

## Series & Progression

Q. word at 44<sup>th</sup> rank alphabetically of word "ROADIE"  
→ for keeping first two constant we have 24 arrangements

$$\therefore AD \Rightarrow 24 \text{ arrangements}$$

$$AE \Rightarrow 24 \text{ arrangements}$$

$$\therefore \boxed{AERDOI}$$

Q. 8<sup>th</sup>, 12<sup>th</sup> terms 39 & 59 then first term is -

$$a + (8-1)d = 39$$

$$a + (12-1)d = 59$$

$$d = 5$$

$$a + 7 \times 5 = 39$$

$$\boxed{a = 4}$$

Q. 15<sup>th</sup> term of 20, 15, 10, ...

$$a + (n-1)d = l$$

$$20 + (15-1) \times -5 = -50$$

Q.  $1^2 + 2^2 + 3^2 + \dots + 10^2 = 385$  then  $2^2 + 4^2 + 6^2 + \dots + 20^2 = ?$

$$(2 \cdot 1)^2 + (2 \cdot 2)^2 + (2 \cdot 3)^2 + (2 \cdot 4)^2 + \dots + (2 \cdot 10)^2 =$$

$$2^2 [1^2 + 2^2 + 3^2 + \dots + 10^2]$$

$$2^2 \times 385$$

$$4 \times 385$$

$$\boxed{1540}$$

Q. AP of 51 terms Sum of first three 65 and sum of middle is 129 what is first and common diff.?

$$\rightarrow S = \frac{n}{2} (a + l) \Rightarrow 65 = \frac{3}{2} (a + l)$$

$$a + a + d + a + 2d = 65$$

$$3a + 3d = 65 \quad \text{--- (I)}$$

$$a + 24d + a + 25d + a + 26d = 129$$

$$3a + 75d = 129 \quad \text{--- (II)}$$

$$\boxed{a = \frac{187}{9} \text{ \& } d = \frac{8}{9}}$$

Q. no. of terms in GP. 3, 6, 12, 24, ... 384?

$$\rightarrow r = \frac{x_2}{x_1} = \frac{6}{3} = 2$$

$$x_n = ar^{(n-1)}$$

$$384 = 3 \times 2^{(n-1)}$$

$$128 = 2^m$$

$$m = 7$$

$$(n-1) = 7$$

$$\boxed{n = 8}$$

Q. How many no. between 11 & 90 divisible by 7?

$$\rightarrow 14 + (n-1)7 = 90$$

$$\boxed{n = 11}$$

Q. In AP  $S_1 : S_4 = 1 : 10$  then ratio of first term to fourth term is -

$$\rightarrow \frac{S_1}{S_4} = \frac{a}{\frac{4}{2}(a + a + 3d)} = \frac{1}{10}$$

$$\frac{a}{4a + 6d} = \frac{1}{10}$$

$$d = \frac{8a}{3}$$

$$\frac{T_1}{T_2} = \frac{a}{(a + 3d)} = \frac{a}{a + 3 \times \frac{8a}{3}} = \frac{a}{4a} = \frac{1}{4}$$

Q. Sum of first three in AP is 21 product of extreme is 45 find numbers.

$$\rightarrow S_n = \frac{n}{2}(a + l) \Rightarrow 21 = \frac{3}{2}(a + l) \Rightarrow a = 14 - b$$

$$a \times l = 45 \Rightarrow a(14 - a) = 45$$

$$a^2 - 14a + 45 = 0$$

$$a = 5 \text{ or } 9 \text{ then } a_3 = 9 \quad a_2 = 7$$



or  $a$  be central number. then no.  $(a-d, a, a+d)$

$$\therefore a-d + a + a+d = 21$$

$$\boxed{a=7}$$

$$(a-d)(a+d) = 45$$

$$a^2 - d^2 = 45$$

$$\boxed{d=2}$$

$$\boxed{5, 7 \text{ \& } 9}$$

Q. Sum of first three  $-33$  and middle three  $75$ . out of 21 terms. what is sum of AP?

$$\rightarrow a + (a+d) + (a+2d) = -33$$

$$3a + 3d = -33 \quad \text{--- (I)}$$

$$(a+9d) + (a+10d) + (a+11d) = 75$$

$$3a + 30d = 75 \quad \text{--- (II)}$$

$$\boxed{d=4}$$

$$\boxed{a=-15}$$

$$S_n = \frac{n}{2} (a + l) = \frac{21}{2} (-15 + (-15 + 20 \times 4))$$

$$\boxed{S_n = 525}$$

Q. The sum of  $n$  terms AP  $= 3n^2 + n$  find  $n$ th term  
let  $n=1, 2$

$$S_2 = 3 \times 2^2 + 2 = 14, \quad S_1 = 3 \times 1^2 + 1 = 4$$

$$S_2 - S_1 = a_2$$

$$\boxed{a=4}$$

$$\boxed{a_2=10}$$

$$\therefore \boxed{d=5}$$

$$n\text{th term is } a + (n-1)d = 4 + (n-1)5 = 5n - 1$$

Q.  $3x+1, 5x+1, 5x+1, \dots$

$$\rightarrow (3x+1) + [(5x+1) - (3x+1)] \times (n-1) = 2$$

$$(3x+1) + (2x-2)(n-1) = 5x+1$$

$$\boxed{x=2}$$

Q. Ball drop from height travel distance  $\frac{128}{9}, \frac{32}{3}, 8$   
total distance travelled?

→

This is Infinite GP. with  $r = \frac{6}{8} = \frac{3}{4}$   
 $\therefore$  total distance =  $\frac{a}{1-r}$

$$= \frac{128}{9(1-\frac{3}{4})} = \frac{4 \times 128}{9} = \frac{512}{9}$$

Q. sum of first second term is ~~48~~<sup>36</sup> and Sum of all terms of GP ~~is~~<sup>is</sup> 48 ~~from~~ find second term?

