

1. Write dual of the following Boolean Expression:

a.) $(x + y') \rightarrow xy'$

b.) $xy + xy' + x'y \rightarrow (x+y)(x+y')(x'+y)$

c.) $a + a'b + b' \rightarrow a(a'+b)b'$

d.) $(x+y'+z)(x+y) \rightarrow xy'z + xy$

2. Find the complement of the following functions applying De Morgan's theorem:

a.) $F(x, y, z) = x'y^*z' + x'y'z^*$

$$F'(x, y, z) = (x'y^*z')'(x'y'z^*)'$$

$$= (x+y'+z)(x+y+z')$$

b.) $F(x, y, z) = x(y'z + yz)$

$$= x + (y'z)'(yz)'$$

$$= x' + (y+z')(y'z')$$

3. Find the complements of the expressions

i.) $X + YZ + XZ \rightarrow f(x, y, z) = X + YZ + XZ$

$$f'(x, y, z) = [X(Y+Z)(X+Z)]'$$

$$= X'(y'+z')(x'+z')$$

ii.) $AB(C'D + B'C) \rightarrow f(A, B, C, D) = AB(C'D + B'C)$

$$f'(A, B, C, D) = [A+B+((C'+D)(B+C))']$$

$$= A'+B'+((C+D')(B'+C'))$$

4. In the boolean Algebra, verify using truth table that $(x+y)' = x'y'$ for each x, y in $\{0, 1\}$.

x	y	$(x+y)'$	$x'y'$
0	0	1	1
0	1	0	0
1	0	0	0
1	1	0	0

5.

Give algebraic Proof of absorption law of boolean algebra:

Absorption law states that:

$$(i) X + XY = X \longrightarrow X(y+1) = X$$

$$X = X$$

$$(ii) X(x+y) = X \longrightarrow X + (0.y) = X$$

$$X + 0 = X$$

$$X = X$$

6.

Convert the following expression to Canonical SOP form:

$$(a) X + X'Y + X'Z'$$

$$\rightarrow X = X(Y+Y')(Z+Z')$$

$$= XYZ + XY'Z + XYZ' + XY'Z'$$

$$\rightarrow X'Y = X'YZ + X'YZ'$$

$$\rightarrow X'Z' = X'YZ' + X'Y'Z'$$

$$\Rightarrow XYZ + XYZ' + XY'Z + XY'Z' + X'YZ + X'YZ' + X'Y'Z + X'Y'Z'$$

$$\text{atau } m_7 + m_6 + m_5 + m_4 + m_3 + m_2 + m_1 + m_0$$

$$(b) YZ + X'Y$$

$$\rightarrow X'YZ + X'Y'Z$$

$$X'Y = X'YZ + X'Y'Z$$

$$\Rightarrow X'YZ + X'Y'Z + X'Y'Z'$$

$$\text{atau } m_7 + m_3 + m_2$$

$$(c) AB'(B'+C') \longrightarrow AB' + AB'C'$$

$$\rightarrow AB' = AB'C + AB'C'$$

$$AB'C' = AB'C'$$

$$\Rightarrow AB'C + AB'C'$$

$$\text{atau } m_5 + m_4$$