

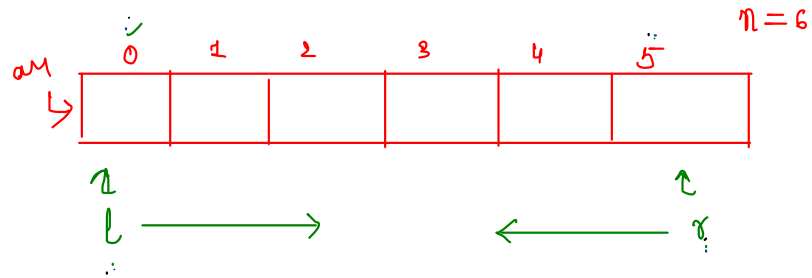
Sprint-3 [Day-2]

→ variable (i, j, ...)

Two - Pointer Technique → Applied on Arrays/strings

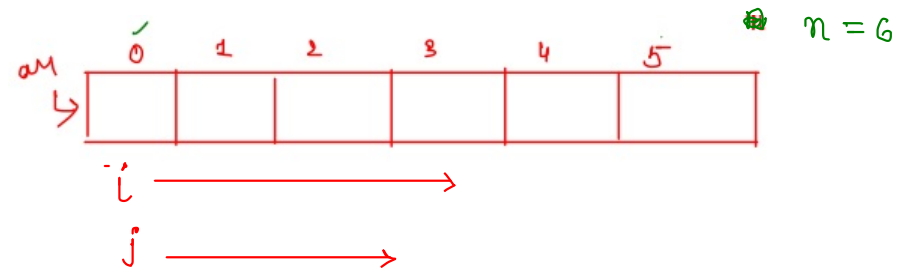
Type-1 ✓

> 2ptr's move's in "opposite" direction



Type-2

> 2ptr's move's in same direction



Two Pointer [Model-1 : Moves in Opposite Direction]

1) Find a pair whose sum is equal to k [$a+b=k$]

i/p

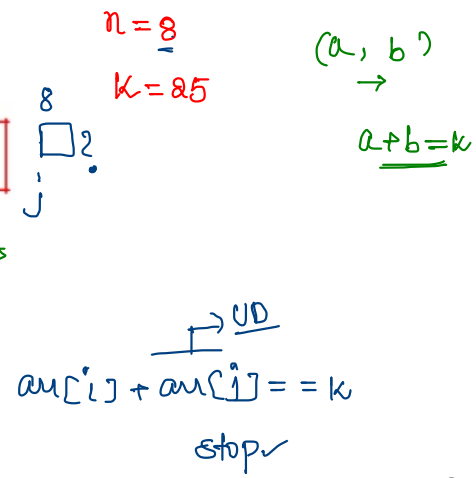
	0	1	2	3	4	5	6	7
arr ↓	7	4	9	6	21	8	11	17

$$n = 8 \checkmark$$

$$k = \underline{25} \checkmark$$

$$4 + 21 = 25 \quad (T)$$

$$8 + 17 = 25$$


$$7 + \underset{\uparrow}{(18)} = 25$$

$$i = 0 \Rightarrow 0 - 1$$

$$j = 1$$

$$arr[i] + arr[j] = k$$
 stop ✓

$$j = i + 1$$

```

* function fun(arr,n,k)
{
    for(i=0;i<=n-2;i++)
    {
        for(j=i+1;j<=n-1;j++)
        {
            if(arr[i]+arr[j]==k)
                return true
        }
    }
    return false
}

```

Handwritten annotations in red:

- Next to the function signature: $\Rightarrow T.C : O(n^2)$
- A horizontal double-headed arrow above the inner loop, with a downward arrow pointing to $T.C$ below it.
- A vertical double-headed arrow to the left of the inner loop, with a downward arrow pointing to $T.C$ below it.

```
function fun(arr,n,k)
{
    flag=0
    for(i=0;i<=n-2;i++)
    {
        for(j=i+1;j<=n-1;j++)
        {
            if(arr[i]+arr[j]==k)
                flag=1
        }
    }
    if(flag==1) return true
    else return false
}
```

