

# Historical biogeography using data augmentation in RevBayes

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## 1 Introduction

This lab describes how to perform Bayesian inference of historical biogeography using RevBayes. The analysis jointly infers the posterior range evolution parameters and ancestral ranges using the data augmentation approach described in Landis et al. (2013). To examine the posterior, we'll use Python scripts, Tracer by Andrew Rambaut, to summarize MCMC output files, and Phylowood, a Javascript web service that animates and filters phylogenetic biogeography reconstructions (Landis and Bedford 2014).

## Outline

### I. Introduction

- a) Workspace setup
- b) Range evolution models and data augmentation

### II. DEC in RevBayes

- a) Tree, range, and geographic input
- b) DEC as a graphical model
- c) Monitors, moves, and MCMC
- d) Model selection with Bayes factors

### III. Output and Analysis

- a) MCMC output in Tracer
- b) Ancestral range output
- c) Animate ancestral ranges

→ These little arrows indicate lines containing key information to progress through the lab. The rest of the text gives context for why we're taking these steps or what to make of results.

## 1.1 Handy links for this lab

RevBayes	<a href="https://github.com/revbayes/revbayes">https://github.com/revbayes/revbayes</a>
Lab zip file	<a href="https://github.com/revbayes/revbayes/.../RB_biogeo_files.zip">https://github.com/revbayes/revbayes/.../RB_biogeo_files.zip</a>
Phylowood software	<a href="http://mlandis.github.io/phylowood">http://mlandis.github.io/phylowood</a>
Phylowood manual	<a href="https://github.com/mlandis/phylowood/wiki">https://github.com/mlandis/phylowood/wiki</a>
Tracer	<a href="http://tree.bio.ed.ac.uk/software/tracer">http://tree.bio.ed.ac.uk/software/tracer</a>

## 1.2 Setting up your workspace

The practical part of the lab will analyze a small dataset of 19 taxa distributed over 4 biogeographic areas. Parts of the lab will require entering terminal commands, which will assume you are using the Unix shell `bash`. Just ask for help if the commands don't seem to work.

- Portions of this lab require Python is installed. No packages are needed.
- This tutorial will assume you have successfully installed RevBayes and can be called from your current working directory.
- Download and unzip the lab zip file, `RB_biogeo_files.zip`.

## 2 Model and method

This section contains a brief description of the data, model, parameters, and method used in BayArea.

First, we define the range for taxon  $i$  as the bit vector  $X_i$ , where  $X_{i,j} = 1$  if the taxon is present in area  $j$  and  $X_{i,j} = 0$  if the taxon is absent. Each taxon range is a bit vector of length  $N$  areas. For example, if taxon  $B$  is present only in areas 2 and 3 out of  $N = 3$  areas, its range is represented as  $X_B = (0, 1, 1)$ , which is translated to the bit string  $X_B = 011$  for short. The data matrix,  $\mathbf{X}$ , is analogous to a multiple sequence alignment where each element in the data matrix reports a discrete value for a homologous character shared by all taxa at column  $j$ .

Next, we need a model of range evolution. Since we have discrete characters we'll use the continuous-time Markov chain, which allows us to compute transition probability of a character changing from  $i$  to  $j$  in time  $t$  through matrix exponentiation

$$\mathbf{P}_{i,j}(t) = [\exp \{ \mathbf{Q}t \}]_{i,j},$$

where  $\mathbf{Q}$  is the instantaneous rate matrix defining the rates of change between all pairs of characters, and  $\mathbf{P}$  is the transition probability rate matrix. This technique of matrix exponentiation is powerful because it integrates over all possible scenarios of character transitions that could occur during  $t$  so long as the chain begins in state  $i$  and ends in state  $j$ .

We can then encode range evolution events into the allowed character transitions of  $\mathbf{Q}$  and parameterize the events so that we may infer their relative importance to generating our observed ranges. We'll take a simple model of range expansion (e.g.  $011 \rightarrow 111$ ) and range contraction (e.g.  $011 \rightarrow 001$ ). (Range expansion may also be referred to as dispersal or area gain and range contraction as extirpation or area loss.) The rates in the transition matrix for three areas might appear as

	000	001	010	011	100	101	110	111
$\mathbf{Q} =$	000	—	0	0	0	0	0	0
	001	$\lambda_0$	—	0	$\lambda_1$	0	$\lambda_1$	0
	010	$\lambda_0$	0	—	$\lambda_1$	0	0	$\lambda_1$
	011	0	$\lambda_0$	$\lambda_0$	—	0	0	$\lambda_1$
	100	$\lambda_0$	0	0	0	—	$\lambda_1$	$\lambda_1$
	101	0	$\lambda_0$	0	0	$\lambda_0$	—	0
	110	0	0	$\lambda_0$	0	$\lambda_0$	0	—
	111	0	0	0	$\lambda_0$	0	$\lambda_0$	—

where  $\lambda_1$  and  $\lambda_0$  are the rates of area gain and loss, respectively. This matrix can be represented compactly as the rate function

$$q_{\mathbf{y},\mathbf{z}}^{(a)} = \begin{cases} \lambda_0 & \text{if } z_a = 0 \\ \lambda_1 & \text{if } z_a = 1 \\ 0 & \mathbf{y} \text{ and } \mathbf{z} \text{ differ in more than one area} \end{cases}.$$

where  $\mathbf{y}$  and  $\mathbf{z}$  are the “from” and “to” ranges and  $a$  is the area that changes. For example,  $q_{011,111}^{(1)}$  is the rate of range expansion for  $011 \rightarrow 111$  to gain area 1. Note the rate of more than one event occurring simultaneously is zero, so a range must expand twice by one area in order to expand by two areas. This model is analogous to the Jukes-Cantor model for three independent characters with binary states, except the all-zero “null range” is forbidden.

Lastly, we may reasonably expect that a range expansion event into an area depends on which nearby areas are currently inhabited, which imposes non-independence between characters. The transition rate might then appear as

$$q_{\mathbf{y},\mathbf{z}}^{(a)} = \begin{cases} \lambda_0 & \text{if } z_a = 0 \\ \lambda_1 \eta(\mathbf{y}, \mathbf{z}, a, \beta) & \text{if } z_a = 1 \\ 0 & \mathbf{y} = 00\dots 0 \\ 0 & \mathbf{y} \text{ and } \mathbf{z} \text{ differ in more than one area} \end{cases}.$$

For this tutorial, you can take  $\eta(\cdot)$  to adjust the rate of range expansion into area  $a$  by considering how close it is to the current range,  $\mathbf{y}$  relative to the closeness of all other areas unoccupied by the taxon. The  $\beta$  parameter rescales the importance of geographic distance between two areas by a power law. Importantly,  $\eta(\cdot) = 1$  when  $\beta = 0$ , meaning geographic distance between areas is irrelevant. Moreover, when  $\beta > 0$ ,  $\eta(\cdot) < 1$  when area  $a$  is relatively distant and  $\eta(\cdot) > 1$  when area  $a$  is relatively close.

