



UNIVERSITÀ
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ARCHITECTURE MODEL AND ANALYSIS OF CYBER PHYSICAL SYSTEMS

(PART II – MODELLING AND ANALYSIS OF CYBER PHYSICAL SYSTEMS)

Submitted to Professor Paolo Lollini

Project: Modelling and Evaluation of Failure-Repair System

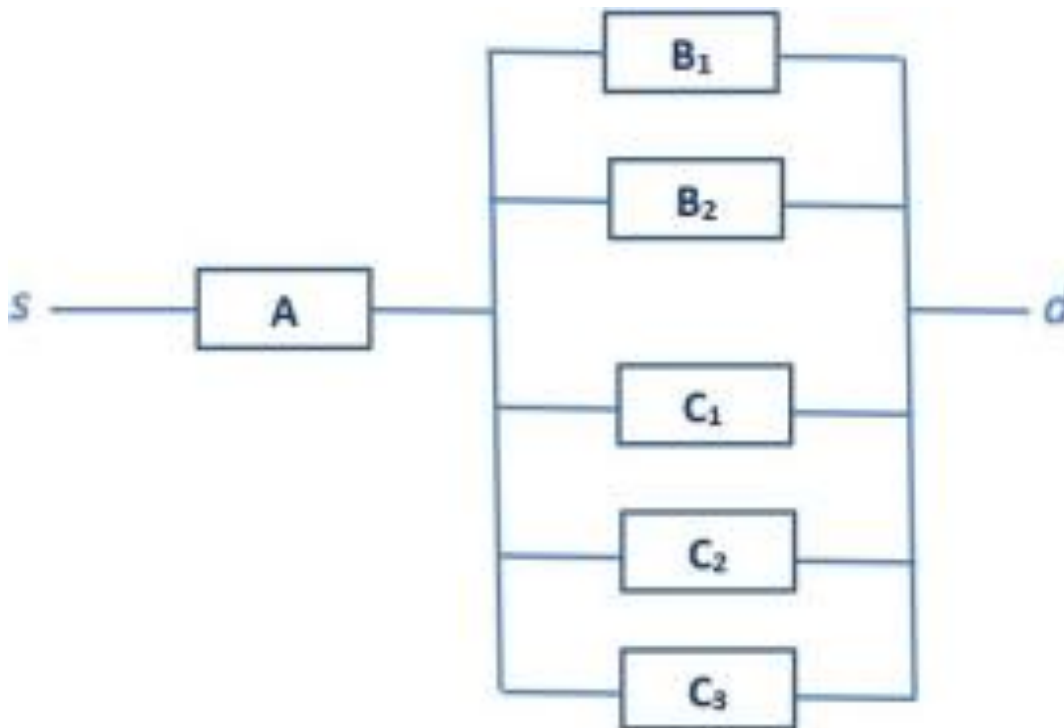
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1.Problem: The objective is to analyse, to model and evaluate the system. To compute the Reliability and Availability of the given system using the Transient Solver.

2.Assumptions & Solutions: We did model and evaluation exercises for analysing the system operations, working, failures and repair using Mobius.

Mobius: Mobius is a software tool for modelling the behaviour of complex systems. Developed for studying the Reliability, Availability, and Performance of Network/Computer systems.

3.System to Analyse:



