

Compiler Design

21/11/18

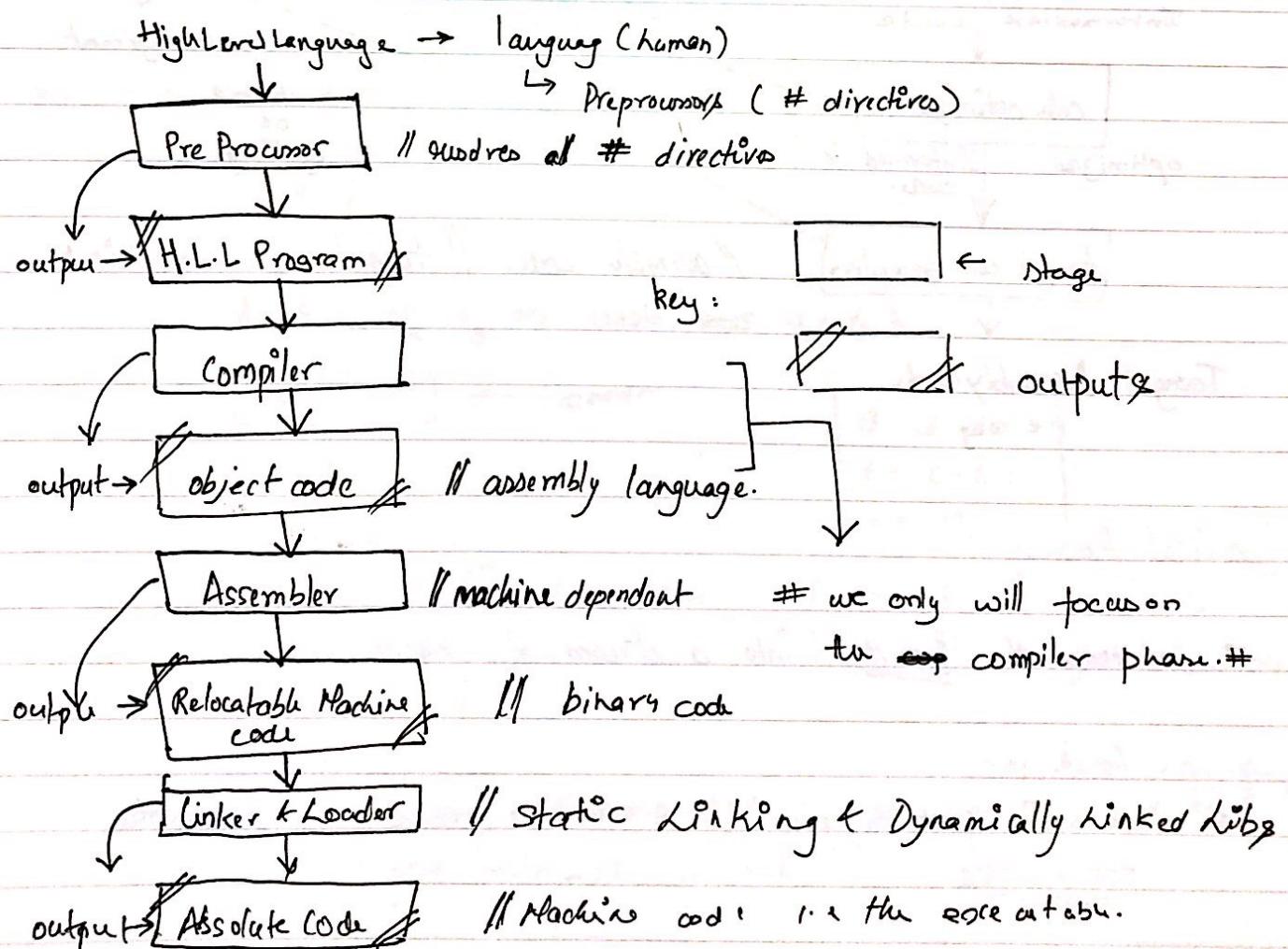
- books:
- 1) Compiler Design: Aho, Ullman & [Dragon series]
 - ↳ 4 books all are same
 - ↳ use Aho, Ullman & Sethi
 - 2) Compiler Design → Rajni Jindal

