# Package 'rdbounds'

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| Title Manipulation Robust Regression Discontinuity Bounds Estimation  |
| Version 1.0   |
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| <b>Description</b> This package implements the estimation procedure in Gerard, Rokkanen, and Rothe (2018) to estimate bounds on treatment effects under potential manipulation of the running varible. This is a preliminary version and is still undergoing testing. We appreciate hearing any comments or issues noted. |
| <pre>URL http://www.nber.org/papers/w22892</pre>  |
| Imports data.table, formattable, parallel   |
| License GPL-3   |
| Encoding UTF-8  |
| RoxygenNote 5.0.1   |
| R topics documented:  |
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#### **Description**

This function implements the estimation procedure in Gerard, Rokkanen, and Rothe (2018) to estimate bounds on treatment effects under potential manipulation of the running varible. Returns an rdbounds object, which can then be passed to rdbounds\_summary and rdbounds\_export. Note on refinements: "Refinement A" calculates bounds based on the assumption that always-assigned units are at least as likely to receive treatment than potentially-assigned units (Theorem 3 in paper). "Refinement B" calculates bounds based on the assumption that always-assigned units always receive treatment (Theorem 4 in paper).

#### Usage

```
rdbounds(y, x, covs = NULL, treatment = NULL, c = 0, discrete_x = FALSE,
    discrete_y = FALSE, bwsx, bwy = NULL, kernel = "triangular",
    orders = array(1, dim = c(2)), evaluation_ys = NULL, ymin = NULL,
    ymax = NULL, type = "ate", percentiles = NULL, num_tau_pairs = 50,
    refinement_A = FALSE, refinement_B = FALSE, right_effects = FALSE,
    yextremes = NULL, num_lambdas = 50, num_bootstraps = c(100, 20),
    Kn = NULL, alpha = 0.05, potential_taus = NULL, parallelize = TRUE,
    progressFile = NULL, warningsFile = NULL, kernel_y = NULL,
    bwsxcov = NULL, bwycov = NULL, CDFinputs = list(original = NULL, CIsetup = NULL))
```

#### **Arguments**

orders

| 0          |  |
|------------|--|
| У          | specifies the outcome/dependent variable. Required.  |
| x          | specifies the running variable that determines eligibilty for treatment. Required.   |
| covs       | specifies covariates to implement the covariate-based refinement. Expected as a single factor variable.  |
| treatment  | specifies the treatment status variable if implementing a Fuzzy RDD. Defaults to computation of Sharp RDD results only.  |
| С          | specifies the threshold for assignment to treatment (assigned iff $x \ge c$ ). Defaults to 0.  |
| discrete_x | Boolean. If TRUE, treat each value of x as a mass-point for density estimation. Defaults to FALSE.   |
| discrete_y | Boolean. If TRUE, treat each value of y as a mass-point for density estimation. Defaults to FALSE.   |
| bwsx       | is a vector of bandwidths in x, respectively for 1) estimation of the discontinuity in the density of x at the cutoff; and 2)local polynomial estimation of conditional means. Expects either a single bandwidth to be used for both or a vector of two. Required. |
| bwy        | is a bandwidth for density estimation of y, implemented if discrete_y=FALSE. Required if discrete_y=FALSE.   |
| kernel     | specificies a kernel function to be used throughout estimation for x. Choices are triangular, rectangular, gaussian and epanechnikov. Defaults to triangular.  |

mented up to quadratic order if discrete\_X=FALSE.

specifies the order of polynomial regression, for: 1) estimation of the discontinuity in the density at the cutoff ( $\tau$  in paper), and 2) local polynomial regressions. Expects either a single integer to be used for both or a vector of two values. Defaults to 1 (local linear regression) for all. Estimation of  $\tau$  can only be imple-

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evaluation\_ys an explicit vector of y-values to evaluate CDF's at (and PDF's if discrete\_y = FALSE). If evaluation\_ys is not set, the set of unique values of y in the sample will be used. Caution is required if discrete\_y=TRUE, because computation will assume a probability mass function can be estimated from differences in estimated CDF's at subsequent values of evaluation\_ys. This can bias FRD estimates if evaluation\_ys does not contain all values in the support of y. left/lower bound on y at which to implement a boundary kernel correction if ymin discrete\_y=FALSE and y is a variable with bounded support (e.g. after censoring). Defaults to NULL, meaning no boundary kernel correction is implemented on the left side of the support of y. right/upper bound on y at which to implement a boundary kernel correction if ymax discrete\_y=FALSE and y is a variable with bounded support (e.g. after censoring). Defaults to NULL, meaning no boundary kernel correction is implemented on the left side of the support of y. "ate" for average treatment effects (default) or "qte" for quantile treatment eftype fects at the percentiles given by parameter percentiles. Defaults to ate. percentiles vector of percentiles at which to asses quantile treatment effects. Defaults to median (.5). User may add -1 as a percentile, in order to estimate average treatment effects along with QTE's. For example, percentiles=c(-1,.3,.5) will compute ATEs as well as the 30 percent and 50 percent QTEs integer number of points to search over in the set of possible values for  $(\tau_0, \tau_1)$ num\_tau\_pairs in notation of paper, for fuzzy RD estimation. Defaults to 50. If set to 1, the single tau is set to the "rightmost" (t=1) extreme of the set T, such that user can enforce the assumption that always-assigned units always receive treatment (see below), if this is consistent with data. Boolean. If TRUE, additionally calculate refined bounds with the restriction that refinement A always assigned units are at least as likely to be treated as potentially assigned units (i.e.  $\tau_1 \ge \tau$ ; see Corollary 1 in paper) Defaults to FALSE.  $Boolean.\ If\ TRUE, additionally\ calculate\ refined\ bounds\ for\ right\_effects\ with$ refinement\_B the restriction that always assigned units on the right side of the cutoff are always treated (i.e.  $\tau_0 = 0$ ; see Corollary 2 in paper) Defaults to FALSE. boolean. If set to TRUE, additionally estimate causal effects for units just to the right\_effects right of the cutoff. Defaults to FALSE. extreme values  $Y_L$  and  $Y_U$  to assume if right\_effects=TRUE, e.g. yextremes=c(0,100). yextremes Defaults to the sample range of y. num\_lambdas integer number of points to search over for the causal effect of units just to the right of the cutoff (lambda in paper). Defaults to 50. num\_bootstraps A vector of the number of bootstrap resamples desired, where the first component is the number of bootstrap samples for estimating confidence intervals, and the second is the number of samples for diagnostic testing of the estimated discontinuity in the density at the cutoff. If a scalar is given, the same number is used for both. Defaults to num\_bootstraps = c(100, 20). To avoid bootstrap testing altogether, set num\_bootstraps=NULL or num\_bootstraps=c(0,0). a hardcoded constant for  $\kappa_n$  (see Section 5.2 on inference in paper). Defaults to Kn  $log(n)^{1/2}$ , where n is the number of observations. sets the level for confidence intervals. Defaults to alpha=.05 for 95 percent alpha confidence intervals. potential\_taus vector of different values of  $\tau$  to use for the confidence intervals estimating the

