

# Geographic Data Science – Lecture VI

## Exploring Space in Data

Dani Arribas-Bel

# Today

- ESDA
- Spatial Autocorrelation
- Measures
  - Global
  - Local

**ESDA**

Exploratory

Spatial

Data

Analysis

[Exploratory]

Focus on discovery and assumption-free investigation

[Spatial]

Patterns and processes that put *space* and *geography* at the core

[Data Analysis]

Statistical techniques

Questions that **ESDA** helps...

**Answer**

- *Is the variable I'm looking at concentrated over space?  
Do similar values tend to locate closeby?*
- *Can I identify any particular areas where certain values are clustered?*

**Ask**

- *What is behind this pattern? What could be generating the process?*
- *Why do we observe certain clusters over space?*

# Spatial Autocorrelation

*Everything is related to everything else, but near things are  
more related than distant things*

Waldo Tobler (1970)



# Spatial Autocorrelation

- Statistical representation of Tobler's law
- Spatial counterpart of traditional correlation

*Degree to which similar values are located in similar locations*

Two flavors:

- **Positive:** similar values → similar location (*closeby*)
- **Negative:** similar values → dissimilar location (*further apart*)

# Examples

Positive SA: income, poverty, vegetation, temperature...

Negative SA: supermarkets, police stations, fire stations, hospitals...

# Scales

## [Global]

*Clustering*: do values tend to be close to other (dis)similar values?

## [Local]

*Clusters*: are there any specific parts of a map with an extraordinary concentration of (dis)similar values?

Global Spatial Autocorr.

# Global Spatial Autocorr.

## *"Clustering"*

*Overall trend where the distribution of values follows a particular pattern over space*