Dy11abus

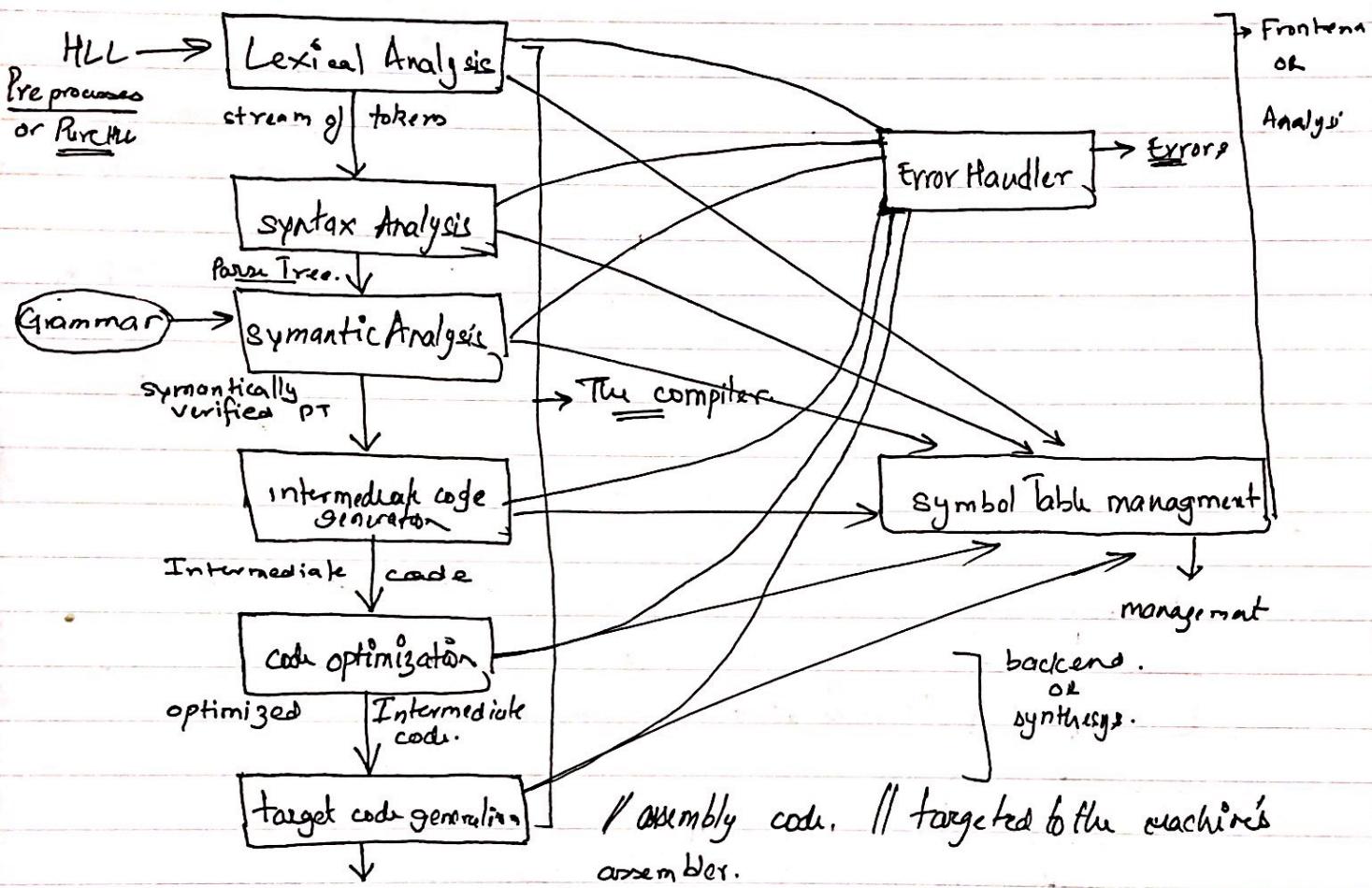
Unit 1: DFA, NFA, NFA → DFA
RE's

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" What is a language translator? Why do we need it? "



