Analyze A/B Test Results

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Introduction

For this project, we will be working to understand the results of an A/B test run by an e-commerce website. The goal is to work through this notebook is to help the company understand if they should implement the new page, keep the old page, or perhaps run the experiment longer to make their decision.

Part I - Probability

```
In [1]:
```

```
import pandas as pd
import numpy as np
import random
import matplotlib.pyplot as plt
%matplotlib inline
#We are setting the seed to assure you get the same answers on quizzes as we set up
random.seed(42)
```

```
In [2]:
```

```
df = pd.read_csv('ab_data.csv')
df.head()
```

Out[2]:

| | user_id | timestamp group landing_page | | converted | | |
|---|---------|------------------------------|-----------|-----------|---|--|
| 0 | 851104 | 2017-01-21 22:11:48.556739 | control | old_page | 0 | |
| 1 | 804228 | 2017-01-12 08:01:45.159739 | control | old_page | 0 | |
| 2 | 661590 | 2017-01-11 16:55:06.154213 | treatment | new_page | 0 | |
| 3 | 853541 | 2017-01-08 18:28:03.143765 | treatment | new_page | 0 | |
| 4 | 864975 | 2017-01-21 01:52:26.210827 | control | old_page | 1 | |

```
In [3]:
```

```
#The number of rows in the dataset.
number_rows = df.shape[0]
print("Number of rows: {}".format(number_rows))
#print(len(df))
```

Number of rows: 294478

In [4]:

```
#The number of unique users in the dataset.
num_unique_users = len(df.user_id.unique())
print("Number of unique users: {}".format(num_unique_users))
```

Number of unique users: 290584

```
In [5]:
#The proportion of users converted.
df['converted'].mean()
Out[5]:
0.11965919355605512
In [6]:
#The number of times the new page and treatment don't line up.
#treatment_new_pg = df[df(['group']=='treatment') & df(['landing_page']=='new_page')]
#control_old_page = df[df(['group']=='control') & df(['landing_page']=='old_page')]
mismatch treatment to old pg = df.query("group=='treatment' & landing page =='old page'")
mismatch_control_to_new_page = df.query("group=='control' & landing_page =='new_page'")
In [7]:
total_ttop = len(mismatch_treatment_to_old_pg)
total ctnp = len(mismatch control to new page)
print(total_ttop+total_ctnp)
3893
In [8]:
# check for missing values
df.isnull().any()
Out[8]:
                 False
user_id
timestamp
                 False
group
                 False
landing page
                False
converted
                 False
dtype: bool
2. For the rows where treatment is not aligned with new_page or control is not aligned with old_page, we cannot be sure if this
row truly received the new or old page. Drop rows and create a new dataset that meets the specifications from the classroom quiz.
Store your new dataframe in df2.
In [9]:
#make a copy of the df
df2 = df
In [10]:
df2.drop(mismatch_treatment_to_old_pg.index, inplace=True)
df2.drop(mismatch_control_to_new_page.index, inplace=True)
In [11]:
# Double Check all of the correct rows were removed - this should be 0
df2[((df2['group'] == 'treatment') == (df2['landing_page'] == 'new_page')) == False].shape[0]
Out[11]:
0
In [12]:
#unique user_ids in df2
len(df2.user id.unique())
```

```
Out[12]:
290584
b. There is one user_id repeated in df2. What is it?
In [13]:
df2.duplicated().sum()
Out[13]:
0
In [14]:
print(df2.user_id.duplicated())
0
          False
1
         False
2
         False
         False
3
4
         False
5
        False
6
         False
7
         False
8
         False
         False
9
10
        False
11
        False
12
         False
13
         False
14
         False
15
         False
16
         False
17
         False
18
         False
19
          False
20
         False
21
         False
23
        False
24
         False
25
         False
26
         False
27
         False
28
         False
29
         False
30
         False
294448
         False
294449
         False
294450
         False
294451
         False
294452
         False
         False
294453
294454
         False
294455
         False
294456
         False
294457
         False
294458
         False
294459
         False
294460
        False
294461
        False
294462
         False
294463
         False
         False
294464
294465
         False
294466
         False
294467
         False
294468
         False
294469
         False
294470
         False
294471
         False
```

```
294472 False
294473 False
294474 False
294475 False
294476 False
294477 False
Name: user_id, Length: 290585, dtype: bool
```

In [15]:

```
df2[df2.duplicated('user_id')]
```

Out[15]:

| | user_id | timestamp | group | landing_page | converted |
|------|---------|----------------------------|-----------|--------------|-----------|
| 2893 | 773192 | 2017-01-14 02:55:59.590927 | treatment | new_page | 0 |

c. What is the row information for the repeat user_id?