In addition to dispersal and extinction, the DEC model allows cladogenic range evolution events. For each internal node in the tree, one of four cladogenic events can occur: narrow sympatry, subset sympatry, allopatry, and wide sympatry. Say the range of a species approaching an internal node, i.e. that is about to speciate, is 1000. Since the species range is size one, this always results in narrow sympatry, where both daughter lineages inherit the ancestral species range. Now suppose the ancestral range is 1110. Under subset sympatric cladogenesis, one lineage identically inherits the ancestral species range, 1110, while the other lineage inherits only a single area, e.g. 0100. Under allopatric cladogenesis, the ancestral range is split evenly among daughter lineages, e.g. one lineage may inherit 1100 and the other inherit 0010. Both daughter lineages inherit the entire

ancestral species range following widespread sympatric cladogenic events. For a general description of state transitions for cladogenic events, see Matzke (2013).

The DEC model ignores speciation events hidden by extinction or incomplete taxon sampling and assigns equal probabilities to all cladogenic event types. Since a range of size zero typically means the species is extinct, the probability of cladogenic events would ideally be linked to a birth-death process, as it is in the GeoSSE model (Goldberg et al. 2011). Unfortunately, since this sort of model scales poorly, DEC models remain the only option when the geography has more than two or three areas.

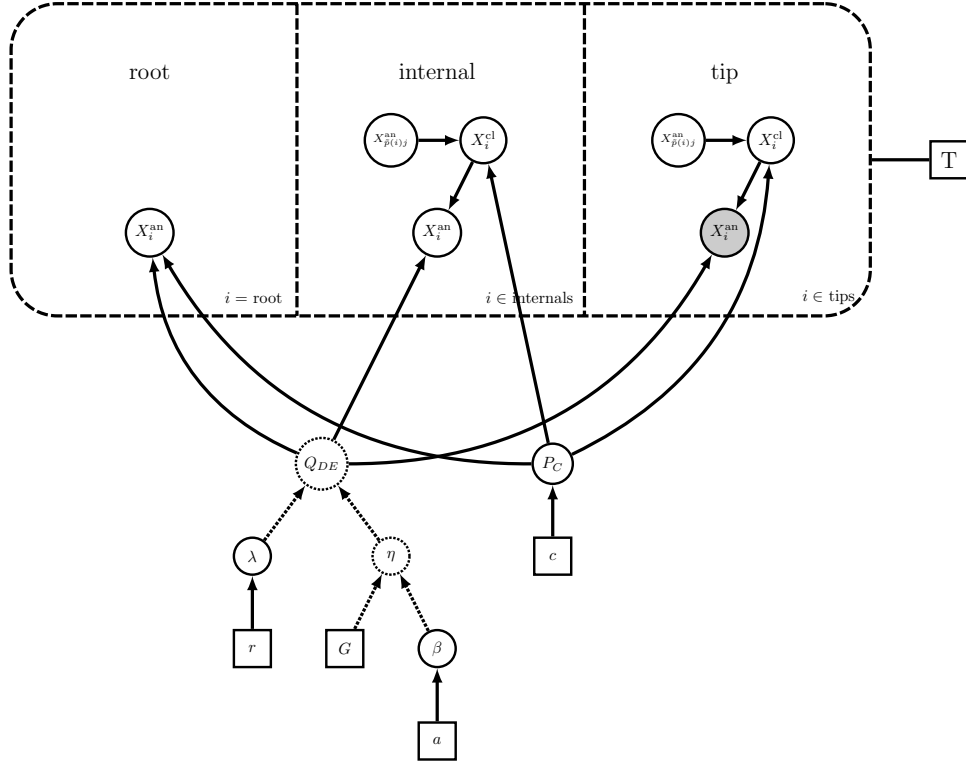


Figure 1: Graphical model of DEC. The tree plate’s topology is fixed by  $T$ , where each internal node has both an anagenic and cladogenic random variable ( $X_i^{\text{an}}$  and  $X_i^{\text{cl}}$ , resp.) that represents an ancestral species before and after it speciated. Anagenic change is modeled by a continuous time Markov process, where  $Q_{DE}$  is the instantaneous rate matrix of area gain and loss, as parameterized by  $\lambda$ . The geographic distance rate modifier function,  $\eta$ , takes in the geographical distances and strata as  $G$ , and the distance power parameter,  $\beta$ . Cladogenic change is modeled by  $P_C$ , a Dirichlet-distributed simplex with a flat prior.

Let’s consider what happens to the size of  $\mathbf{Q}$  when the number of areas,  $N$ , becomes large. For three areas,  $\mathbf{Q}$  is size  $8 \times 8$ . For ten areas,  $\mathbf{Q}$  is size  $1024 \times 1024$ , which approaches the largest size matrix that can be exponentiated in a practical amount of time. This is problematic, meaning we need an alternative method to integrate over historical range evolution events.

You may wonder why matrix exponentiation works fine for molecular substitution models and large multiple sequence alignments. Molecular substitution models typically assume each site in the multiple sequence alignment evolves independently, which may be justified because recombination degrades linkage disequilibrium over geological timescales. Conveniently, this keeps  $\mathbf{Q}$  small even

for datasets with many sites.

Remember matrix exponentiation integrates over all *unobserved* transition events during time  $t$ . The likelihood of beginning in character  $i$  and ending in character  $j$  can be computed easily when the explicit series of event types and times are known. While we will never know the exact history of events, we can use stochastic mapping in conjunction with Markov chain Monte Carlo (MCMC) to repeatedly sample range evolution histories that are consistent with the ranges observed in the study taxa at the tips of the phylogeny. This technique is an adaptation of the data-augmented phylogenetic method first described by Robinson et al. (2003), and was first applied to tertiary structure-dependent evolution of protein-coding nucleotide sequences.

This is the strategy we will use to infer the posterior distribution approximated is  $\text{Prob}(\mathbf{X}_{aug}, \theta \mid \mathbf{X}_{obs}, T, M)$ , where  $\mathbf{X}_{obs}$  is the range data observed at the tips,  $\mathbf{X}_{aug}$  is the distribution of ancestral range reconstructions over the phylogeny,  $T$ , where  $\mathbf{X}_{aug}$  is inferred jointly with the parameters,  $\theta$ , assuming the range evolution model,  $M$ , that describes **Q** above. Ancestral range reconstructions are often of primary interest in phylogenetic biogeographic analyses, which are generated with support values as a by-product of the MCMC analysis.

The rest of this tutorial will describe how to assemble the input, run the analysis, assess the output, and visualize the results.

### 3 Input

For this tutorial, we'll use a dataset for 19 species of *Psychotria* whose range spans the Hawaiian archipelago. The dataset was originally reported in Nepokroeff et al. (2003) and analyzed using the maximum likelihood method, LAGRANGE, by Ree and Smith (2008). We'll use this dataset for three reasons. First, it is relatively small, meaning we can produce results quickly. Second, the Hawaiian archipelago can be broken into naturally discrete areas and has a well-characterized geographical history that is uncomplicated to model. Third, it has previously been analyzed, which provides some basis for comparison to other methods. To simplify things, this model will assume we live in a gentler world where presence-absence characters are known without error.

For larger datasets to play with, see `input/sim_aus_50tip_33area.*` for a simulated model where all cladogenic events were sympatric (wide and narrow only).

