

Thapar Institute of Engineering and Technology

School of Physics and Materials Science

Quantum Mechanics

TUTORIAL #9

1. Kinetic energy of an electron and photon is 4.55×10^{-25} J. Calculate the velocity, momentum and wavelength of the electron and photon.
2. Write down the conditions for the acceptable wave function and prove that $\Psi = Ae^{-x^2}$ ($-\infty \leq x \leq \infty$) is an acceptable wave function.
3. The wave function of a free particle in normalized state is represented by

$$\Psi = Ne^{-\left(\frac{x^2}{2a^2}\right) + ikx}$$

Calculate the normalization factor N and the maximum probability of finding the particle.

4. Which of the following are eigenfunctions of the operator $\frac{\partial^2}{\partial x^2}$? Find out the appropriate eigenvalues of the following functions.
 - (i) $\sin x$
 - (ii) $\sin^2 x$
5. A particle limited to the x axis has the wave function $\Psi = ax$ between $x = 0$ and $x = 1$; $\Psi = 0$ elsewhere. (a) Find the probability that the particle can be found between $x = 0.45$ and $x = 0.55$. (b) Find the expectation value $\langle x \rangle$ of the particle's position.
6. In a region of space, a particle with zero energy has a wave function $\Psi = Ae^{-\left(\frac{x^2}{L^2}\right)}$. Determine the steady state potential energy as a function of x.
7. A proton is confined in an infinite square well of width 10 fm. Calculate the energy and wavelength of the photon emitted when the proton undergoes a transition from the first excited state ($n = 2$) to the ground state ($n = 1$).
8. Electrons with energies of 1.0 eV and 2.0 eV are incident on a barrier 10.0 eV high and 0.50 nm wide. (a) Find their respective transmission probabilities. (b) How are these affected if the barrier is doubled in width?