In [16]:

```
df2[df2['user_id']==773192]
```

Out[16]:

| | user_id | timestamp | group | landing_page | converted |
|------|---------|----------------------------|-----------|--------------|-----------|
| 1899 | 773192 | 2017-01-09 05:37:58.781806 | treatment | new_page | 0 |
| 2893 | 773192 | 2017-01-14 02:55:59.590927 | treatment | new_page | 0 |

d. Remove one of the rows with a duplicate user_id, but keep your dataframe as df2.

In [17]:

```
#drop
df2.drop(labels=1899, axis=0, inplace=True)
#confirm
df2[df2['user_id']==773192]
```

Out[17]:

| | user_id | timestamp | group | landing_page | converted |
|------|---------|----------------------------|-----------|--------------|-----------|
| 2893 | 773192 | 2017-01-14 02:55:59.590927 | treatment | new_page | 0 |

- 4. Use df2 in the below cells to answer the quiz questions related to Quiz 4 in the classroom.
- a. What is the probability of an individual converting regardless of the page they receive?

In [18]:

```
df2['converted'].mean()
```

Out[18]:

0.11959708724499628

b. Given that an individual was in the control group, what is the probability they converted?

In [19]:

```
control_conversion = df2[df2['group'] == 'control']['converted'].mean()
control_conversion
```

```
Out[19]:
```

0.1203863045004612

c. Given that an individual was in the treatment group, what is the probability they converted?

```
In [20]:
```

```
treatment_conversion = df2[df2['group'] == 'treatment']['converted'].mean()
treatment_conversion
```

Out[20]:

0.11880806551510564

d. What is the probability that an individual received the new page?

```
In [21]:
```

```
df2['landing_page'].replace({'old_page':0,'new_page':1},inplace=True)
#df2['landing_page'].mean()
#df2['landing_page'].value_counts()[0]/len(df2)
#df.converted.sum()/len(df)
```

```
In [22]:
```

```
df2['landing_page'].mean()
```

Out[22]:

0.5000619442226688

```
In [23]:
```

```
obs_diff = treatment_conversion - control_conversion
```

e. Is there evidence to suggest that one page leads to more conversions?

The control group which was shown the old page had a higher conversion rate. However, the difference is small at .2%. Given the current data, the new page has a lower conversion rate than the old, control page. Conclusion: we need more information to make a final decision. Further questions to consider:

- did change aversion play a role in the results?
- how did test span duration impact results?

Part II - A/B Test

Notice that because of the time stamp associated with each event, you could technically run a hypothesis test continuously as each observation was observed.

However, then the hard question is do you stop as soon as one page is considered significantly better than another or does it need to happen consistently for a certain amount of time? How long do you run to render a decision that neither page is better than another?

1. For now, consider you need to make the decision just based on all the data provided. Assume that the old page is better unless the new page proves to be definitely better at a Type I error rate of 5%.

Null hypothesis

```
H_{1}\: p_{\text{new}} - p_{\text{old}} > 0
```

2. Assume under the null hypothesis, $p_{\text{new}}\$ and $p_{\text{old}}\$ both have "true" success rates equal to the **converted** success rate regardless of page - that is $p_{\text{new}}\$ and $p_{\text{old}}\$ are equal. Furthermore, assume they are equal to the **converted** rate in **ab_data.csv** regardless of the page.

Use a sample size for each page equal to the ones in **ab_data.csv**.