#### 3.1 Nexus file

The data file contains a matrix of binary characters corresponding to the observed ranges of the study taxa.

→ Open the file `examples/psychotria_range.txt`.

```
#NEXUS

begin data;
  dimensions ntax=19 nchar=4;
  format datatype=standard symbols = "01";
  matrix
    P_mariniana_Kokee2  1000
    P_mariniana_Oahu    0100
    ...
    P_hexandra_Oahu     0100
  ;
end;

Begin trees;
  TREE tree1 = (((((((P_hawaiiensis_WaikamoiL1:0.9656850499,
P_mauiensis_Eke:0.9656850499):0.7086257935,(P_fauriei2:1.23
0218511,P_hathewayi_1:1.230218511):0.4440923324):0.17671155
...
89):0.4630447802,P_hexandra_Oahu:2.826939991):2.372081244);
End;
```

Range data is stored in standard Nexus format. In the `data` block, the first line gives the dimensions of the data matrix and the second line indicates we will be using binary characters. The four characters correspond to areas defined by the geography file (next subsection). Rows in

the `matrix` block correspond to taxa and their range data, while columns give in which areas each taxon is present (1) or absent (0). For example, taxon `P_hexandra_Oahu` is present only in area 2.

The `trees` block gives the tree describing the shared ancestry of the study species. Because range evolution occurs in units of geological time, the analysis in this tutorial requires a high-quality time-calibrated phylogeny. This typically requires a multiple sequence alignment over several loci plus fossils for calibration. Since this data availability is often the limiting factor for which taxa to include for your analysis, it is best to produce the phylogeny first. Only afterwards should you begin assembling data for your data matrix. If your phylogeny cannot be calibrated (e.g. it has no fossils) your best alternative is to proceed with a time tree resulting from a divergence time estimation analysis. For this tutorial, the phylogeny is assumed to contain no uncertainty.

### 3.2 Atlas file

The geography used in this tutorial represents the Hawaiian archipelago. Beneath Hawaii, currently the largest and youngest island, is a volcanic hotspot that periodically creates new islands. The ages of these islands are fairly well known, meaning we can model range availability as a function of time. Following Ree and Smith (2008), we will lump groups of smaller islands into single areas to simplify the analysis, leaving us with four areas: Hawaii (H), Oahu (O), Maui (M; this includes Molokai and Lanai), and Kauai (K; this includes Niihau). These areas are modeled have arisen 0.5, 1.9, 3.7, and 5.5 million years ago, respectively.

Although the model will use discrete-state biogeographic ranges, geographical area is naturally continuous. This means we must impose some discretization upon the geography to designate a set of biogeographically meaningful characters called areas. Different methods use different criteria for this discretization, so it is best to perform the discretization yourself rather than blindly using the discretization given from a previous study or method (but do blindly use the dataset included in this tutorial). Some geographies have natural discretizations: for instance, the Hawaiian archipelago forms naturally discrete areas on the basis of islands. For many geographies, however, it may unclear how to perform this discretization. Much like morphological analyses, you might choose to choose areas based on expert opinion, based on some model, or using some “naive” uniform discretization. This procedure is not part of the tutorial, but you should be aware that area definitions are not always obvious or objective.

→ Open the file `examples/hawaii_dynamic.atlas.txt`.

```
{
  "name": "HawaiianArchipelago5my",
  "epochs": [
    {
      "name": "epoch1",
      "start_age": 100.0,
      "end_age": 3.7,
      "areas": [
        { "name": "Kauai", "latitude": 19.5667, "longitude": -155.5000, "dispersalValues": [ 1, 0, 0, 0 ] },
        { "name": "Oahu", "latitude": 19.5667, "longitude": -155.5000, "dispersalValues": [ 0, 0, 0, 0 ] },
        { "name": "Maui", "latitude": 19.5667, "longitude": -155.5000, "dispersalValues": [ 0, 0, 0, 0 ] },
        { "name": "Hawaii", "latitude": 19.5667, "longitude": -155.5000, "dispersalValues": [ 0, 0, 0, 0 ] }
      ],
      {
        "name": "epoch2",
        ...
      },
      {
        "name": "epoch3",
        ...
      },
      {
        "name": "epoch4",
        "start_age": 0.5,
        "end_age": 0.0,
        "areas": [
          { "name": "Kauai", "latitude": 22.0833, "longitude": -159.5000, "dispersalValues": [ 1, 1, 1, 1 ] },
          { "name": "Oahu", "latitude": 21.4722, "longitude": -157.9772, "dispersalValues": [ 1, 1, 1, 1 ] },
          { "name": "Maui", "latitude": 20.8000, "longitude": -156.3333, "dispersalValues": [ 1, 1, 1, 1 ] },
          { "name": "Hawaii", "latitude": 19.5667, "longitude": -155.5000, "dispersalValues": [ 1, 1, 1, 1 ] }
        ]
      }
    ]
  }
}
```

This is called the Atlas file, which uses a file format called JSON. JSON is a lightweight format used to assign values to variables in a hierarchical manner. There are three main tiers to the hierarchy in the Atlas file: the atlas, the epoch, and the area. In the lowest tier, each area corresponds to a character in the model and is assigned its own properties. In the middle tier, each epoch contains the set of homologous areas (characters) that may be part of a species' range, but importantly the properties of these areas may take on different values during different intervals of time, as given by the `start_age` and `end_age` variables. Because the tree and range evolution model also operate on units of geological time, the rates of area gain and loss can condition on areas' properties as a function of time. Sometimes these models are called stratified models or epochal models. Finally, the atlas contains the array of epochs in the highest tier.

Each area is assigned a `latitude` and `longitude` to represent its geographical coordinates, ideally the area's centroid. If a centroid does not represent the distance between areas, splitting the area into multiple smaller areas is reasonable. The data augmentation approach used in this analysis allows you to use more areas as desired, whereas matrix exponentiation methods are limited to approximately ten areas. The distance between any two areas' coordinates inform to distance-dependent dispersal parameter ( $\beta$  from the  $\eta(\cdot)$  function) for range expansion events, so coordinates roughly close to the center of the area suffice. Here, the `latitude` and `longitude` change in each of the four epochs, where they begin at the current location of Hawaii and drift northwesterly until they reach their current positions.

In addition, each area is marked as habitable or not using the `dispersalValues` array. The elements in the array correspond to the other areas defined in the analysis. For example, in `epoch1`, Kauai's `dispersalValues` is equal to `[ 1, 0, 0, 0 ]`, which indicates Kauai exists at that point in time but it is not in contact with any other areas, i.e. the range in that area cannot expand into other areas. The `dispersalValues` for Oahu, Maui, and Hawaii are all equal to `[ 0, 0, 0, 0 ]`,



meaning no species may be present in that area during the time interval of epoch1 during ages from 10.0 to 3.7. In contrast, `epoch4`, from ages 0.5 to the present, range expansions may occur between any pair of areas and any area may be included in a species' range.

## 4 RevBayes Analysis

There are six major parts to the analysis.