Phases of the compiler



Lexical Analyzer

→ converts the PureHLL into a stream of tokens.

Syntax Analyzer

→ the main part of compiler, A.K.A the parser, it builds the parse tree (like a derivation tree)

Semantic Analyzer

It builds the semantically verified parse tree.

Intermediate Code Generation

It builds the intermediate 3 address codes/ graph rep code
This is a syntax tree (a way to rep IC)

Code optimizer

This optimizes the IC. It makes the optimized IC (optimized Syntax tree)

Error Handler: " ; is what error "

→ Lexical error : misspelt words. e.g. if() → f^e()

example of Lexical analysis:

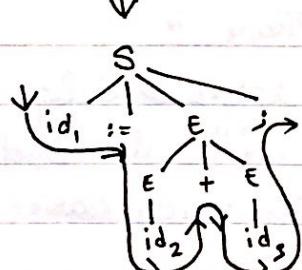
C := a+b ; // match with RE.

↓
Lex Ana

id, op, id, op, id, OR id := id + id ;

↓
Synt Ana ← Grammar

S: id := E ;
E = E + E ;
E = id ;



// parse tree. if tree is similar to its input then it's syntactically correct.

↓
semantic. Ana

// type checking e.g. float = char + double X

↓
ICG → Optimizer

"How the 1st compiler was compiled".

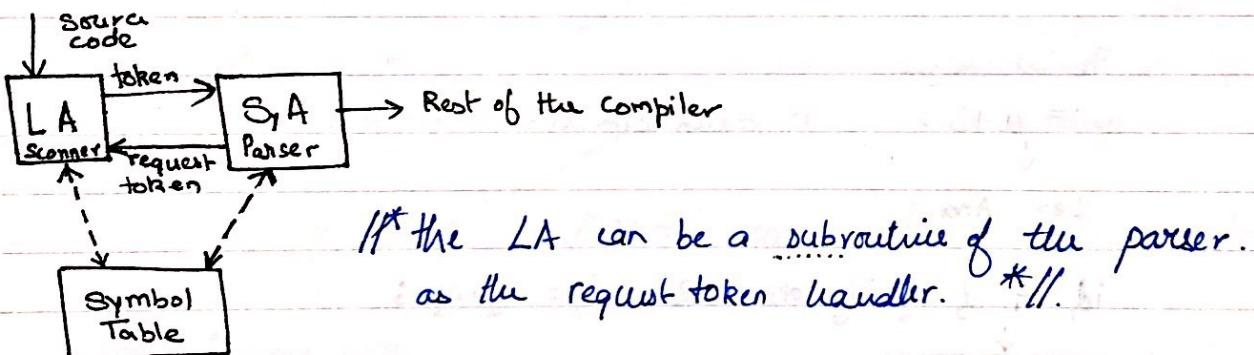
Lexical Analyser (Scanner)

The reads the source code char by char & translates it into sequence of primitive units called tokens.

e.g. key words, identifiers, const.

Tasks of L.A

- 1) Read Input, convert to token
- 2) Removes comments, white spaces (';', '→', & '\n')
- 3) Makes a copy of the program with error message marked in it, i.e. errors are associated with line numbers.
[Keeps track of '\n' to get line no.]