Perform the sampling distribution for the difference in **converted** between the two pages over 10,000 iterations of calculating an estimate from the null.

a. convert rate for \$p_{new}\$ under the null

```
In [24]:
```

```
p_new = df2['converted'].mean()
print(p_new)
```

0.11959708724499628

b. convert rate for \$p_{old}\$ under the null

```
In [25]:
```

```
p_old = df2['converted'].mean()
print(p_old)
```

0.11959708724499628

c. \$n_{new}\$

d. \$n_{old}\$

In [26]:

```
n_new, n_old = df2['landing_page'].value_counts()
print("n_new:", n_new, "\nn_old:", n_old)
```

n_new: 145310
n_old: 145274

In [27]:

```
#number of users that received the new page; where group = treatment
df2.query("group=='treatment'").count()
```

Out[27]:

```
user_id 145310
timestamp 145310
group 145310
landing_page 145310
converted 145310
dtype: int64
```

In [28]:

```
#number of users that received the old page; where group = control
df2.query("group=='control'").count()
```

Out[28]:

user id 145274

```
timestamp 145274
group 145274
landing_page 145274
converted 145274
dtype: int64

In [29]:

#n_new = df2.query("group=='treatment'").count()

In [30]:

#n_old = df2.query("group=='control'").count()
```

e. Simulate $n_{\text{new}}\$ transactions with a convert rate of $p_{\text{new}}\$ under the null. Store these $n_{\text{new}}\$ 1's and 0's in $new_page_converted$.

```
In [31]:
```

```
new_page_converted = np.random.choice([1,0], size=n_new, p=[p_new, (1 - p_new)])
#new_page_converted = np.random.binomial(1,p_new,n_new)
#new_page_converted = \
    #np.random.choice([0,1], size=n_new, p=[(1-p_new), p_new])
```

f. Simulate $n_{old}\$ transactions with a convert rate of $p_{old}\$ under the null. Store these $n_{old}\$ 1's and 0's in $old_page_converted$.

```
In [32]:
```

```
old_page_converted = np.random.choice([1,0], size=n_old, p=[p_old, (1-p_old)])
```

g. Find \$p_{new}\$ - \$p_{old}\$ for your simulated values from part (e) and (f).

```
In [33]:
```

```
new_page_converted.mean() - old_page_converted.mean()
```

Out[33]:

0.0005141862086504162

h. Simulate 10,000 \$p_{new}\$ - \$p_{old}\$ values using this same process similarly to the one you calculated in parts **a. through g.** above. Store all 10,000 values in **p diffs**.

```
In [34]:
```

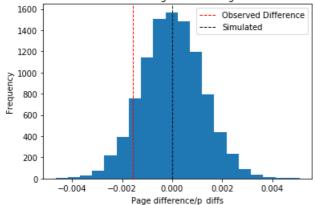
```
p_diffs = []
for _ in range(10000):
    new_page_converted = np.random.choice([1,0], size=n_new, p=[p_new, (1-p_new)]).mean()
    old_page_converted = np.random.choice([1,0], size=n_old, p=[p_old, (1-p_old)]).mean()
    diff=new_page_converted-old_page_converted
    p_diffs.append(diff)
```

i. histogram of the **p_diffs**.

In [35]:

```
plt.hist(p_diffs, bins=20)
plt.title('10k - Simulated Difference of New Page and Old Page Conversions Under the Null')
plt.xlabel('Page difference/p_diffs')
plt.ylabel('Frequency')
plt.axvline(x=obs_diff, color='red', linewidth=1, linestyle='dashed',label="Observed Difference")
plt.axvline(x=(np.array(p_diffs).mean()), color='black', linestyle='dashed', linewidth=1, label="Simulated")
plt.legend()
plt.show();
```

10k - Simulated Difference of New Page and Old Page Conversions Under the Null



This simulated difference shows a mean of zero, this is what the data looks like under the null hypothesis. You can see how this differs from the observed difference.

j. proportion of the p_diffs that are greater than the actual difference observed in ab_data.csv

In [36]:

```
p_diff = p_new - p_old
p_diff
```

Out[36]:

0.0

In [37]:

```
p_diffs = np.array(p_diffs)
(p_diffs > obs_diff).mean()
```

Out[37]:

0.905100000000000002

k. A look at the p-value and statistical significance

A p-value of 90% is significant and allows us to fail to reject the null hypothesis.

- A p-value helps determine the significance of results.
- The P value, or calculated probability, is the probability of finding the observed...given that the null hypothesis is true.
- p-value is the chance that you'd get data that are as extreme as the data you have, from a random sample of points...the probability of the observed.
- The p-value is the level of marginal significance within a statistical hypothesis test representing the probability of the
 occurrence of a given event. The p-value is used as an alternative to rejection points to provide the smallest level of
 significance at which the null hypothesis would be rejected.