First, we need to read in the input files and assign analysis settings. Second, we need to construct our model. Third, we need to assign moves and monitors to our model parameters for use with Markov chain Monte Carlo (MCMC). Fourth, we will run an MCMC analysis assuming a complex model. Fifth, we will compare the complex model with a simple model using Bayes factors. Finally, we'll analyze our MCMC output.

### 4.1 Analysis settings

→ Open the RevBayes console

```
$ revbayes
```

First, we'll assign all our input files to **String** variables.

```
RevBayes > in_fp    <- "./input/"
RevBayes > data_fn  <- "psychotria_range.nex"
RevBayes > area_fn  <- "hawaii_dynamic.atlas.txt"
RevBayes > out_fp   <- "./output/"
RevBayes > out_str  <- "bg_2rate"
```

Then we'll create our range data, tree, and atlas objects

```
RevBayes > data    <- readCharacterData(in_fp + data_fn)
RevBayes > tree    <- readTrees(in_fp + data_fn)[1]
RevBayes > atlas   <- readAtlas(in_fp + area_fn)
```

### 4.2 Creating the model

Here, we will compose our rate matrix, **Q**, parameterized by the transition rates,  $\lambda$ , and the distance dependent dispersal power parameter,  $\beta$ .

First, for  $\lambda$ , we will create a vector of two rates, where `glr[1]` corresponds to the rate of area loss (local extinction) and `glr[2]` corresponds to the rate of area gain (dispersal). Each rate will be

drawn from an exponential distribution with rate 10.0 (mean 0.1). Because our tree is in units of millions of years, this means our prior expectation is that any given species undergoes one dispersal or extinction event per area per ten million years.

To introduce this to the model, type

```
RevBayes > for (i in 1:2) glr[i] ~ dnExponential(10.0)
```

Next, we will create `dp`, which determines the importance of geographical distance to dispersal. Remember that values of  $\beta$  far from zero means distance is important. So, if we assign a prior that pulls  $\beta$  towards zero, then posterior values of  $\beta$  far from zero indicate the range data are informative of the importance of distance to dispersal. We'll use an exponential distribution with rate 10.0 (mean 0.1) as a prior for `dp`.

We will also create a deterministic node to modify the rate of dispersal between areas by evaluating `dp` and `atlas`. This node is determined by the function `fnBiogeoGRM`, where GRM stands for “geographical rate modifier”, and plays the role of the  $\eta(\cdot)$  rate-modifier function mentioned earlier. We will tell the `fnBiogeoGRM` function to modify dispersal rates based on distances and whether or not the area exists during an epoch.

```
RevBayes > dp ~ dnExponential(10.0)
RevBayes > grm := fnBiogeoGRM(atlas=atlas, distancePower=dp,
    useAvailable=true, useDistance=true)
```

Now we need a deterministic node to represent the rate matrix, `Q`. To determine the value of this node, we'll use the function `fnBiogeoDE` to assign our model parameters to transition rates as described in the introduction. As input, we'll pass our gain and loss rates, `glr`, and our geographical rate modifier, `grm`. In addition, we'll inform the function of the number of areas in our analysis and whether we will allow species to be absent in all areas (i.e. have the null range).

```
RevBayes > Q := fnBiogeoDE(gainLossRates=glr, geoRateMod=grm, numAreas
    =4, forbidExtinction=true)
```

To extract information for the frequencies of different cladogenic event types, we will create a Dirichlet-distributed stochastic node. The simplex is over three events, subset sympatry (index 0), allopatry (index 1), and widespread sympatry (index 2), but not over narrow sympatry whose range size is one. The prior parameter `[1,1,1]` is known as a flat prior, meaning all event types are expected to occur at equal frequency. If there is information in the data of a dominant cladogenic mode of range evolution, the posterior simplex values in `csf` will reflect this.

```
RevBayes > csf ~ dnDirichlet([1,1,1])
```

For the model's final node, we create the stochastic node for the continuous-time Markov chain (CTMC). This node's distribution is `dnPhyloDACTMC` where DA indicates the CTMC uses data-augmentation to compute the likelihood rather than Felsenstein's pruning algorithm. To create the

distribution, we must pass it our **tree** and **Q** objects, but additionally inform the distribution that it will be using a biogeographic model, that it will introduce the simple cladogenic range evolution events described in Ree and Smith (2008) (**useCladogenesis=true**), and that it will assign zero probability to a transition away from the null range state.

```
RevBayes > M ~ dnPhyloDACTMC(tree=tree, Q=Q, C=csf, type="biogeo",  
  forbidExtinction=true, useCladogenesis=true)
```

So we may evaluate the graphical model's likelihood, we tell the CTMC to observe the **data** object, which will prime the model with data-augmented character histories. Now **M** has a defined likelihood value.

```
RevBayes > M.clamp(data)  
RevBayes > M.lnProb  
-56.0288
```

Finally, we encapsulate our graphical model into a **Model** object, which can learn the model's structure and dependencies from any model parameter.

```
RevBayes > my_model <- model(glr)
```

### 4.3 Running an MCMC analysis

Now that we have our **Model** object, we can soon run an MCMC analysis. Remember that MCMC approximates the posterior distribution by repeatedly proposing new model parameter values, accepting or rejecting those new parameter values based on the model likelihood (and on biases in the proposal distribution), then reporting the sampled parameter values.

First, let's assign moves to our model parameters. These parameters are all supported for real positive values, which is appropriate for use with scale-multiplier proposal, **mvScale()**. To inspect our model parameter types and the proposal argument types, enter

```
RevBayes > type(dp)  
  RealPos  
RevBayes > type(glr)  
  RealPos[]  
RevBayes > mvScale  
  Move_Scale function (RealPos x, RealPos lambda, Bool tune, RealPos  
    weight)
```

The arguments for **mvScale** are fairly typical as far as RevBayes **Move** objects go: **x** is the stochastic node the **Move** will update, **lambda** is proportional to how radically different proposed parameter

values will tend to be, **tune** allows **lambda** to be adjusted automatically as the MCMC runs, and **weight** tells the MCMC how many times to perform the **Move** during a single MCMC generation (e.g., **weight=2.0**) means each generation will call that **Move** for the parameter **x** twice).

```
RevBayes > moves[1] <- mvScale(x=glr[1], lambda=0.5, tune=false, weight=5.0)
RevBayes > moves[2] <- mvScale(x=glr[2], lambda=0.5, tune=false, weight=5.0)
RevBayes > moves[3] <- mvScale(x=dp, lambda=0.5, tune=false, weight=5.0)
RevBayes > moves[4] <- mvSimplexElementScale(csf, alpha=10.0, tune=false, weight=4.0)
```

In addition to proposing new model parameter values, we must also propose new data-augmented states and events to properly integrate over the space of possible range histories. The major challenge to sampling character histories is ensuring the character histories are consistent with the observations at the tip of the tree. The proposals in this tutorial use Nielsen (2002)'s rejection sampling algorithm, with some modifications to account for cladogenic events and epoch-based rate matrices.