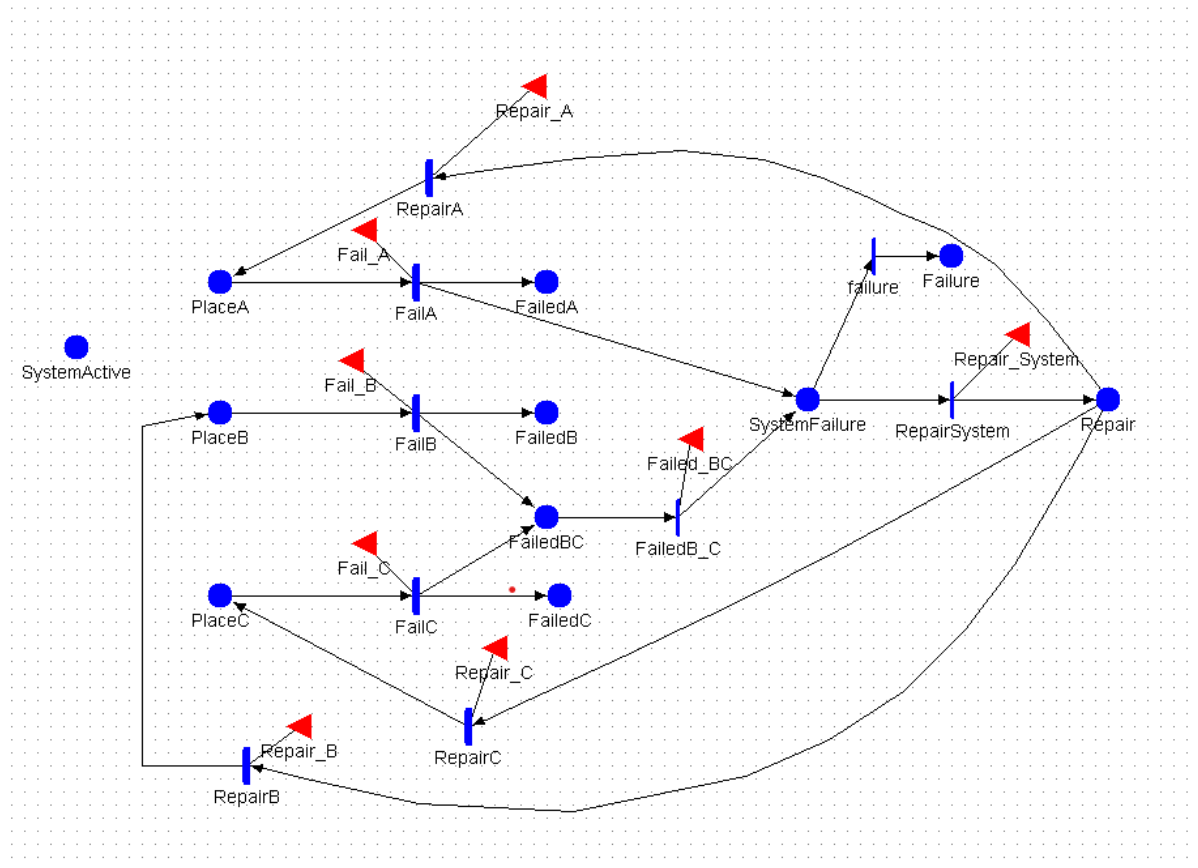
4.System Configuration: R1-O1-W1

Option (R1) : the units cannot be repaired until the whole system fails (i.e., there is no path between s and d).

Option (O1) : repairs are carried out sequentially (one after the other), respecting the following order: first A, then B1, B2 and finally C1, C2, C3.

Option (W1) : the failed system re-starts working as soon as there again a path between s and d; the failed system re-starts working as soon as there again a path between s and d.

5. Model Description



Initial Markings:

- 3 Token in PlaceC
- 2 Token in PlaceB
- 1 Token in PlaceA
- 1 Token in SystemActive
- 0 Token in other place's

Rate of Failure Activities:

- PlaceA Failure: $\lambda * (\text{PlaceA} \rightarrow \text{Mark}()) / 4.0$
- PlaceB Failure: $\lambda * (\text{PlaceB} \rightarrow \text{Mark}()) / 2.0$
- PlaceC Failure: $\lambda * (\text{PlaceC} \rightarrow \text{Mark}())$

Rate of Repair Activities:

- PlaceA Repair: $\mu / 4.0$
- PlaceB Repair: $\mu / 2.0$
- PlaceC Repair: μ

Global Variables

Add
short

Name	Type
lamda	double
mu	double

Delete

Close

- Failure Activity fire, 1 token is removed from PlaceA/B/C, 1 is added to FailedA/B/C, this token is consumed when the repairing activity fires. Later token is added back to PlaceA/B/C.
- When FailedA has 1 token it directly goes to SystemFailure. And when FailedBC has 2 tokens (1 from FailedB & 1 FailedC) it goes to SystemFailure continuously system will stop working.
- We have a system failure when FailedA fires or when FailedB_C has 5 tokens, after that 1 token is added to Failure_Memory (only the first time), used to calculate Reliability.
- The input gates Repair_A/B/C allow component repairing only if the places FailedA/B/C contain at least one token, and the units that have a priority no longer have a token in FailedA/B/C.
- Activity Repair gets fired only when FailedA/B/C no longer contains tokens and the repair takes place in a sequential order A, B then C.

Reward Variable:

1.Availability (Steady State Checking): The Reward function returns 1 if "SystemWorking" has 1 token.

Performance Variables
Model

(Enter new variable name)

Add Variable:

Variable List

Availability
Reliability

Variable Name: Availability

Submodels
Rate Rewards
Impulse Rewards
Time
Simulation

Available State Variables (double click to insert)

Repair->PlaceA
Repair->PlaceB
Repair->PlaceC
Repair->FailedA
Repair->FailedB
Repair->FailedC
Repair->Repair
Repair->SystemFailure
Repair->FailedBC

Reward Function

```
if(Repair->SystemActive-> Mark()>0) return 1;
```

2.Reliability: Reward Function return 1 if “Failure” has 1 token. This indicates that system failed at the first time.

Performance Variables | Model

(Enter new variable name)

Add Variable:

Variable List

- Availability
- Reliability**

Variable Name: Reliability

Submodels | Rate Rewards | Impulse Rewards | Time | Simulation

Available State Variables (double click to insert)

- Repair->PlaceA
- Repair->PlaceB
- Repair->PlaceC
- Repair->FailedA
- Repair->FailedB
- Repair->FailedC
- Repair->Repair
- Repair->SystemFailure
- Repair->FailedBC

Reward Function

```
if (1>Repair->Failure->Mark())return 1;
```

Time Range :

Variable Name: Reliability

Submodels | Rate Rewards | Impulse Rewards | Time | Simulation

Type: Instant of Time

Time Point definition method: Manual Range

Number of Time Measurements: 6

Time Measurement	Start Time:
1	32
2	280
3	1200
4	2460
5	5240
6	10520

Transformers:

first run a state-space generator on the model to build a representation of the stochastic process underlying the model and then use a transient solver to compute the measures.

File Edit Help

SSG Info SSG Output

Study Name: Study

Experiment List: Experiment_1, Experiment_2, Experiment_3, Experiment_4, Experiment_5