The p-value is a number between 0 and 1:

- A small p-value (typically ≤ 0.05) indicates strong evidence against the null hypothesis...reject the null hypothesis.
- A large p-value (> 0.05) indicates weak evidence against the null hypothesis...fail to reject the null hypothesis.
- p-values very close to the cutoff (0.05) are marginal and require additional information.

I. We could also use a built-in to achieve similar results. Calculate the number of conversions for each page, as well as the number of individuals who received each page. Let n_old and n_new refer the number of rows associated with the old page and new pages, respectively.

In [38]:

```
import statsmodels.api as sm
```

```
convert_old = sum(dr2.query("group == control")[ converted ])
convert_new = sum(df2.query("group == 'treatment'")['converted'])
n_old = len(df2.query("group == 'control'"))
n_new = len(df2.query("group == 'treatment'"))

/Users/Irene/anaconda3/lib/python3.6/site-packages/statsmodels/compat/pandas.py:56: FutureWarning:
The pandas.core.datetools module is deprecated and will be removed in a future version. Please use the pandas.tseries module instead.
    from pandas.core import datetools
```

m. Now use stats.proportions ztest to compute your test statistic and p-value. Read more on using the built-in.

```
In [39]:
```

```
z_score, p_value = sm.stats.proportions_ztest([convert_old, convert_new], [n_old, n_new],
alternative='smaller')
z_score, p_value
```

Out[39]:

(1.3109241984234394, 0.90505831275902449)

n. About the z-score and p-value:

A z-score shows the number of standard deviations from the mean a data point is, positive z-scores show that our data point is on the right side of the mean on the bell curve. This p value is very close to the p value that we calculated earlier. With this confirmed 90% p-value (using the built-in) we continue to fail to reject the null hypothesis.

Part III - A regression approach

1. The result acheived in the previous A/B test can also be acheived by performing a Logistic regression.

Logistic regression will work because each row is either a conversion or no conversion.

b. The goal is to use **statsmodels** to fit the regression model specified in part **a.** to see if there is a significant difference in conversion based on which page a customer receives. However, we first need to create a column for the intercept, and create a dummy variable column for which page each user received.

Add an intercept column, as well as an ab_page column, which is 1 when an individual receives the treatment and 0 if control.

```
In [40]:
```

```
df.head()
```

Out[40]:

| | user_id | timestamp | group | landing_page | converted |
|---|---------|----------------------------|-----------|--------------|-----------|
| 0 | 851104 | 2017-01-21 22:11:48.556739 | control | 0 | 0 |
| 1 | 804228 | 2017-01-12 08:01:45.159739 | control | 0 | 0 |
| 2 | 661590 | 2017-01-11 16:55:06.154213 | treatment | 1 | 0 |
| 3 | 853541 | 2017-01-08 18:28:03.143765 | treatment | 1 | 0 |
| 4 | 864975 | 2017-01-21 01:52:26.210827 | control | 0 | 1 |

```
In [41]:
```

```
df2.head()
```

user_id timestamp group landing_page converted **0** 851104 2017-01-21 22:11:48.556739 control 0 0 **1** 804228 2017-01-12 08:01:45.159739 0 0 control **2** 661590 2017-01-11 16:55:06.154213 0 treatment 1 3 853541 2017-01-08 18:28:03.143765 treatment 864975 2017-01-21 01:52:26.210827 control 0

```
In [42]:
```

```
df_r = df2.copy()
```

In [43]:

```
df_r['intercept']=1
df_r[['control', 'treatment']] = pd.get_dummies(df['group'])
```

In [44]:

```
df_r.head()
```

Out[44]:

| | user_id | timestamp | group | landing_page | converted | intercept | control | treatment |
|---|---------|----------------------------|-----------|--------------|-----------|-----------|---------|-----------|
| 0 | 851104 | 2017-01-21 22:11:48.556739 | control | 0 | 0 | 1 | 1 | 0 |
| 1 | 804228 | 2017-01-12 08:01:45.159739 | control | 0 | 0 | 1 | 1 | 0 |
| 2 | 661590 | 2017-01-11 16:55:06.154213 | treatment | 1 | 0 | 1 | 0 | 1 |
| 3 | 853541 | 2017-01-08 18:28:03.143765 | treatment | 1 | 0 | 1 | 0 | 1 |
| 4 | 864975 | 2017-01-21 01:52:26.210827 | control | 0 | 1 | 1 | 1 | 0 |