The basic idea is simple. Each time a character history proposal is called, it selects a node at random from the tree. Path history proposals (**mvPathCHRS()**) propose a new character history for the lineage leading to that node. Node history proposals (**mvNodeCHRS()**) propose a new character history for the node and for the three lineages incident to that node. The character history proposal also samples some number of areas to update, ranging from one to all of the areas. Once the new character history is proposed, the likelihood of the model is evaluated and the MCMC accepts or rejects the new state according to e.g. the Metropolis-Hastings algorithm.

Because these **Move** objects update the character histories stored in the data-augmented CTMC node, e.g. **M**, they require access to a **TimeTree** object to know which lineages are sisters and whether the lineages span various epochs, and a **RateMap\_Biogeography** object to propose new character histories. The **lambda** argument gives what proportion of areas' character histories to update. Here, if **lambda=0.2**, then the proposal will redraw character histories for each area with probability 0.2 (in addition to one random area with probability 1). Below, we use two moves of each type with **lambda=0.2** and **lambda=1.0** for partial and full character history updates, respectively. Indicating **type="biogeo"** informs the **Move** object to be aware of special character history constraints, such as cladogenic events and forbidden null ranges. The **weight** parameter should be assigned a value proportional to the number of nodes in the analysis to ensure proper mixing.

Let's create the character history moves as follows.

```
RevBayes > n_nodes <- tree.nnodes()
RevBayes > moves[5] <- mvNodeCHRS(ctmc=M, qmap=Q, tree=tree, lambda=0.2, type="biogeo", weight=2.0*n_nodes)
RevBayes > moves[6] <- mvPathCHRS(ctmc=M, qmap=Q, tree=tree, lambda=0.2, type="biogeo", weight=2.0*n_nodes)
RevBayes > moves[7] <- mvNodeCHRS(ctmc=M, qmap=Q, tree=tree, lambda=1.0, type="biogeo", weight=n_nodes)
```

```
RevBayes > moves[8] <- mvPathCHRS(ctmc=M, qmap=Q, tree=tree, lambda
  =1.0, type="biogeo", weight=n_nodes)
```

Now that we have moves for all our parameters and the character histories, we'll proceed with assigning **Monitor** objects to record their values. The first two **Monitor** objects are fairly standard and found in most RevBayes MCMC analyses. **mnScreen** reports the values for any nodes assigned to **RevObject** ... every **printgen** generations to the terminal screen. **mnModel** reports the values for all nodes in the **Model** object every **printgen** generations to the file assigned to **filename**, which is delimited by the **separator** character.

```
RevBayes > mnScreen
  Mntr_Screen function (RevObject ..., Natural printgen, Bool
    posterior, Bool
    likelihood, Bool prior)
RevBayes > monitors[1] <- mnScreen(printgen=10, glr, dp, csf)
RevBayes > mnModel
  Mntr_Model function (String filename, Natural printgen, String
    separator,
    Bool posterior, Bool likelihood, Bool prior, Bool append, Bool
    stochasticOnly)
RevBayes > monitors[2] <- mnModel(filename=out_fp+params_fn, printgen
  =10)
```

Like any parameter, we can sample the augmented range histories from the MCMC to approximate the posterior distribution of range histories. This is statistically equivalent to generating ancestral state reconstructions from a posterior distribution via stochastic mapping. We will extract these reconstructions using special monitors designed for the **dnPhyloDACTMC** distribution.

Next, we will create **Mntr\_CharacterHistoryNewickFile** objects to record the sampled character history states for each node in the tree. This **Monitor** has two **style** options: **counts** reports the number of gains and losses per branch in a tab-delimited Tracer-readable format; **events** reports richer information of what happens along a branch, anagenically and cladogenically, using an extended Newick format. How to read these file formats will be discussed in more detail in Section ??.

```
RevBayes > mnCharHistoryNewick
  Mntr_CharacterHistoryNewickFile function (String filename,
    AbstractCharacterData ctmc, TimeTree tree, Natural printgen, String
    separator, Bool posterior, Bool likelihood, Bool prior, Bool append,
    String
    style = events|counts
    , String type = biogeo
    )
RevBayes > monitors[3] <- mnCharHistoryNewick(filename=fp+out_str+".
  events.txt", ctmc=M, tree=tree, printgen=100, style="events")
```

```
RevBayes > monitors[4] <- mnCharHistoryNewick(filename=fp+out_str+".
  counts.txt", ctmc=M, tree=tree, printgen=100, style="counts")
```

As our last monitor, the `Mntr_CharacterHistoryNhxF` records character history values throughout the MCMC analysis, then stores some simple posterior summary statistics as a Nexus file. These summary statistics could be computed from the previously mentioned `Monitor` output files, but `mnCharHistoryNhxF` provides a simple way to produce PhyloWood-compatible files. We will also discuss this file's format in more detail later in the tutorial.

```
RevBayes > mnCharHistoryNhxF
  Mntr_CharacterHistoryNhxF function (String filename,
    AbstractCharacterData
    ctmc, TimeTree tree, RlAtlas atlas, Natural samplegen, Natural
      maxgen,
    Probability burnin, String separator, Bool posterior, Bool
      likelihood, Bool
    prior, String type = biogeo
  )
RevBayes > monitors[5] <- mnCharHistoryNhxF(filename=fp+out_str+".nhx.
  txt", ctmc=M, tree=tree, atlas=atlas, samplegen=100, maxgen=25000,
  burnin=0.2)
```

Before we run the MCMC, we'd like to get the node index of the ancestor. When analysing the output, we'll take some special interest in the branch for the most recent common ancestor of *P. kaduana* and *P. hathewayi*. We will identify this lineage by its index, 23, which is meaningful only for a fixed tree topology,

```
RevBayes > names = tree.names()
RevBayes > names[15]
  P_kaduana_PuuKukuiAS
RevBayes > names[16]
  P_hathewayi_1
RevBayes > mrcaIndex(tree=tree, clade=clade(names[15], names[16]))
  23
```

## 4.4 Running an MCMC analysis

Now all that's left is to configure and run our MCMC analysis. For this, we create an `Mcmc` object, which we give our `Move` vector, our `Monitor` vector, and our `Model` object

```
RevBayes > mcmc
  MCMC function (Model model, Monitor[] monitors, Move[] moves, String
```

```

moveschedule = sequential|random|single
)
RevBayes > my_mcmc <- mcmc(my_model, monitors, moves)

```

MCMC typically requires some period of burn-in before it reaches stationarity, i.e. from a random starting point, it takes some time for the chain to produce valid samples from the posterior distribution. By running `burnin()`, we tell the `Mcmc` object to propose and reject new states but *not* to record anything to file. After burn-in is complete, we call `run()`, where we begin recording valid posterior samples under our model.

```

RevBayes > my_mcmc.burnin(generations=1000, tuningInterval=50)
RevBayes > my_mcmc.run(generations=25000)

```

Everything we’ve done is contained in the file `biogeography_DEC_2rate.Rev`. You can modify this file as you like then re-run the analysis by typing

```

RevBayes > source("../scripts/biogeography_DEC_2rate.Rev")

```

## 4.5 Model selection using Bayes factors

Bayes factors (BFs) are used to select which of two models better describes the observed data,  $\mathbf{X}_{obs}$ , and are computed as the ratio of marginal likelihoods for those two models. One might prefer to analytically compute the marginal likelihood, but it’s the same intractable quantity we intentionally avoid computing when using MCMC in a Bayesian context. Instead, we must estimate the marginal likelihood from our posterior distribution samples. Here, we will use thermodynamic integration (Lartillot and Philippe 2006) and stepping-stone approximation (Xie et al. 2010). The exact details of these techniques will not be covered here, but there is an important practical point to mention: both methods rely on computing a number of “power posterior” distributions. Computing more power posteriors increases the marginal likelihood estimator’s accuracy at the cost of computational time.