Run Name: Results

Build Type: Optimize

Trace Level: Level 0: None

Hash Value: 0.5

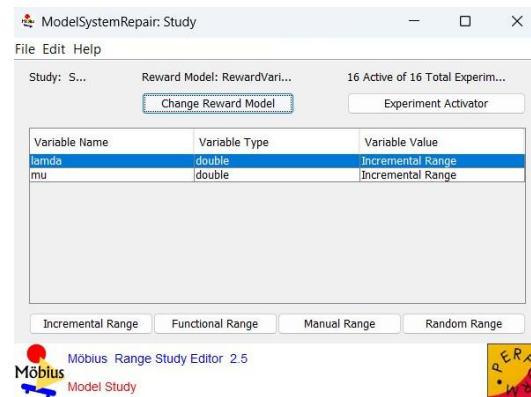
☐ Flag Absorbing States

☐ Place Comments in Output

Start State Space Generation

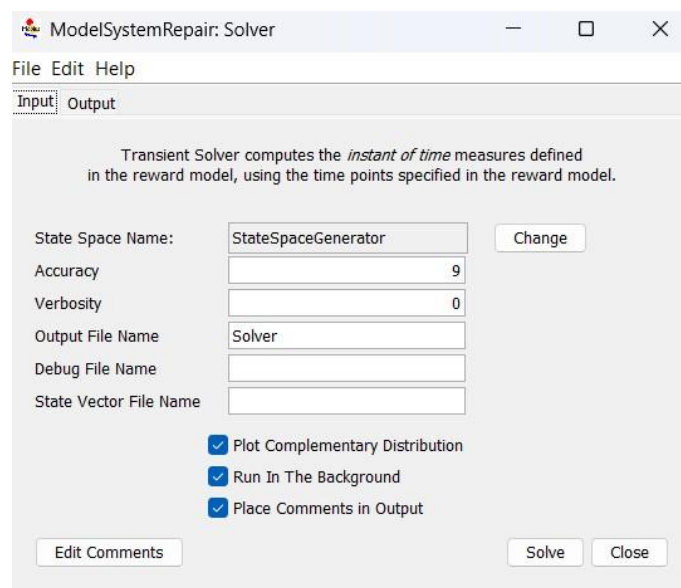
Study:

Once we have done with modelling, we need to check the behaviour of the system for different parameter values and number of experiments.



Transient Solver:

The transient solver (TRS) solves for instant-of-time variables with $t < \infty$ using randomization. It calculates the mean and variance of each performability variable for the time points defined for the reward variable within the reward model.