potential impact of manipulation, e.g. potential\_taus=c(.025, .05, .1, .2).

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| parallelize  | indicates whether to parallelize bootstrap computations across the available number of cores on machine, minus one. Defaults to TRUE.   |
|--------------|---|
| progressFile | a file to output progress to (useful if parallelize=TRUE and the individual cores can't write to screen). File will be appended to.   |
| warningsFile | a file to output full warning messages to from bootstrap estimation if parallelize=TRUE). File will be appended to.   |
| kernel_y     | allows a separate kernel for density estimation of y. Same choices as kernel for x. Defaults to kernel specified for use with x.  |
| bwsxcov      | an optional separate bwsx to use for quantities that are computed on a subsample conditioned on a value of covs (e.g. covariate-conditional CDFs).  |
| bwycov       | an optional separate bwy to use for quantities that are computed on a subsample conditioned on a value of covs (e.g. covariate-conditional CDFs).   |
| CDFinputs    | optional, the rdbounds\$CDFinputs object from a previous run of rdbounds on the same dataset. This can be used to speed up processing by allowing CDF and PDF estimation to be skipped on a second run. |

#### References

Francois Gerard, Miikka Rokkanen, and Christoph Rothe (2016). "Bounds on Treatment Effects in Regression Discontinuity Designs under Manipulation of the Running Variable, with an Application to Unemployment Insurance in Brazil". NBER Working Paper 22892.

# **Examples**

```
df<-rdbounds_sampledata(50000, covs=TRUE)</pre>
rdbounds\_est < -rdbounds(y = df\$y, x = df\$x, covs = as.factor(df\$cov), treatment = df\$treatment, c = 0, treatment = df\$treatment = 0, treatment = 0, treat
                                                                                                                            discrete_x=FALSE, discrete_y=FALSE, bwsx=c(.2,.5), bwy = .1,
                                                                                                                            kernel="epanechnikov", orders=1,
                                                                                                                            evaluation_ys = seq(from = 0, to=23, by=.2), ymin=0, ymax=23,
                                                                                                                            num_bootstraps=0, refinement_A=TRUE, refinement_B=TRUE,
                                                                                                                            right_effects=TRUE, yextremes = c(0,23))
rdbounds_summary(rdbounds_est, title_prefix="Sample Data Results")
```

 ${\tt rdbounds\_export}$ 

Export Results from Manipulation Robust RD Estimation

# **Description**

This function exports tables from manipulation robust RD estimation

## Usage

```
rdbounds_export(rdbounds, file_name = NULL, view_it = FALSE)
```

# **Arguments**

| rdbounds  | An rdbounds object resulting from rdbounds. Required.   |
|-----------|---|
| file_name | base filename to output tables to. Expects a string of the form "path/filename", where filename has no extension and will be the root filename for a series of different files containing different tables. If omitted no files will be produced. |
| view it   | Boolean. View main results table in Rstudio viewer. Defaults to FALSE.  |

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#### **Examples**

rdbounds\_sampledata

Generate a simulated dataset for testing estimation

#### Description

This function generates a simulated dataset with which to test rdbounds. The x-values of potentially-assigned units (95 Specifically:

```
y=(x+10)/2*treatment*(always assigned=0)+5*treatment*(always assigned=1)+normal(0,1)) and y is censored at 0 and 23.
```

#### **Usage**

```
rdbounds_sampledata(sample_size = 50000, covs = FALSE)
```

#### **Arguments**

sample\_size Sample size for the dataset.

covs

If set to TRUE, generates a sample in which half of the units have one of two covariate values, where the proportion of always-assigned units is slightly different for each.

# **Examples**

```
df<-rdbounds_sampledata(50000);</pre>
```

rdbounds\_summary

Summarize Results from Manipulation Robust RD Estimation

#### **Description**

This function reports main estimands from rdbounds, as a formatted table, and optionally as text output.

#### Usage

```
rdbounds_summary(rdbounds, title_prefix = "", text = TRUE)
```

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## **Arguments**

rdbounds an rdbounds object resulting from the function rdbounds(). Required.

title\_prefix Optional prefix before "Average Treatment EFfects" or "Quantile Treatment Ef-

fects" in table.

if set to TRUE, display results as text as well as formatted table. Defaults to TRUE.

#### **Examples**

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