if $a \leq x$

0	1	2	3	4	5	6	7
7	4	9	6	21	8	11	17

✓ ✓ ✓ ✓ ✓ ✓ ✓

a

0	1	2	3	4	5	6	7
4	6	7	8	9	11	17	21

✓

$$n=8$$

$$a+b=k$$

$$BF: O(n^2) \rightarrow \downarrow T.C$$

$$< n^2$$

$$k = \underline{18} \checkmark$$

$$k=18$$

$$1 - 809 \text{ at } (1) \checkmark$$

$$4 + 21 = \underline{25} > k$$

$$(a[l] + a[r]) > k$$

$l++ \checkmark$ $l=1, r=7$ $6 + 21 = \underline{27} > 18$	$r-- \checkmark$ $l=0, r=6$ $4 + 17 = \underline{21}$
--	---

$$l=2, r=7$$

$$7 + 21 = 28 > 18$$

$$(a[l] + a[r]) \text{ vs } k$$

C_1

$$(a[l] + a[r]) == k$$

Stop

C_2

$$(a[l] + a[r]) < k$$

$$l++$$

C_3

$$(a[l] + a[r]) > k$$

$$r--$$

ip \rightarrow arr

0	1	2	3	4	5	6	7
7	4	9	6	21	8	11	17
✓	✓	✓	✓	✓	✓	✓	✓

a

0	1	2	3	4	5	6	7
4	6	7	8	9	11	17	21
		l			r		

$$n=8 \quad a+b=k$$

$$k = \underline{18} \checkmark$$

1-8094(L) ✓

$$4+21=25 > 18 \rightarrow r--$$

$$4+17=21 > 18 \rightarrow r--$$

$$4+11=15 < 18 \rightarrow l++$$

$$6+11=17 < 18 \rightarrow l++$$

$$7+11=18 == 18 \checkmark$$

$$(a[l] + a[r]) \text{ vs } k$$

c_1

$$(a[l] + a[r]) == k$$

Stop.

c_2

$$(a[l] + a[r]) < k$$

$l++$

c_3

$$(a[l] + a[r]) > k$$

$r--$

```
function fun(arr,n,k)
{
```

✓ arr.sort(function(a,b){return a-b}) $\Rightarrow n \cdot \log_2^n$

l=0,r=n-1;

* while(l<r) $\Rightarrow n$

{

if(arr[l]+arr[r]==k)

return true;

else if(arr[l]+arr[r]>k)

r--;

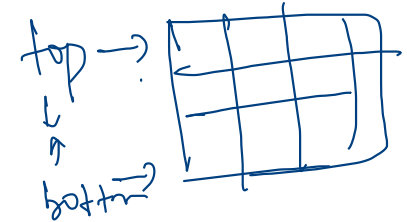
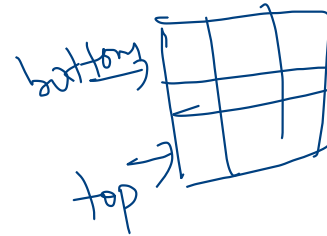
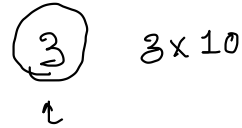
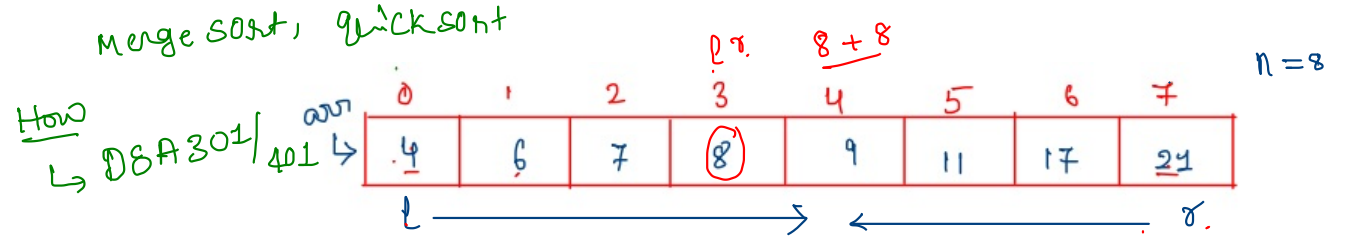
else // arr[l]+arr[r]<k

l++;

}

return false;