Moving on, we’ll compute the Bayes factor to compare a simple one-rate model, which asserts the rate of area gain and loss are always equal, to a two-rate model which allows these rates to vary independently. Rather than specifying the model manually, we will load (source) the model definition from a file then enter the commands to compute its marginal likelihood. For faster results, we will use two separate RevBayes sessions, one for each model. For each session, the power posterior analysis run for 1000 generations during burn-in then 1000 generations per each of 30 power posterior categories.

First session:

```

RevBayes > source("../scripts/biogeography_DEC_1rate.Rev")
RevBayes > pp_fn <- out_fp + out_str + ".pp.txt"

```

```

RevBayes > pow_p <- powerPosterior(my_model, moves, pp_fn, cats=30)
RevBayes > pow_p.burnin(generations=1000,tuningInterval=100)
RevBayes > pow_p.run(generations=5000)

```

Second session:

```

RevBayes > source("./scripts/biogeography_DEC_2rate.Rev")
RevBayes > pp_fn <- out_fp + out_str + ".pp.txt"
RevBayes > pow_p <- powerPosterior(my_model, moves, pp_fn, cats=30)
RevBayes > pow_p.burnin(generations=1000,tuningInterval=100)
RevBayes > pow_p.run(generations=5000)

```

Each power posterior analysis will write their contents to the file given in **pp\_fn**. These files are **bg\_1rate.pp.txt** and **bg\_2rate.pp.txt** for the simple and complex models, respectively. This may take a few minutes. When complete, the power posterior files may then be used to compute marginal likelihoods. For example, from the RevBayes session analyzing the simple one-rate model

```

RevBayes > ss <- steppingStoneSampler(file=pp_fn)
RevBayes > ss.marginal()
RevBayes > ps <- pathSampler(file=pp_fn)
RevBayes > ps.marginal()

```

For a given model, the path sampling and stepping stone sampling methods should produce similar marginal likelihood estimates. Values should be within one log likelihood unit of one another. If the values are extremely different, this may indicate **powerPosterior** should be re-run with a larger number of **cats**. We chose **cats=30** which should suffice, and we see no problem. Then from the complex two-rate model RevBayes session using the same commands as above. Finally, we can compute the Bayes factor, which is simply the ratio of marginal likelihoods.

```

RevBayes > exp(-51.7202)/exp(-52.3158)
1.81412

```

A value of one would mean both models had equal marginal likelihoods. A value less than one would indicate the first model, the simple model, had a larger marginal likelihood, and was therefore favored by model testing. But that's not the case, the value is greater than one, and the complex two-rate model is favored. Similar to frequentist interpretations of significance for p-values, there is no universal and objective criterion of significance with Bayes factors, but most would agree a factor of 1.8 (or 1.0/1.8) indicates weak support for one model over the other.



## 5 Output

### 5.1 Sampled parameters from ScreenMonitor

The `mnScreen` monitor reports model parameter values to the screen, where each row corresponds to the current accepted MCMC state, and each column reports some model feature, such as the model likelihood or a parameter value. Every 20 iterations, this monitor re-prints the column headers.

```
RevBayes > my_mcmc.run(generations=25000)

Running MCMC simulation for 25000 iterations
The simulator uses 8 different moves in a random
move schedule with 241 moves per iteration
```

Iteration	Posterior	dp	glr[1]	glr[2]	csf[1]	csf[2]	csf[3]
0	-51.3307	0.0570518	0.175137	0.0580957	0.330891	0.255308	0.413801
10	-54.4257	0.0416423	0.166936	0.178402	0.0549136	0.148854	0.796233
20	-58.0696	0.0991853	0.136495	0.122135	0.308418	0.448892	0.242689
30	-46.5049	0.10676	0.0958918	0.0959592	0.543837	0.363871	0.0922922
40	-42.8697	0.173549	0.158565	0.0662419	0.569416	0.126439	0.304145
50	-43.5319	0.117868	0.196497	0.0523307	0.440269	0.257171	0.30256
...							

For the complex 2-rate model, our model parameters are `dp`, the distance power parameter, and the rates of area loss and gain, `glr[1]` and `glr[2]`, respectively, and the frequencies for subset sympatry, allopatry, and widespread sympatry `csf[1]`, `csf[2]`, and `csf[3]`, respectively. If you notice the value of some parameter is rarely updated from iteration to iteration, the MCMC is probably mixing poorly therefore it's not generating samples from the posterior distribution (the MCMC's stationary distribution). In this case, you may want to re-run the analysis with different arguments for the `Move` object assigned to that parameter.

### 5.2 Sampled parameters from ModelMonitor

This tab-delimited file contains parameter samples from the posterior distribution. As with the `ScreenMonitor`, columns are model or parameter values and rows are MCMC cycles.

Iteration	Posterior	Likelihood	Prior	glr[1]	glr[2]	dp	csf[1]	csf[2]	csf[3]
0	-51.3307	-56.0288	4.69806	0.175137	0.0580957	0.057051	0.330891	0.255308	0.413801
10	-54.4257	-58.1568	3.73110	0.166936	0.1784020	0.041642	0.054913	0.148854	0.796233
20	-58.0696	-62.0923	4.02274	0.136495	0.1221350	0.099185	0.308418	0.448892	0.242689
30	-46.5049	-51.1197	4.61480	0.095891	0.0959592	0.106760	0.543837	0.363871	0.092292
40	-42.8697	-46.4870	3.61735	0.158565	0.0662419	0.173549	0.569416	0.126439	0.304145
50	-43.5319	-47.4659	3.93394	0.196497	0.0523307	0.117868	0.440269	0.257171	0.302560
...									

→ Open Tracer, select the fields for the posterior probability and area gain rate, `glr[2]`, then click the Joint-Marginal tab.

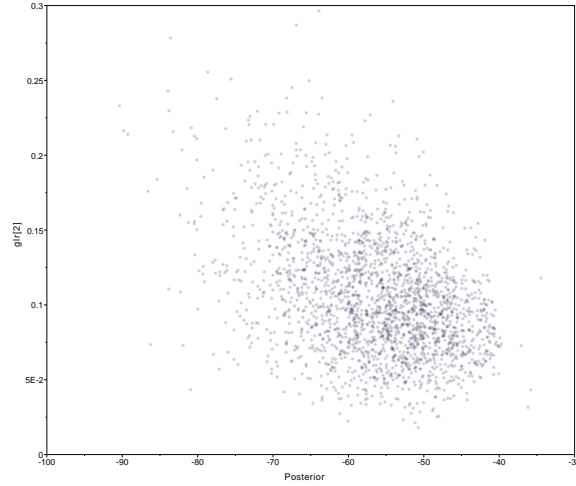


Figure 2: Joint-marginal distribution of posterior and area gain rate,  $\lambda_1$ .