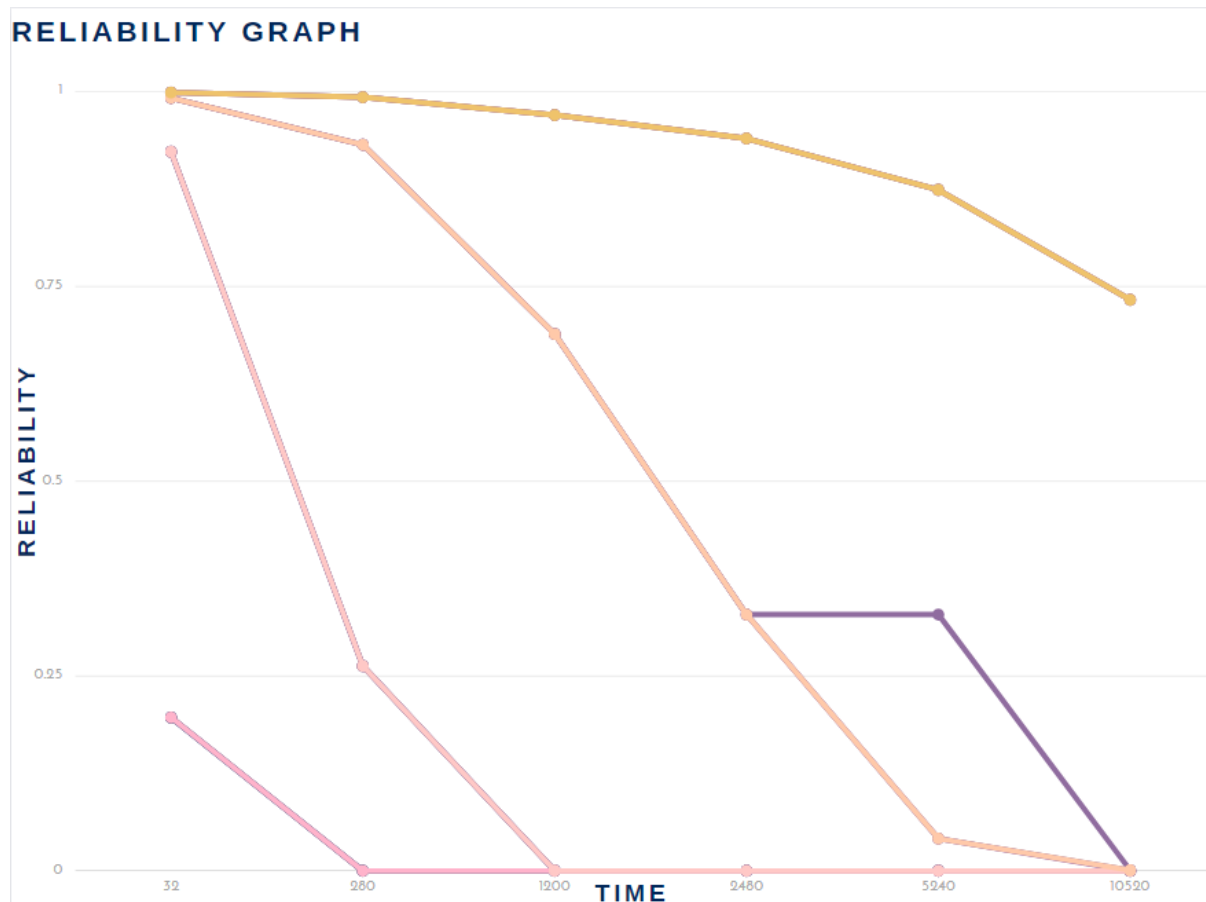


7. Analysis of System

Probability of Continuous Operation:

The probability that the system remains continuously operational in the interval $[0; t]$ is influenced by the failure rates λ and the repair rates μ . As the failure rate decreases (lower values of λ), the system's overall reliability improves. Similarly, higher repair rates (greater values of μ) lead to quicker recovery after a failure. Consequently, by adjusting these parameters, you can enhance the system's continuous operation probability.

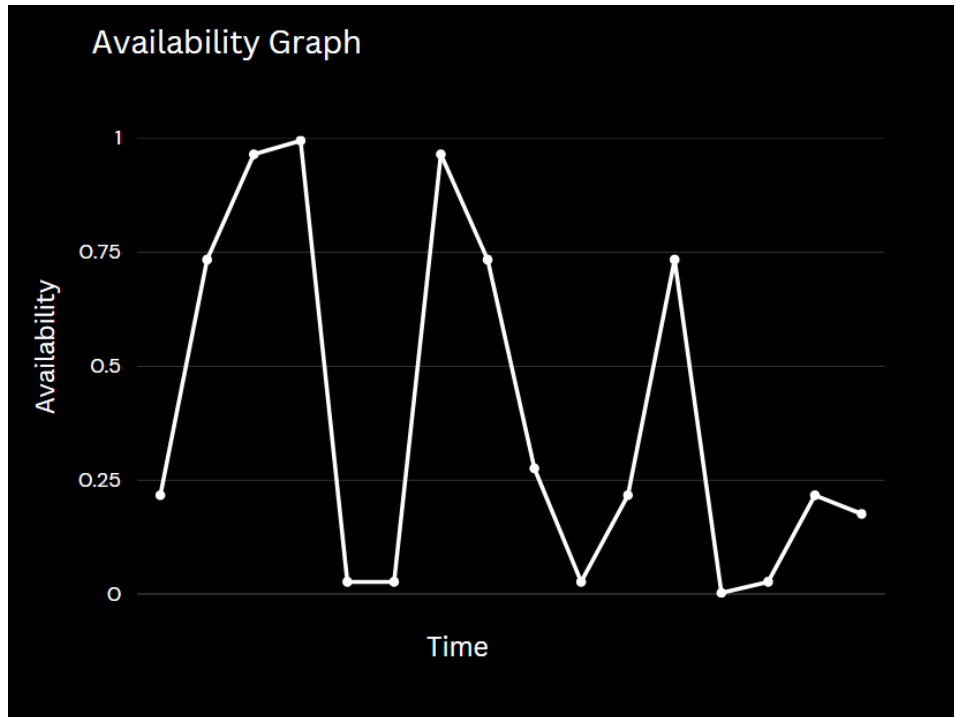
Reliability Matrix							
Experiments	Time Point						
	32	280	1200	2480	5240	1520	
Experiment_1	1.97E-01	1.52E-09	1.64E-39	3.10E-81	3.34E-172	0.00E+00	
Experiment_2	9.23E-01	2.63E-01	2.47E-04	1.67E-08	1.71E-17	1.08E-34	
Experiment_3	9.92E-01	9.32E-01	6.89E-01	3.29E-01	4.15E-02	7.53E-04	
Experiment_4	9.99E-01	9.93E-01	9.70E-01	9.40E-01	8.74E-01	7.33E-01	
Experiment_5	1.97E-01	1.52E-09	1.64E-39	3.10E-81	3.34E-172	0.00E+00	
Experiment_6	9.23E-01	2.63E-01	2.47E-04	1.67E-08	1.71E-17	1.08E-34	
Experiment_7	9.92E-01	9.32E-01	6.89E-01	3.29E-01	3.29E-01	7.53E-04	
Experiment_8	9.99E-01	9.93E-01	9.70E-01	9.40E-01	8.74E-01	7.33E-01	
Experiment_9	1.97E-01	1.52E-09	1.64E-39	3.10E-81	3.34E-172	0.00E+00	
Experiment_10	9.23E-01	2.63E-01	2.47E-04	1.67E-08	1.71E-17	1.08E-34	
Experiment_11	9.92E-01	9.32E-01	6.89E-01	3.29E-01	4.15E-02	7.53E-04	
Experiment_12	9.99E-01	9.93E-01	9.70E-01	9.40E-01	8.74E-01	7.33E-01	
Experiment_13	1.97E-01	1.52E-09	1.64E-39	3.10E-81	3.34E-172	0.00E+00	
Experiment_14	9.23E-01	2.63E-01	2.47E-04	1.67E-08	1.71E-17	1.08E-34	
Experiment_15	9.92E-01	9.32E-01	6.89E-01	3.29E-01	4.15E-02	7.53E-04	
Experiment_16	9.99E-01	9.93E-01	9.70E-01	9.40E-01	8.74E-01	7.33E-01	



