

**Lecture summary**

- Polarized atoms as a precision sensor for magnetometry and gyroscope
- Zeeman shift
  - First-order Zeeman shift
  - $g$  factors:  $g_L$ ,  $g_s$ ,  $g_I$ ,  $g_F$
  - Ground-level of the hydrogen
- Level avoided-crossing
  - Landau-Zener transition
- Stark shift
  - Scalar polarizability and tensor polarizability

**Homework**

1. **Zeeman shift in hydrogen maser.** There is a uniform magnetic field of 5 mGauss present in the active region of a hydrogen maser. What fractional frequency shift would result from a drift of magnetic field by 5  $\mu$ Gauss (micro-Gauss) in the following two cases: (a) the maser operates on the transition between  $|F=1, M_F=1\rangle$  and  $|F=0, M_F=0\rangle$ ; (b) the maser operates on the transition between  $|F=1, M_F=0\rangle$  and  $|F=0, M_F=0\rangle$ .
2. Textbook Exercise (6.8) Zeeman effect on hyperfine-structure at all field strengths
3. **Positronium atom.** A positronium atom is a hydrogen-like atom formed by a positron and an electron. What is the wavelength of the photons emitted by a transition from the  $n = 2$  level to the  $n = 1$  level (ground-level)? Determine the structure of the  $n = 1$  level due to magnetic dipole-dipole coupling. Draw a diagram showing how the energies of the four  $n = 1$  states evolve with magnetic field (see Fig. 6.10 for a corresponding diagram for a hydrogen atom).
4. **Stark shift** can be expressed as (E field direction is the quantization axis):

$$\Delta = -\frac{1}{2}\alpha_0 E^2 - \frac{1}{2}\alpha_2 E^2 \cdot \frac{3M_F^2 - F(F+1)}{F(2F-1)}$$

- a. Derive the expression for the Stark shift of the stretched states ( $F, M_F = +F$  or  $-F$ );
- b. Derive the expression for the Stark shifts averaged over all  $M_F$  states.
- c. Estimate the order of magnitude of the polarizabilities of the ground level of the hydrogen atom.

**Reading Assignments:**

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