Here, we see a strong negative correlation between the posterior probability and the area gain rate, which is expected. Next, click the Estimates tab then select the three `csf` parameters.

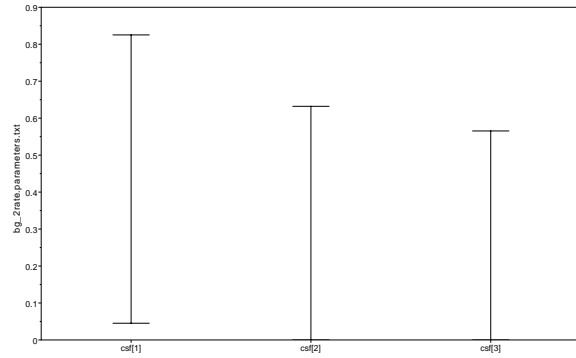


Figure 3: Mean values for the cladogenic state frequency simplex, where `csf[1]`, `csf[2]`, and `csf[3]` correspond to subset sympatry, allopatry, and wide sympatry whose mean posterior values are 0.45, 0.30, and 0.25, respectively.

### 5.3 Biogeographic event counts from `mnCharHistoryNewick`

Recording stochastic mappings in a Tracer-compatible format requires some summarization. This monitor generates a tab-delimited file where the number of events of each type for each branch is recorded.

→ Open `./output/bg_2rate.counts.txt` in a text editor.

Iteration	Posterior	Likelihood	Prior	t_s0	t_s1	t_c0	t_c1	t_c2	t_c3	b0_s0	b0_s1	b0_c	...
0	-51.3307	-56.0288	4.69806	9	9	18	0	0	0	1	1	0	...
10	-54.4257	-58.1568	3.73110	9	10	17	0	0	1	1	1	0	...
20	-58.0696	-62.0923	4.02274	11	9	15	2	1	0	2	1	1	...
30	-46.5049	-51.1197	4.61480	8	8	18	0	0	0	1	1	0	...

40	-42.8697	-46.4870	3.61735	7	7	18	0	0	0	1	1	0	...
50	-43.5319	-47.4659	3.93394	7	7	18	0	0	0	1	1	0	...
...													

For example, **b2\_s1** gives the number of areas that are gained for the branch leading to the node indexed 2. **b2\_c** gives the cladogenic event type that gives rise to the node indexed 2, where narrow sympatry, subset sympatry, allopatry, and widespread sympatry are recorded as 0, 1, 2, and 3, respectively. The columns **t\_s0** and **t\_s1** give the sum of events over all branches. **t\_c0**, **t\_c1**, and **t\_c2** give the total number of narrow sympatric, subset sympatric, allopatric, and widespread sympatric cladogenic events over the entire tree.

Because the expected number of gain events should be proportional to the area gain rate, we expect to see the same negative correlation between posterior probability and number of events as we did with the posterior and rate in the **parameters.txt** file.

Open Tracer, select the fields for the posterior probability and the number of gained areas over the tree, **t1**, then click the Joint-Marginal tab.

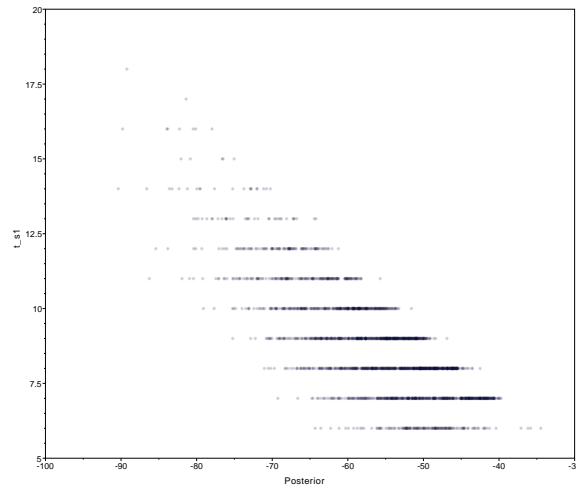


Figure 4: Joint-marginal distribution of posterior and number dispersal events summed over the tree.

One interesting facet of this output is there are never fewer than six events. In fact, since we assume a stratified geography and that only one event may occur per instant, it is impossible to describe the data we see at the tips with fewer than six gain events. That is, six gain events is part of the maximum parsimony solution.

## 5.4 Biogeographic event histories from **mnCharHistoryNewick**

For more detailed data exploration, this analysis also provides annotated Newick strings with the complete character mappings for the tree.

→ Open **./output/bg\_2rate.events.txt** in a text editor.

```

Iteration Posterior Likelihood Prior Tree
Iteration Posterior Likelihood Prior Tree
0 -51.3307 -56.0288 4.69806 (((((((P_hawaiiensis_WaikamoiL1[&index=18;nd=0010;pa=0010;ev={}]:0.96 ...
10 -54.4257 -58.1568 3.7311 (((((((P_hawaiiensis_WaikamoiL1[&index=18;nd=0010;pa=0010;ev={}]:0.96 ...
20 -58.0696 -62.0923 4.02274 (((((((P_hawaiiensis_WaikamoiL1[&index=18;nd=0010;pa=0010;ev={}]:0.96 ...
30 -46.5049 -51.1197 4.6148 (((((((P_hawaiiensis_WaikamoiL1[&index=18;nd=0010;pa=0010;ev={}]:0.96 ...
40 -42.8697 -46.4870 3.61735 (((((((P_hawaiiensis_WaikamoiL1[&index=18;nd=0010;pa=0010;ev={}]:0.96 ...
50 -43.5319 -47.4659 3.93394 (((((((P_hawaiiensis_WaikamoiL1[&index=18;nd=0010;pa=0010;ev={}]:0.96 ...
...

```

Each iteration records the data-augmented character history (stochastic mapping) using metadata labels, which, for an internal node, looks like

```
[&index=23;nd=0110;pa=0010;ch0=0010;ch1=0110;cs=s;bn=16;ev={{t:0.2513,a
:1.1195,s:1,i:1}}
```

**index=23** indicates this branch leads to the node indexed 23. The branch began in the ancestral state **pa=0100** and terminated in the state **nd=0110**. Since this node is not a tip node, it represents a speciation event, so the daughter ranges are also given, **ch0=0010** and **ch1=0110**. The cladogenic state for this speciation event was subset sympatric, **cs=s**, rather than sympatric (wide or narrow; **w** or **n**) or allopatric (**a**). Anagenic dispersal and extinction events occurring along the lineage leading to node 19 are recorded in **events**, where each event has a time (relative to the absolute branch length), absolute age, state (into), and character index (**t**, **a**, **s**, **i**, resp.). For this posterior sample of the character history for the branch leading to node 22, the species range expanded into Oahu at age 1.1195.

To manipulate this data format, we'll use Python scripts. Below are a few examples of interesting posterior features.

