powerful approach because many mechanisms in biology and inherently non-linear
- MLE/Bayesian methods: more robust if you are able to calculate the likelihood function analytically or numerically.
- Al/machine Learning: most versatile for large amounts of noisy data

SUMMARY: MODEL SELECTION IS THE KEY

- Ideally, several competing (meaningful, not just null) hypotheses (mathematical models) should be fitted to data and compared using statistical theory
- This is an advance over the traditional "null hypothesis" approach in Biology
- Necessary for developing the advancement of Biology from from an observational and axiomatic discipline to one with general theories.
- Necessary for understanding the mechanisms underlying biological patterns/phenomena

COMPARING AND SELECTING MODELS

 It's all about the "Likelihood" of a model: the set of parameter values of the model (θ) given outcomes (x), equals the probability of those observed outcomes given those parameter values, that is,

$$\mathcal{L}(\theta|\mathbf{x}) = P(\mathbf{x}|\theta)$$

- The easiest thing to do for you is to use information theory (including AIC and BIC) to compare models.
- Both AIC and BIC use the estimated (log-) likelihood of a model:
 - AIC: $-2 \ln[\mathcal{L}(\theta|x)] + 2p$
 - BIC (Schwartz criterion): $-2ln[\mathcal{L}(\theta|x)] + p\ln(n)$ (n = sample size, p = number of free parameters)
- The lower the AIC or BIC, the better.

AIC AND BIC

• In models fitted with least squares and normally-distributed errors, $\ln[\mathcal{L}(\theta|x)] = -\frac{n}{2}\ln\left(\frac{RSS}{n}\right)$

Thus

$$AIC = -2\ln[\mathcal{L}(\theta|x)] + 2p$$
$$= n + 2 + n\ln\left(\frac{2\pi}{n}\right) + n\ln(RSS) + 2p$$

And

$$BIC = -2ln[\mathcal{L}(\theta|x)] + p \ln(n)$$

$$= n + 2 + n \ln\left(\frac{2\pi}{n}\right) + n \ln(RSS) + p \ln(n)$$

 The small sample AIC can also be calculated similarly (see Johnson & Omland 2004)

COMPARING AND SELECTING MODELS

This is how you calculate AIC and BIC (using python syntax):

- residuals = Observations Predictions
- rss = sum(residuals ** 2)
- Then, AIC = n + 2 + n * log((2 * pi) / n) + n * log(rss) + 2 * p (note n and p!)
- And BIC = n + 2 + n * log((2 * pi) / n) + n * log(rss) + (log(n)) * (p + 1)
- For both AIC and BIC, If model A has AIC lower by 2-3 or more than model B, it's better — Differences of less than 2-3 don't really matter

Also note that:

 R² = 1 - (rss/tss), where tss is total sum of squares: tss = sum((Observations - mean(Predictions)) ** 2) (a useful measure of goodness of fit)

COMPARING AND SELECTING MODELS: MORE STUFF

- You can also calculate Akaike Weights, which is very useful/important when comparing > 2 models. These weights can then be used to perform model averaging.
- Model selection using the Likelihood-Ratio test (LRT) is another option when you are comparing 2 models.
- Adjusted R² can be used to get a rigorous "idea" about how alternative models are performing.
- Very often, you will end up doing model simplification, especially in for linear least squares model fitting — starting with a complex model and then dropping terms till you have found a the most parsimonious version of the original model. There are functions in R to do this (of course!).

READINGS

- Levins, R. (1966) The strategy of model building in population biology. Am. Sci. 54, 421–431.
- Johnson, J. B. & Omland, K. S. (2004) Model selection in ecology and evolution. Trends Ecol. Evol. 19, 101–108.
- Bolker, B. M. et al. (2013) Strategies for fitting nonlinear ecological models in R, AD Model Builder, and BUGS. Methods Ecol. Evol. 4. 501–512.
- Additional readings on the TheMulQuaBio git repository