}



$\frac{n \cdot \log_2^n + n}{2}$

max: $O(n \log_2^n)$

n \rightarrow change bound

$l < r$ $l \leq r$

Ap₁ :- BF

$O(n^2)$

Ap₂ :- 2ptn (Type-1)

$O(n \log_2 n)$ ✓

Ap₃

if array is
already sorted

$O(n)$ ✓

3) Separate 0's and 1's



ip

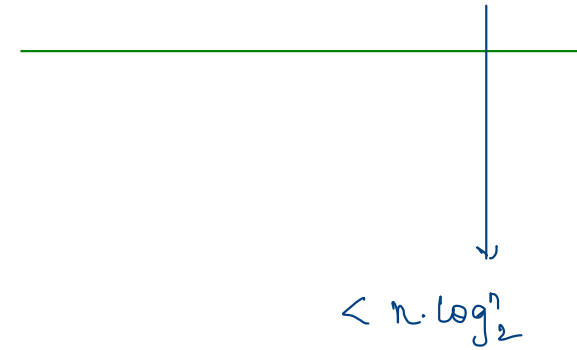
0	1	2	3	4	5	6	7	8	9	10	11	12
1	1	0	0	0	1	1	0	0	1	0	0	0

op

0	1	2	3	4	5	6	7	8	9	10	11	12
0	0	0	0	0	0	0	0	1	1	1	1	1

Apz:-

Sorting $\Rightarrow O(n \cdot \log_2 n)$



AP₂

018
L →

i	0	1	2	3	4	5	6	7	8	9	10	11	12
	1	1	0	0	1	1	0	0	1	0	0	0	0

Zero = [] ✓ \Rightarrow $n-1$ (0)

One = [] ✓ \Rightarrow 1 (n)

n = 13

12 (0) 11 (1)

T.C :- $O(n)$

S.C :- $O(n)$ ✓

AP₁

AP₂

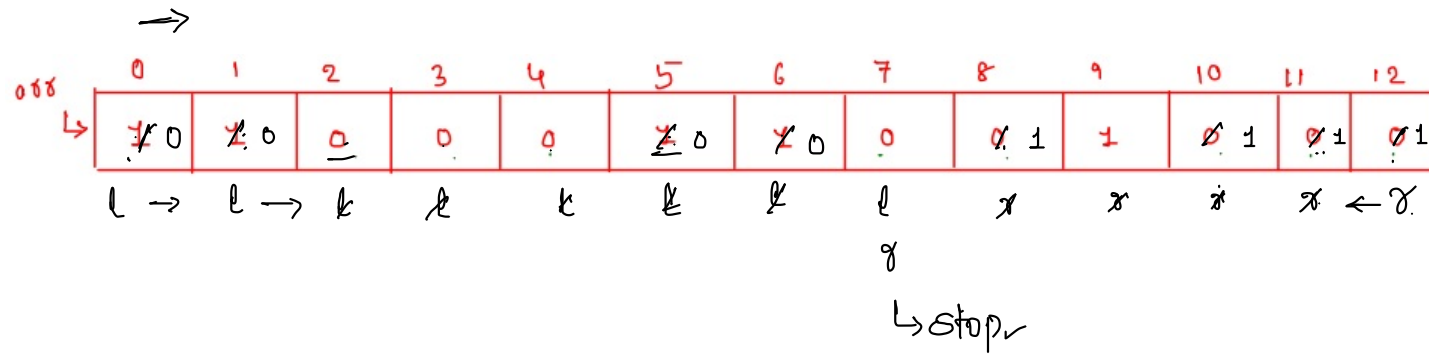
AP₃

T.C :- $O(n \log_2 n)$ \rightarrow $O(n)$

S.C :- $O(1)$ \rightarrow $O(n)$

$O(n)$

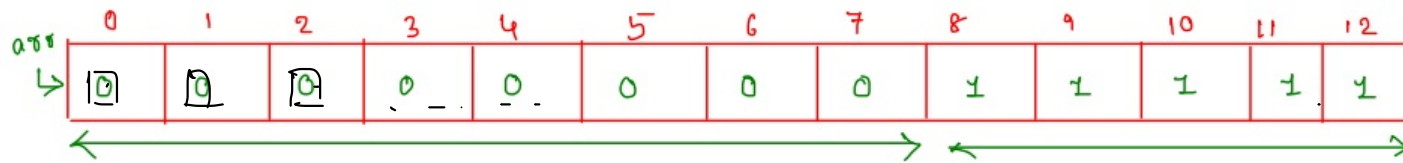
\downarrow 2 ptr
 $O(1)$



2ptr (Type-1)