→ Open a Python console and read in the events.

```

> cd scripts
> python27

...

>>> from bg_parse import *
>>> dd=get_events(fn="../output/bg_2rate.events")

```

By default, **get\_events()** extracts a dictionary where each node index maps to a branch's character history as reported in **./input/bg\_2rate.events.txt**. Each branch is a dictionary whose keys are various parts of the MCMC state and whose values the MCMC samples.

```

>>> dd[23].keys()
['ch1', 'iteration', 'bn', 'nd', 'ch0', 'prior', 'posterior', 'cs', 'ev', 'likelihood']

```

```
>>> dd[23]['posterior'][0:5]
[-48.6952, -60.1832, -53.2286, -57.5778, -53.4633]
```

To get the  $n = 1$  highest-valued sample for a branch by its posterior value

```
>>> get_best(dd[23],n=1,p='posterior')
{'prior': [4.48225], 'iteration': [14890], 'bn': [22], 'nd': [[0, 1, 1,
0]], 'ch0': [[0, 1, 1, 0]], 'ch1': [[0, 0, 1, 0]], 'posterior':
[-34.7139], 'pa': [[0, 1, 0, 0]], 'cs': ['p'], 'ev': [[{'age':
1.5637, 'state': 1, 'idx': 2, 'time': 0.8611}]], 'likelihood':
[-39.1962]}
```

To get the probability that area  $i$  and area  $j$  are both part of the species range as the branch for node 23 terminates, just before the speciation event

```
>>> get_area_pair(dd[23])
[[0.0816, 0.0188, 0.0628, 0.0000],
 [0.0188, 0.7081, 0.4390, 0.0000],
 [0.0628, 0.4390, 0.7141, 0.0000],
 [0.0000, 0.0000, 0.0000, 0.0000]]
```

showing area 3 was occupied nearly with probability 0.71 and both areas 2 and 3 were occupied with probability 0.44. Note, Hawaii was submerged until approximately 0.5 million years ago, and thus the probability of being in that area is 0.0.

If the range is size one during a speciation event, the cladogenic event state is always narrow sympatric, “n”. But given the opportunity for non-sympatric events, i.e. that the range is larger than size one, we can get the probability of cladogenic state using For the probability for cladogenic event state given the range was larger than size one

```
>>> get_clado_state(dd[23])
{'a': 0.0224, 's': 0.1463, 'w': 0.3183, 'n': 0.5130}
>>> get_clado_state(dd[23],minSize=2)
{'a': 0.0460, 's': 0.3005, 'w': 0.6535, 'n': 0.0000}
>>> get_clado_state(get_best(dd[23],n=100),minSize=2)
{'a': 0.1290, 's': 0.6774, 'w': 0.1936, 'n': 0.0000}
```

Depending on your question, different aspects of the posterior cladogenic state will interest you. Narrow sympatry is the favored ancestral state, but wide sympatry is favored for ranges of size  $n > 1$ . However, when we look at the 100 most probable samples, subset sympatry becomes most favored.

More script functions are found in `./scripts/bg_parse.py`.

## 5.5 New Hampshire extended format file (`./output/bg_2rate.nhx`)

Because this data is very high-dimensional, we'll use an external data exploration tool to look at range evolution.

This file summarizes the input and output from a BayArea analysis using NEXUS format containing a New Hampshire eXtended (NHX) tree string. NHX allows you to annotate nodes in a Newick string with meta-information, which BayArea uses to report the probabilities in the `my_run.area_probs.txt` file. The `geo` block gives the geographical latitudes and longitudes for the areas in the order they are reported as probabilities. Like the `my_run.area_probs.txt` file, this file is not written until the analysis is complete. This annotation is used for the two visualization programs covered in the next section, PhyloWood and BayArea-Fig. The anatomy of the PhyloWood and BayArea-Fig settings blocks will also be explained there.

## 6 Visualization

Here we'll explore two options for visualizing ancestral range reconstructions. I'll walk you through some of the basic functionality, but feel free to play around as you like.

### 6.1 PhyloWood

PhyloWood generates interactive animations to explore biogeographic reconstructions.

- Open <http://mlandis.github.io/phylowood>.
- Drag and drop `./output/bg_2rate.nhx.txt` into the text field.



Figure 5: PhyloWood frame showing posterior ancestral range of root node.

- Click the Play button to view the animation.

There are three control panels to help you filter data: the media panel, the map panel, and the phylogeny panel. The media buttons correspond to Beginning, Slow/Rewind, Play, Stop, Fast Forward, Ending (from left to right). The animation will play the timeframe corresponding to the slider.

→ Drag the slider to the right (the present).

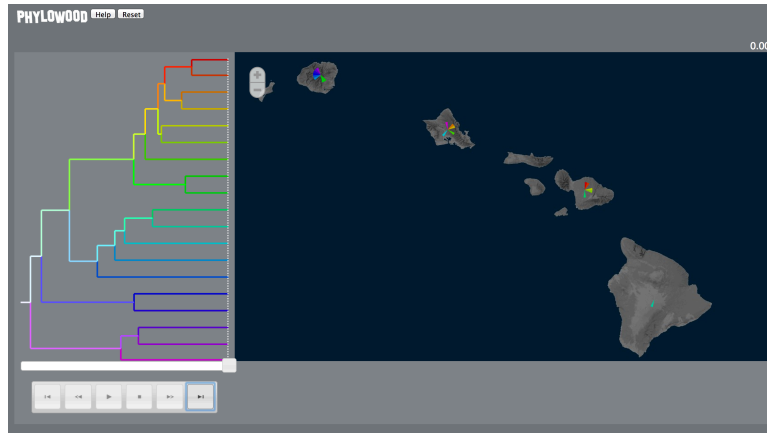


Figure 6: Phylowood frame showing distribution of extant taxon ranges.

→ Pan and zoom around the map.

Marker colors correspond to the phylogenetic lineages in the phylogeny panel. Markers are split into slices and (loosely) sorted phylogenetically, so nearby slices are generally closely related. At divergence events, a marker's radius is proportional to the marginal posterior probability the node was present in the area at that time. Between divergence events, marker's radius is simply an interpolation of the values at the two endpoints. Some information about geological constraints and cladogenic events is lost.

→ Mouseover an area to learn which lineage it belongs to and its presence probability.

Since it's difficult to see how specific clades evolve with so many taxa, Phylowood offers two ways to filter taxa from the animation. We call the set of a lineage, all its ancestral lineages towards the root, and all descendant lineages a phylogenetic heritage. The root's heritage is the entire clade. A leaf node's heritage is a path from the tip to the root.

→ Mouseover a lineage to temporarily highlight the lineage's heritage. Remove the mouseover to remove the highlight effect.

The highlight effect is temporary and quickly allows you to single out lineages of interest during animation. Phylowood also offers a masking effect that persists until an unmask command is issued.

- Double-click the white root branch to mask the root node's heritage (all lineages). Single click a lineage to unmask that lineage's heritage.



Figure 7: PhyloWood frame highlighting the posterior range for the most recent common ancestor of *P. mawiensis* and *P. hawaiiensis*.

Now that the masking effects are in place, you're free to interact with other map components. In addition, the area of marker sizes is only distributed among unmasked lineages.

- Visit <https://github.com/mlandis/phylowood/wiki> to learn more about PhyloWood.

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