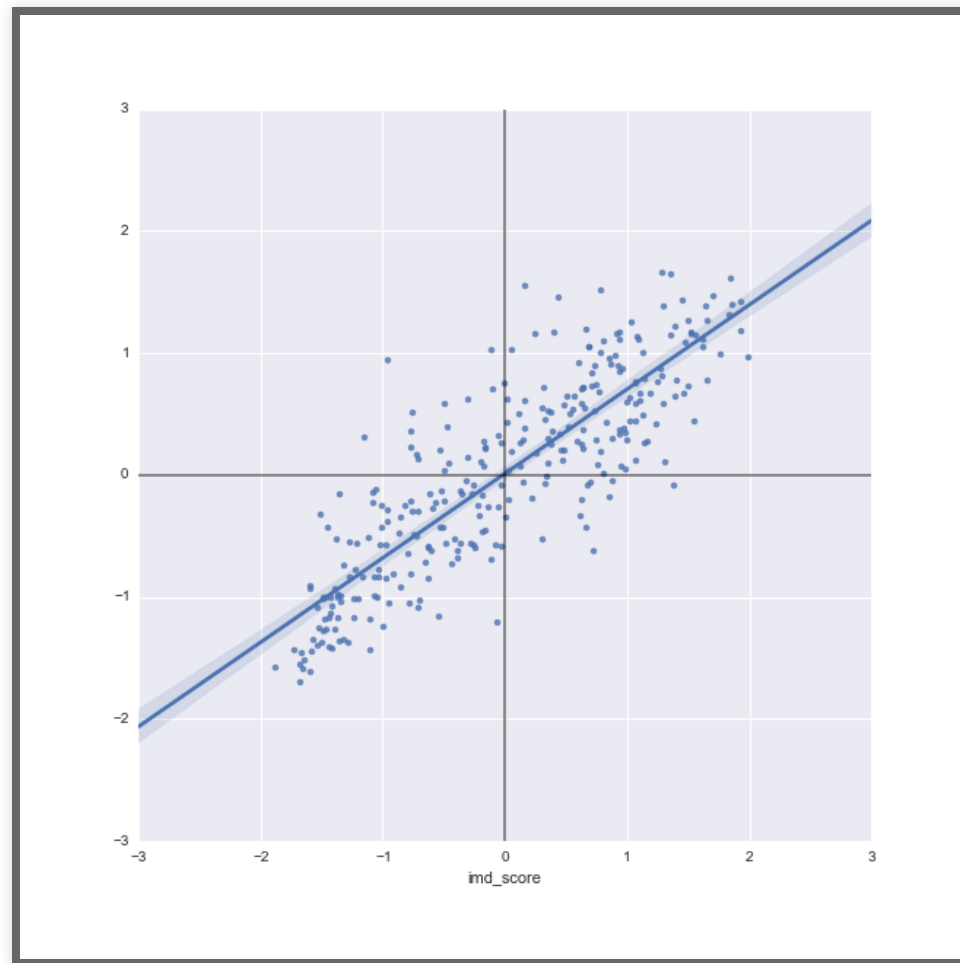
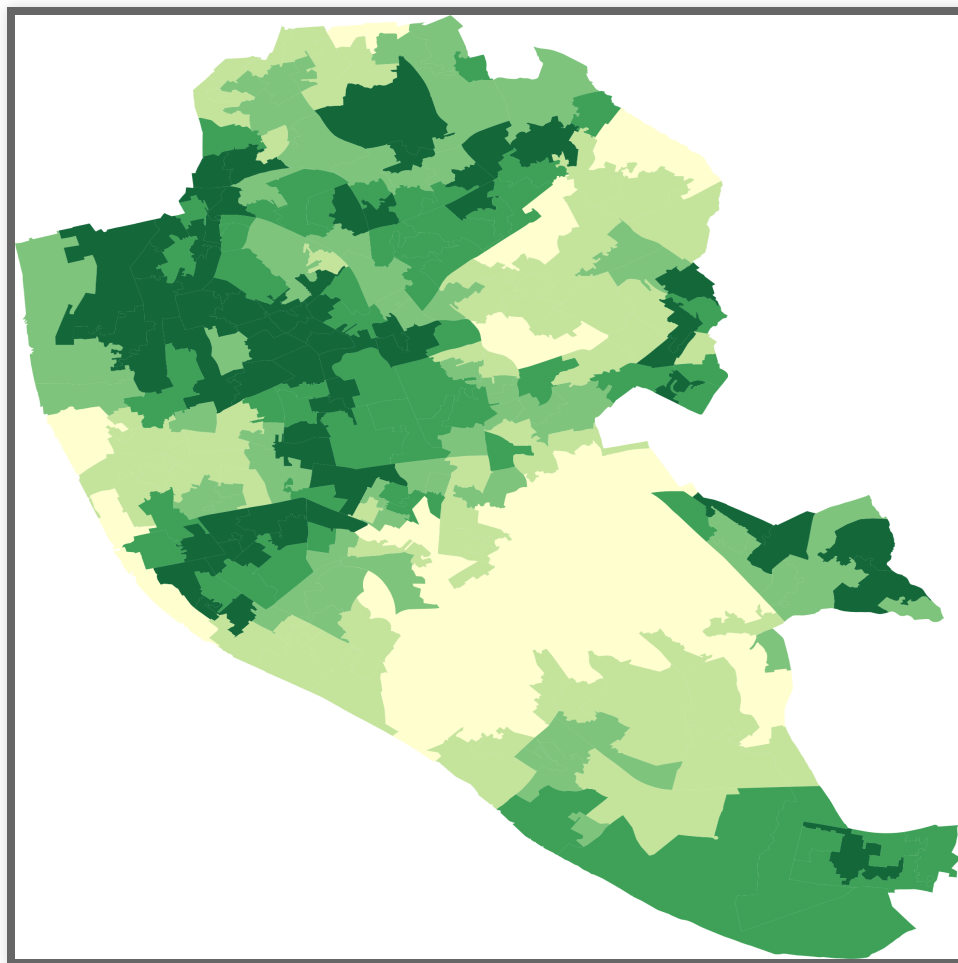
[Positive] Similar values close to each other (high-high, low-low)

[Negative] Similar values far from each other (high-low)

How to measure it???