When you
see 0 $\Rightarrow l++$

When you
see 1 $\Rightarrow r--$



o/p

//input is always : either 0/1

function fun(arr,n)

{

l=0,r=n-1;

while(l<r)

while(arr[l]==0 && l<r)

{

l++;

}

while(arr[r]==1 && l<r)

{

r--;

}

if(l<r)

{

temp=arr[l];

arr[l]=arr[r];

arr[r]=temp;

l++;

r--;

}

}

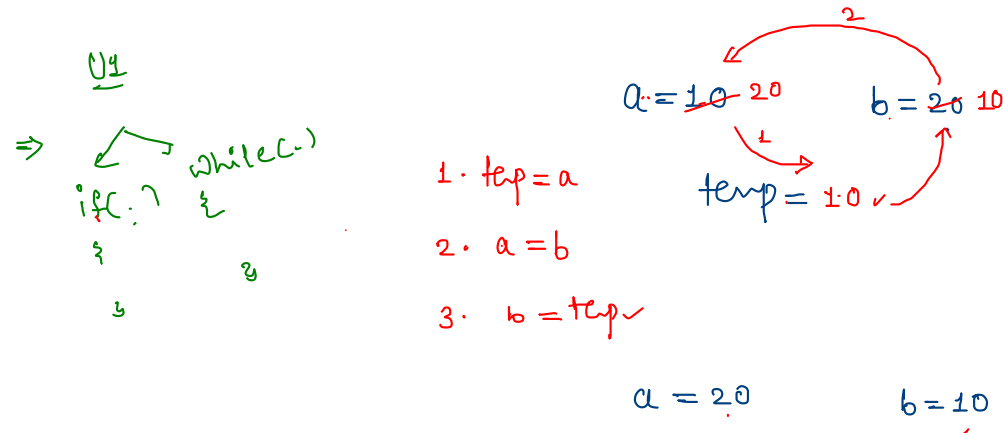
return arr;

}

arr

0	1	2	3	4	5	6	7	8	9
0	0	1	0	1	1	0	0	1	1
k	k	l					g	g	g

n=10



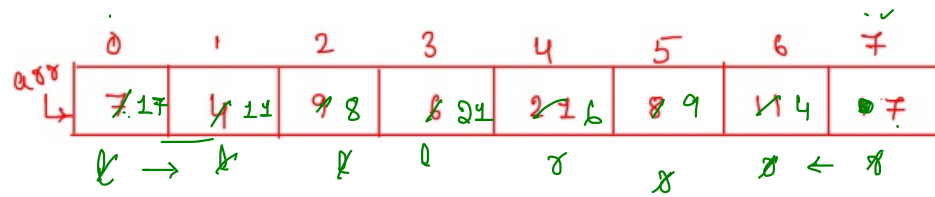
arr

0	1	2	3	4	5	6	7	8	9
0	0	0	0	0	0	0	0	0	0
g	g	g	g						g

$\rightarrow O(1)$ space

$n=7$

4. Reverse the array [in-place]



$n=8$

$O(n)$: time

$O(1)$: space ✓

$l=0, r=n-1$

while($l < r$)

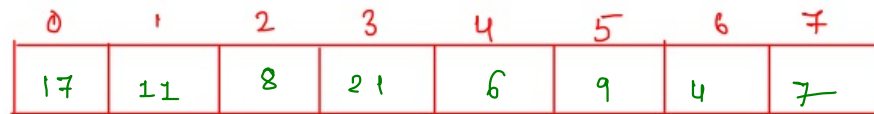
{

 swap($a[l], a[r]$)

$l++$

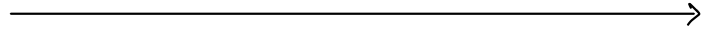
$r--$

}



$\Rightarrow \text{rev}(arr)$

Two Pointer [Model-2 : Same Direction]