In [45]:

```
df_regression = df2.copy()
```

In [46]:

```
df_regression['intercept']=1
df_regression[['drop', 'ab_page']] = pd.get_dummies(df_regression['group'])
df_regression.drop(['drop'], axis=1, inplace=True)
df_regression.head()
```

Out[46]:

| | | user_id | timestamp | group | landing_page | converted | intercept | ab_page |
|----|---|---------|----------------------------|-----------|--------------|-----------|-----------|---------|
| (| 0 | 851104 | 2017-01-21 22:11:48.556739 | control | 0 | 0 | 1 | 0 |
| | 1 | 804228 | 2017-01-12 08:01:45.159739 | control | 0 | 0 | 1 | 0 |
| : | 2 | 661590 | 2017-01-11 16:55:06.154213 | treatment | 1 | 0 | 1 | 1 |
| [; | 3 | 853541 | 2017-01-08 18:28:03.143765 | treatment | 1 | 0 | 1 | 1 |
| Ŀ | 4 | 864975 | 2017-01-21 01:52:26.210827 | control | 0 | 1 | 1 | 0 |

c. Use **statsmodels** to import your regression model. Instantiate the model, and fit the model using the two columns you created in part **b.** to predict whether or not an individual converts.

.....

```
In [47]:
```

```
lrm = sm.Logit(df_regression['converted'],df_regression[['intercept', 'ab_page']])
```

d. Provide the summary of your model below, and use it as necessary to answer the following questions.

In [48]:

```
results = lrm.fit()
results.summary()
```

Optimization terminated successfully.

Current function value: 0.366118

Iterations 6

Out[48]:

Logit Regression Results

| Dep. Variable: | converted | No. Observations: | 290584 |
|----------------|------------------|-------------------|-------------|
| Model: | Logit | Df Residuals: | 290582 |
| Method: | MLE | Df Model: | 1 |
| Date: | Sun, 12 Aug 2018 | Pseudo R-squ.: | 8.077e-06 |
| Time: | 16:42:37 | Log-Likelihood: | -1.0639e+05 |
| converged: | True | LL-Null: | -1.0639e+05 |
| | | LLR p-value: | 0.1899 |

| | coef | std err | z | P> z | [0.025 | 0.975] |
|-----------|---------|---------|----------|-------|--------|--------|
| intercept | -1.9888 | 0.008 | -246.669 | 0.000 | -2.005 | -1.973 |
| ab_page | -0.0150 | 0.011 | -1.311 | 0.190 | -0.037 | 0.007 |

In []:

```
# interprete the coefficients
1/np.exp(results.params[1])
```

In []:

```
# p-value as if it were a one-tailed test
1-0.190/2
```

- e. The p-value associated with ab_page
 - p-value associated with ab_page = .19
 - p-value calculated in part II = .90
 - p-value calculated in part II with the built-in method = .90

This difference is due to the null and alternative hypothesis. The main null hypothesis of a multiple logistic regression is that there is no relationship between the X variables and the Y variable; in other words, the Y values you predict from your multiple logistic regression equation are no closer to the actual Y values than you would expect by chance.

```
Hypothesis from Part II H_{0}\: p_{\text{new}} - p_{\text{old}} \le 0 H_{1}\: p_{\text{new}} - p_{\text{old}} > 0
```

H0= conversion probability for a user receiving the new page is less than or equal to that of a user receiving the old page

Hypothesis from Part III Regression Model $$H_{0}: p_{new} - p_{old} = 0$$$ H_{1}: p_{new} - p_{old} \neq 0$$ Ho = there is no relationship between which page a user is shown and the conversion rate.$

f. Advantages and disadvantages to adding additional terms into the regression model

It is advantagous to research additional factors and assess whether to add them to the model. For example, it could be worthwhile to look at

- · prerequisiste knowledge
- · prior conversions on similar sites
- · traffic source
- CTR
- age

Disagvantages include potential multicollinearity, issues with higher order terms, and making the model too complex.

g. Review the impact if any of 'user country of access' Read more on merging here are the docs for joining tables.