→

$$a + ar = 36$$

$$\frac{a}{(1-r)} = 48$$

$$\therefore r = \frac{1}{2}$$

$$a = 24$$

$$a_2 = 12$$

Q. find three GM of 2, 81/8

→

$$a = 2$$

$$ar^4 = \frac{81}{8} \Rightarrow r^4 = \frac{81}{16} \Rightarrow \boxed{r = \frac{3}{2}}$$

$$ar = 3, ar^2 = \frac{9}{2}, ar^3 = \frac{27}{4}$$

Q. AM is 75 and GM is 21 Find no.

→

$$\frac{a_1 + a_2}{2} = 75$$

$$a_1 = 150 - a_2$$

$$\sqrt{a_1 a_2} = 21$$

$$a_1 = \frac{441}{a_2}$$

$$\boxed{a_1 = 3 \quad a_2 = 147}$$

Q. The product of first three terms of GP is 512  
if we add 2 to second term, the three terms  
becomes AP. find GP

let  $\frac{a}{r}, a, ar$

$$a^3 = 584$$

$$\boxed{a = 8}$$

$a, a+2, ar$  in ap (AP) hence  
 $(a+2) - a/r = ar - (a+2)$

$$10 - \frac{8}{r} = 8r - 10$$

$$8r^2 - 20r + 8 = 0$$

$$r = 2 \text{ or } r = \frac{1}{2}$$

$$\boxed{GP = 4, 8, 16 \text{ or } 16, 8, 4}$$

7. What is 8th term of  $1, 1/8, 1/27 \dots$

$$\frac{1}{(1)^3}, \frac{1}{(2)^3}, \frac{1}{(3)^3} \dots \frac{1}{(8)^3}$$

$$\boxed{= \frac{1}{512}}$$

8. Sum of three terms of GP is 105 and if first two multiplied by 4 and third by 3 then they are in AP.  
 → find highest term.

$$\frac{a}{r} + a + ar = 105$$

$$4 \times \frac{a}{r} + 4ar = 2 \times a$$

$$\left(a - \frac{a}{r}\right) \times 4 = 3ar - 4a$$

$$a(r-1)4 = (3r-4)a$$

$$4r-4 = 3r-4$$

$$3r^2 - 8r + 4 = 0$$

$$r = 2 \text{ or } \frac{2}{3}$$

$$\therefore \frac{a}{2} + a + 2a = 105$$

$$\therefore \frac{7a}{2} = 105$$

$$\therefore a = 30$$



Q.  $x, y, z$  betn 4 & 40 such that i) sum is 37 ii)  $4, x, y$  is f  
 iii)  $y, z, 40$  is GP find  $z$

$$\rightarrow 2x = 4 + y$$

$$2z = 40y \Rightarrow y = \frac{z^2}{40}$$

$$x + y + z = 37 \Rightarrow x = 37 - y - z$$

$$\therefore 2(37 - y - z) = 4 + y$$

$$3y = 70 - 2z$$

$$3y = 70 - 2 \times \frac{z^2}{40}$$

$$\frac{3z^2}{40} = 70 - 2z$$

$$\boxed{z = 20}$$

$$\therefore \boxed{y = 10 \text{ \& } x = 7}$$

Q. four no.  $p, q, r, s$  with first three in GP and last in AP with  $d$   
 first and fourth is same find  $p$ .

$$\rightarrow \frac{a}{r}, a, ar, ar+3$$

from (I) & (II)

$$\frac{3}{(r-1)r} = \frac{3r}{(r-1)} + 3$$

$$\frac{a}{r} = ar + 3 \quad \text{--- (I)}$$

$$3 = 6r^2 - 3r$$

$$ar - a = 3 \quad \text{--- (II)}$$

$$6r^2 - 3r - 3 = 0$$

$$r = 1 \text{ or } -1/2$$

$$\therefore a = \frac{3}{r-1} = \frac{3}{-1/2-1} = -2$$

$$\therefore \boxed{a = -2}$$

$$\therefore \boxed{4, -2, 1, 4}$$

Q. Sum of three no. in GP is  $21/2$  and their product is 72  
 what are no?

$$\rightarrow \frac{a}{r}, a, ar$$

$$\frac{a}{r} \times a \times ar = 72 \Rightarrow a^3 = 216 \Rightarrow a = 6$$

$$\frac{a}{r} + a + ar = 21/2 \Rightarrow (r^2 + r + 1) \frac{a}{r} = 21/2 \Rightarrow 2r^2 + 5r + 2 = 0$$

$$r = 2 \text{ or } 1/2$$

$$\therefore \boxed{3/2, 6, 9 \text{ \& } 6, 3, 3/2}$$