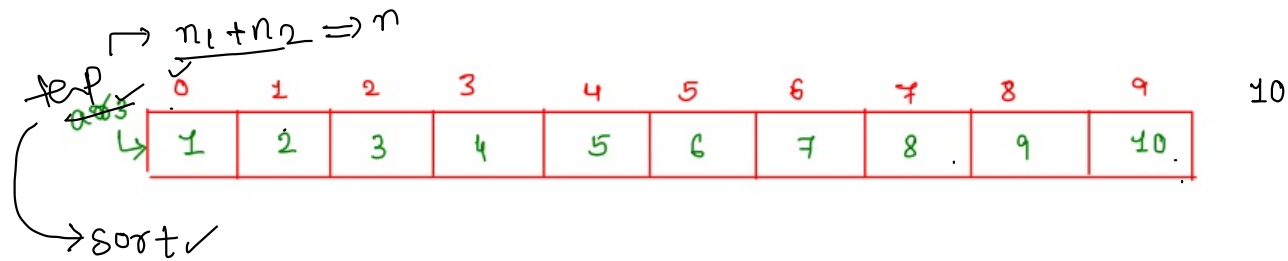
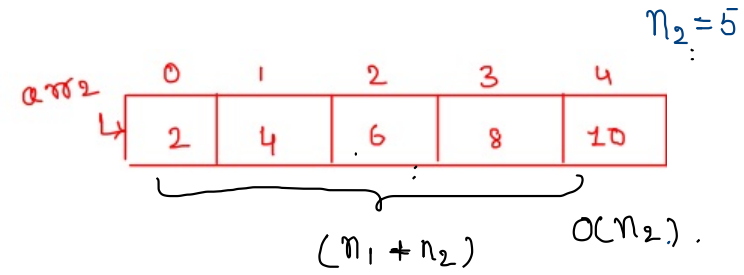
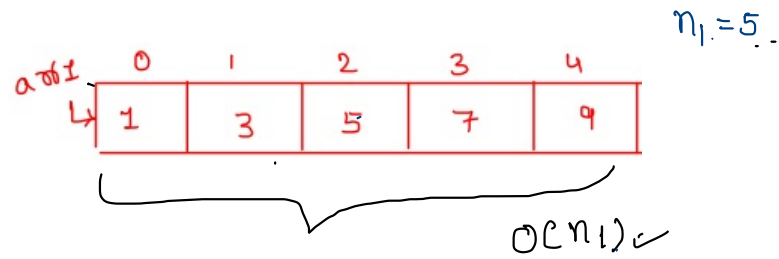
$i \rightarrow$

$j \rightarrow$

n_1 & n_2 can be same / different

5) Merge Two Sorted Arrays :-

$$n = n_1 + n_2$$



n_1 ✓

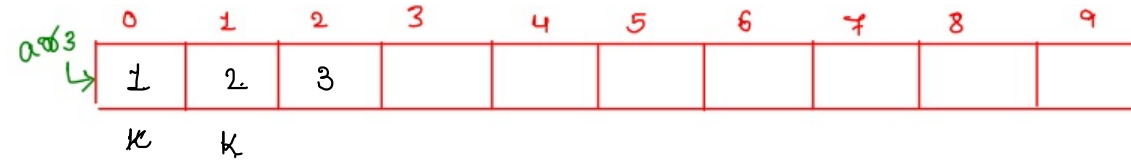
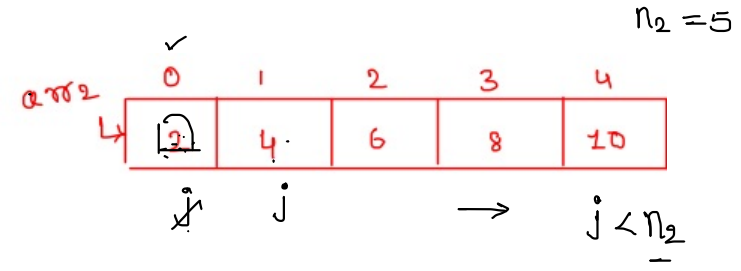
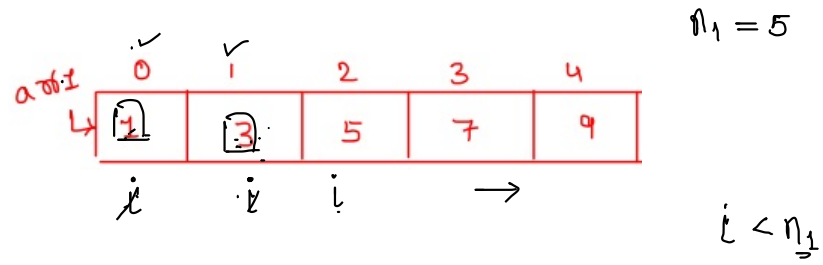
$\rightarrow T.C;$