Does it appear that country had an impact on conversion?

In [49]:

```
countries_df = pd.read_csv('countries.csv')
countries_df.head()
```

Out[49]:

| | user_id | country |
|---|---------|---------|
| 0 | 834778 | UK |
| 1 | 928468 | US |
| 2 | 822059 | UK |
| 3 | 711597 | UK |
| 4 | 710616 | UK |

In [50]:

```
df_c_merge = countries_df.set_index('user_id').join(df_regression.set_index('user_id'),
how='inner')
df_c_merge.head()
```

Out[50]:

| | country | timestamp | group | landing_page | converted | intercept | ab_page |
|---------|---------|----------------------------|-----------|--------------|-----------|-----------|---------|
| user_id | | | | | | | |
| 834778 | UK | 2017-01-14 23:08:43.304998 | control | 0 | 0 | 1 | 0 |
| 928468 | US | 2017-01-23 14:44:16.387854 | treatment | 1 | 0 | 1 | 1 |
| 822059 | UK | 2017-01-16 14:04:14.719771 | treatment | 1 | 1 | 1 | 1 |
| 711597 | UK | 2017-01-22 03:14:24.763511 | control | 0 | 0 | 1 | 0 |
| 710616 | UK | 2017-01-16 13:14:44.000513 | treatment | 1 | 0 | 1 | 1 |

In [51]:

```
#See types and options for country
for feature in ['country']:
    print("{}: {}".format(feature, countries_df[feature].unique()))
```

```
country: ['UK' 'US' 'CA']
In [52]:
df_c_merge['country'].astype(str).value_counts()
Out[52]:
US
      203619
      72466
UK
       14499
CA
Name: country, dtype: int64
In [53]:
#df_c_merge['country']['converted'].mean()
df_c_merge.groupby('country')['converted'].mean()
Out[53]:
country
      0.115318
IJK
     0.120594
     0.119547
Name: converted, dtype: float64
In [54]:
UK_treatment_conversion = df_c_merge[(df_c_merge['group']== 'treatment') & (df_c_merge['country'] =
= 'UK')]['converted'].mean()
UK_treatment_conversion
Out[54]:
0.1211709965102753
In [55]:
UK_control_conversion = df_c_merge[(df_c_merge['group']== 'control') & (df_c_merge['country'] ==
'UK')]['converted'].mean()
UK_control_conversion
Out[55]:
0.12002200220022002
      The UK has a higher conversion rate overall. This is slightly higher in the treatment group.
```

h. Are there significant regional effects on conversion?

```
In [56]:
```

```
#create dummy variables
df_c_merge[['CA', 'UK', 'US']] = pd.get_dummies(df_c_merge['country'])
df_c_merge.head()
```

Out[56]:

| | country | timestamp | group | landing_page | converted | intercept | ab_page | CA | UK | US |
|---------|---------|----------------------------|-----------|--------------|-----------|-----------|---------|----|----|----|
| user_id | | | | | | | | | | |
| 834778 | UK | 2017-01-14 23:08:43.304998 | control | 0 | 0 | 1 | 0 | 0 | 1 | 0 |
| 928468 | US | 2017-01-23 14:44:16.387854 | treatment | 1 | 0 | 1 | 1 | 0 | 0 | 1 |
| 822059 | UK | 2017-01-16 14:04:14.719771 | treatment | 1 | 1 | 1 | 1 | 0 | 1 | 0 |
| | | | i | | | | | | | |

| 711597 | Country | 2017-01-22 03:14:24.763511 timestamp | group! | landing_page | Converted | intercept | ab_page | ВA | ŮΚ | _ย ร |
|--------|---------|---|-----------|--------------|-----------|-----------|---------|----|----|----------------|
| 719616 | UK | 2017-01-16 13:14:44.000513 | treatment | 1 | 0 | 1 | 1 | 0 | 1 | 0 |

In [57]:

```
#fit the linear model
linear_model_p3 = sm.OLS(df_c_merge['converted'], df_c_merge[['intercept', 'ab_page', 'US',
'UK']])
lin_results = linear_model_p3.fit()
lin_results.summary()
```