# Moran Plot

- Graphical device that displays a variable on the horizontal axis against its spatial lag on the vertical one
- Variable and spatial weights matrix are preferably standardized
- Assessment of the overall association between a variable in a given location and in its *neighborhood*



[Interactive Demo]



# Moran's I

Formal test of global spatial autocorrelation

Statistically identify the presence of clustering in a variable

Slope of the Moran plot

Inference based on how likely it is to obtain a map like observed from a purely random pattern

$$I = \frac{N}{\sum_i \sum_j w_{ij}} \frac{\sum_i \sum_j w_{ij} (Z_i)(Z_j)}{\sum_i (Z_i)^2}$$

Local Spatial Autocorr.

# Local Spatial Autocorr.

## *"Clusters"*

*Pockets of spatial instability*

Portions of a map where values are correlated in a particularly strong and specific way

[High-High] + SA of *high* values (*hotspots*)

[Low-Low] + SA of *low* values (*coldspots*)

[High-Low] - SA (*spatial outliers*)

[Low-High] - SA (*spatial outliers*)

# LISAs

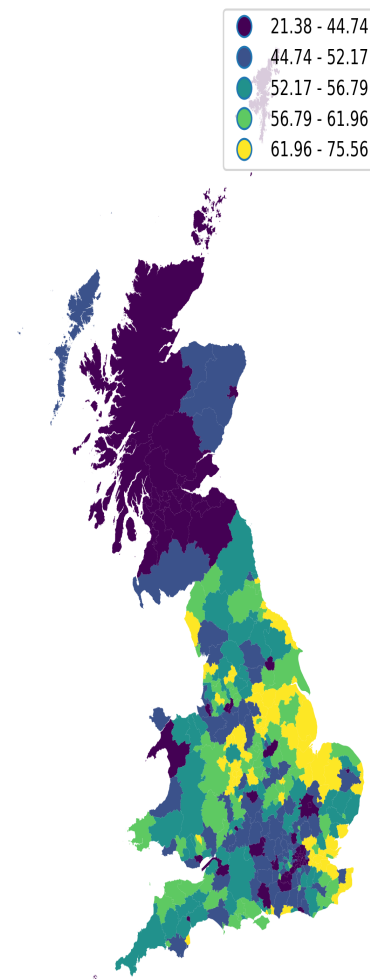
Local Indicators of Spatial Association

Statistical tests for spatial cluster detection →  
Statistical significance

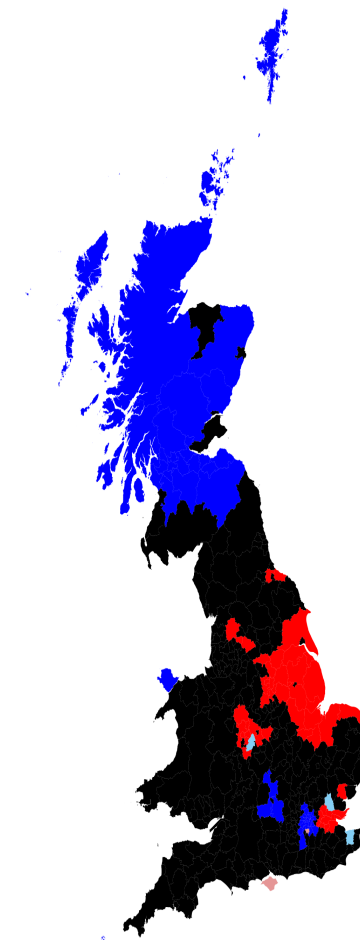
Compares the observed map with many randomly generated ones to see how likely it is to obtain the observed associations for each location

$$I_i = \frac{Z_i}{m_2} \sum_j W_{ij} Z_j \quad ; \quad m_2 = \frac{\sum_i Z_i^2}{N}$$

% to Leave



LISA for Brexit vote



# Recapitulation

**ESDA** is a family of techniques to explore and spatially interrogate data

Main function: characterize **spatial autocorrelation**, which can be explored:

- **Globally** (e.g. Moran Plot, Moran's I)
- **Locally** (e.g. LISAs)



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