n_2 ✓

$n \cdot \log_2$ ✓

$$\Rightarrow O((n_1 + n_2) \cdot \log_2(n_1 + n_2)) : T.C$$

$$O(n) : S.C$$

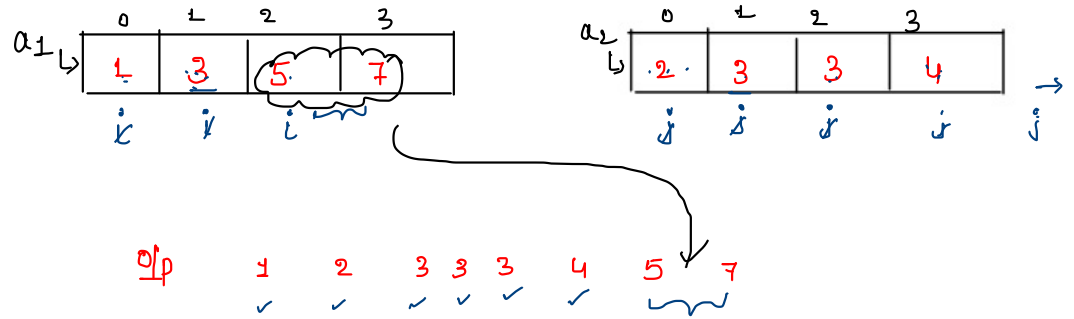


$$i = 0, j = 0, k = 0$$

$$\underline{a_1[i] \vee a_2[j]}$$

```
function fun(arr1,arr2,n1,n2)// n1 is size of arr1 and n2 is size of arr2
```

```
{  
    i=0,j=0,k=0  
    let arr3=new Array(n1+n2);  
    → while(i<n1 && j<n2)  
    {  
        ✕ ✕ if(arr1[i]<arr2[j])  
        {  
            arr3[k]=arr1[i];  
            i++;  
            k++;  
        }  
        ✓ else  
        {  
            arr3[k]=arr2[j];  
            j++;  
            k++;  
        }  
    }  
}
```




```

function fun(arr1,arr2,n1,n2)// n1 is size of arr1 and n2 is size of arr2
{
    i=0,j=0,k=0
    ✎ let arr3=new Array(n1+n2);
    ✓ while(i<n1 && j<n2)
    {
        if(arr1[i]<arr2[j])
        {
            arr3[k]=arr1[i];
            i++;
            k++;
        }
        else
        {
            arr3[k]=arr2[j]
            j++;
            k++;
        }
    }
    while(i<n1)
    {
        arr3[k]=arr1[i];
        i++;
        k++;
    }
    while(j<n2)
    {
        arr3[k]=arr2[j];
        j++;
        k++;
    }
    return arr3;
}

```

```

function fun(arr1,arr2,n1,n2)// n1 is size of arr1 and n2 is size of arr2
{
    i=0,j=0,k=0
    let arr3=new Array(n1+n2);
    while(count<(n1+n2))
    {
        if(i<n1 && arr1[i]<arr2[j] )
        {
            arr3[k]=arr1[i];
            i++;
            k++;
            count++
        }
        else if(arr1[j]>arr2[j] && i<n1 && j<n2)
        {
            arr3[k]=arr2[j]
            j++;
            k++;
        }
        else
        {
            arr3[k]=arr2[j]
            j++;
            k++;
        }
    }
    j++;
    k++;
}
return arr3;
}