Out[57]:

OLS Regression Results

| Dep. Variable: | converted | R-squared: | 0.000 |
|-------------------|------------------|---------------------|-----------|
| Model: | OLS | Adj. R-squared: | 0.000 |
| Method: | Least Squares | F-statistic: | 1.640 |
| Date: | Sun, 12 Aug 2018 | Prob (F-statistic): | 0.178 |
| Time: | 16:42:39 | Log-Likelihood: | -85266. |
| No. Observations: | 290584 | AIC: | 1.705e+05 |
| Df Residuals: | 290580 | BIC: | 1.706e+05 |
| Df Model: | 3 | | |
| Covariance Type: | nonrobust | | |

| | coef | std err | t | P> t | [0.025 | 0.975] |
|-----------|---------|---------|--------|-------|--------|--------|
| intercept | 0.1161 | 0.003 | 42.036 | 0.000 | 0.111 | 0.122 |
| ab_page | -0.0016 | 0.001 | -1.307 | 0.191 | -0.004 | 0.001 |
| US | 0.0042 | 0.003 | 1.514 | 0.130 | -0.001 | 0.010 |
| UK | 0.0053 | 0.003 | 1.784 | 0.074 | -0.001 | 0.011 |

| Omnibus: | 125551.169 | Durbin-Watson: | 1.996 | |
|----------------|------------|-------------------|------------|--|
| Prob(Omnibus): | 0.000 | Jarque-Bera (JB): | 414297.780 | |
| Skew: | 2.345 | Prob(JB): | 0.00 | |
| Kurtosis: | 6.497 | Cond. No. | 10.8 | |

In [58]:

```
#fit the logistical regression model
df_c_merge['intercept'] = 1

lm = sm.Logit(df_c_merge['converted'], df_c_merge[['intercept', 'US', 'CA']])
results_countries = lm.fit()
results_countries.summary()
```

Optimization terminated successfully.

Current function value: 0.366116

Iterations 6

Out[58]:

Logit Regression Results

| Dep. Variable: | converted | No. Observations: | 290584 |
|----------------|------------------|-----------------------|-----------|
| Model: | Logit | Df Residuals: | 290581 |
| Method: | MLE | Df Model: | 2 |
| Date: | Sun, 12 Aug 2018 | Pseudo R-squ.: | 1.521e-05 |
| T: | 10.40.40 | 1 a.a. 1 !!ra!!haaal. | 4 0000 OF |

| ı ime: | 16:42:40 | Log-Likelinooa: | -1.0639e+05 | |
|------------|----------|-----------------|-------------|--|
| converged: | True | LL-Null: | -1.0639e+05 | |
| | | LLR p-value: | 0.1984 | |

| | coef | std err | z | P> z | [0.025 | 0.975] |
|-----------|---------|---------|----------|-------|--------|--------|
| intercept | -1.9868 | 0.011 | -174.174 | 0.000 | -2.009 | -1.964 |
| US | -0.0099 | 0.013 | -0.746 | 0.456 | -0.036 | 0.016 |
| CA | -0.0507 | 0.028 | -1.786 | 0.074 | -0.106 | 0.005 |

```
In [59]:
np.exp(results.params)
Out[59]:
intercept
             0.136863
            0.985123
ab_page
dtype: float64
In [60]:
1/np.exp(-0.0099), np.exp(-0.0506)
Out[60]:
(1.009949167117542, 0.95065885803307082)
In [61]:
1/np.exp(results_countries.params[1])
Out[61]:
1.0099656034853544
```

• US web visitors/users are roughly as likely to convert as users from the UK (1.00)

- Canadian web visitors/users are .95 times more likely to convert as users from the UK
- The linear and regression models show low statistical significance given the high p-values.

Finishing Up

```
In [62]:

from subprocess import call
call(['python', '-m', 'nbconvert', 'Analyze_ab_test_results_notebook.ipynb'])

Out[62]:
255

In [1]:
wkhtmltopdf notebook.html notebook.pdf

File "<ipython-input-1-1f9b643067f3>", line 1
    wkhtmltopdf notebook.html notebook.pdf

SyntaxError: invalid syntax

In [3]:
./nbconvert.py --format=pdf analysis.ipynb
```