Steady-State Availability:

The steady-state availability of the system is a measure of how often the system is operational over the long term. It accounts for both failures and repairs. In this scenario, since repairs are carried out sequentially after a total system failure, the steady-state availability is determined by the sum of the operational times and the repair times. As the failure rates decrease and the repair rates increase, the steady-state availability of the system improves, indicating better overall system reliability and readiness.

Availability Matrix			
Global Variable		Time Measurement	
lambda	mu	Steady State	
0.1	0.1	2.17 e-1	
0.01	0.1	7.34 e-1	
0.001	0.1	9.65 e-1	
1.00E-04	0.1	9.95 e-1	
0.1	0.01	2.69 e-2	
0.01	0.01	2.70 e-2	
0.001	0.01	9.65 e-1	
1.00E-04	0.01	7.34 e-1	
0.1	0.001	2.76 e-1	
0.01	0.001	2.70 e-2	
0.001	0.001	2.17 e-1	
1.00E-04	0.001	7.34 e-1	
0.1	1.00E-04	2.76 e-3	
0.01	1.00E-04	2.69 e-2	
0.001	1.00E-04	2.17 e-1	
1.00E-04	1.00E-04	1.76 e-1	



Conclusion

We evaluated the reliability of a critical system under the unique conditions of Options R1, O1, and W1 during this project. In this case, we focused on restoring the system one step at a time, beginning with A, then B1, B2, and lastly C1, C2, and C3. It should be noted that repairs could only begin if the entire system failed, and the system would restart operating once a path between its source and destination was restored.

These findings highlight the need of designing systems with efficient repair strategies and considering the relation between failure and repair rates in order to improve overall system dependability and availability.

In conclusion, this project shows the importance of careful system design and repair planning. It highlights the importance of dependable systems in today's society and how dependability analysis helps to ensure their success. This project's results not only improve our academic understanding but also help us better manage and improve the systems that support our society. This effort shows how theory and practical implementation may improve the way we interact directly.