```


6) Remove Duplicates from Sorted array

arr \Rightarrow

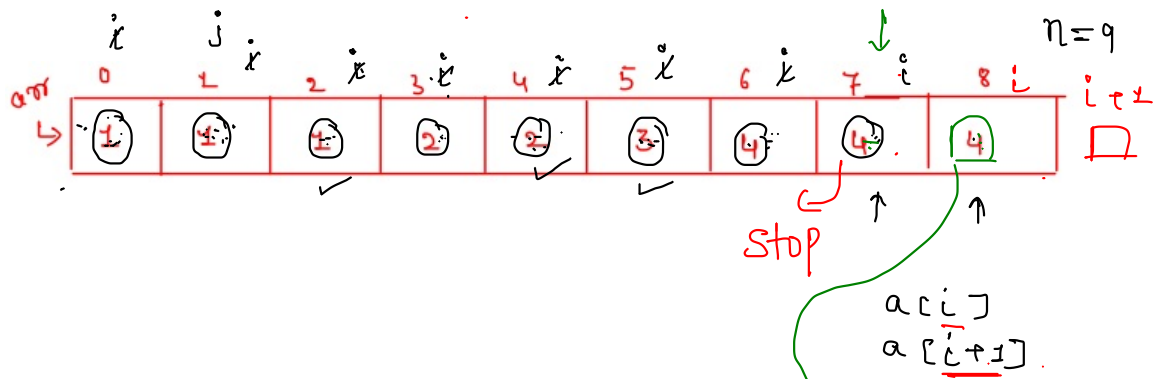
0	1	2	3	4	5	6	7	8
1	1	1	2	2	3	4	4	4

 $n=9$ \Rightarrow ~~arr~~ 1 2 3 4

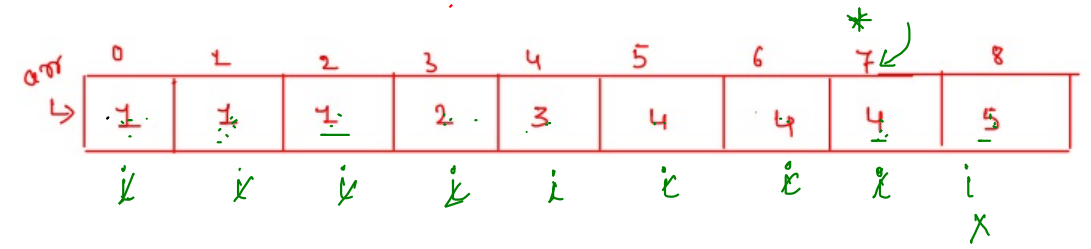
arr \Rightarrow

0	1	2	3	4	5	6	7	8
1	1	1	2	3	4	4	4	5

 \Rightarrow ~~arr~~ 1 2 3 4 5



$\text{temp}[9] \Rightarrow [1, 2, 3, 4]$



$\text{temp}[] = \{1, 2, 3, 4, 5\}$ ✓

```
function removeDuplicates(arr, n)
{
    let temp = new Array(n)
    for(i=0; i<=n-2; i++)
    {
        if(arr[i] != arr[i+1])
        {
            temp.push(arr[i])
        }
    }
    temp.push(arr[n-1]);
    return temp;
}
```

T.C: $O(n)$

S.C: $O(n)$

$\Rightarrow O(n) \checkmark$
 $+ O(1) \cdot S.C$
 Assignment

Object

$\hookrightarrow T.C: O(n)$

S.C: $O(n)$

$\hookrightarrow delete()$

arr

↳

0	1	2	3	4	5	6	7	8
1	1	1	2	2	3	4	4	4

arr

↳

0	1	2	3	4	5	6	7	8
1	1	1	2	3	4	4	4	5

☐ Test against custom input

Run Code

Submit

a_1 \rightarrow i \rightarrow i $n_1 = 5$
 \hookrightarrow $\textcircled{1}$ 2 3 4 5

a_2 \hookleftarrow j \leftarrow j $n_2 = 5$
 4 3 2 1 $\textcircled{1}$

count = 0

while $i \leq n_1 - 1$ & $j > 0$

{

if $(a_1[i] == a_2[j])$

{ count++

$i++$, $j--$

}

$a_1[i] < a_2[j]$

$\hookrightarrow j--$

else ~~$a_1[i] > a_2[j]$~~

$\hookrightarrow i++$

^