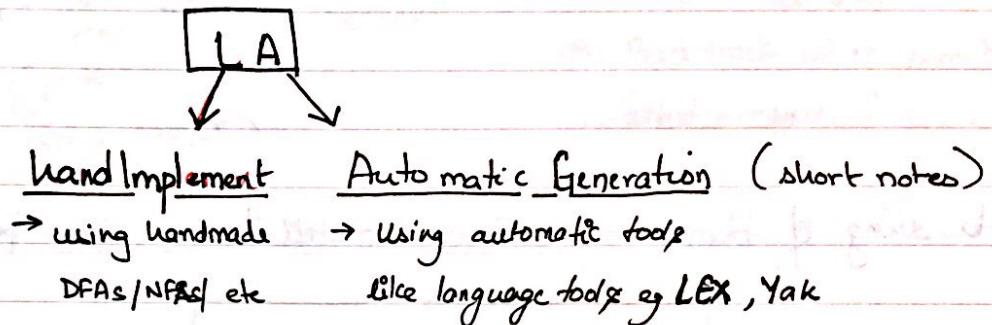


"Advantages of LA as an Independent Phase"

- > To simplify the overall design : we are dealing with structure of tokens. The Sy deals with the syntactical structure - doing these separately is much easier and faster.
- > Reading the source is the most time consuming part, separating this from Sy makes it faster. This allows to have input buffering ~~schemes~~ schemes.
- > Changes to separate modules are much easier to incorporate

- > Enhances the portability of the compiler.
- > All device related matters consolidated to the LA.

Design and Implementation of LA



Design Issues

- > a way to describe tokens (i.e regex)
- > Mechanism to recognize a token (i.e Recognizers / DFA_z)
- > Actions, what to do with a token like buffer, Pass to SA, ~~etc~~, add to symbol table, error/diagnostic messages.

Token, Lexeme & Pattern

Lexeme : (An example of token). Is the smallest logical unit of a program or sequence of chars for which a token is produced. (a, b, c, int)

Token : Class of similar lexemes given a name (Identifiers)

Pattern : Rule describing a token (Regex, Grammars) ($P[ld]^*$)

The pattern $l(lord)^*$ \rightarrow T \rightarrow $\begin{matrix} \text{int } a,b,c; \\ | \\ \text{lexemes.} \end{matrix}$
 identifier

→ attributes (value, type, scope, other)

< token name, pointer to symbol Table >

eg < keyword, [if (value of keyword)] >

< id, [value of id] >

put → kw | if → keyword

[// different keyword will
have different entries //]

Issues in implementation.

1> Handling of blanks (if lexeme matches it, else don't produce a token)

delimiter → blanks, tabs, \n
whiteSpace → delimiter.

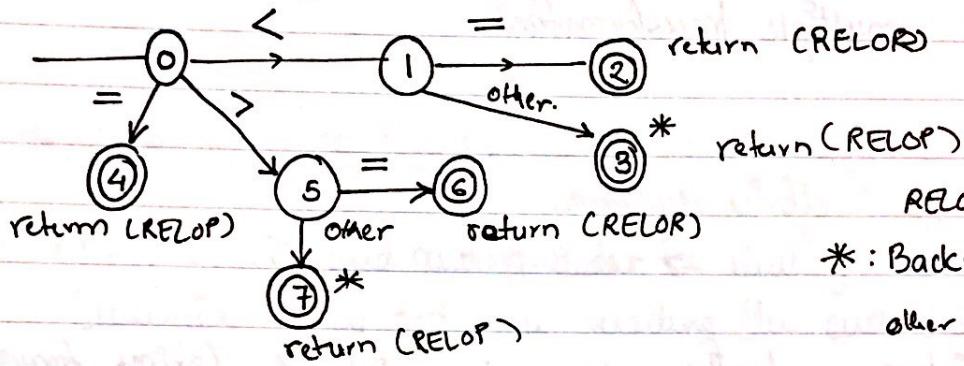
2> different languages treat blanks differently.

DO 5 I = 1.25

↳ some language may call this an identifier.

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Lexical Analyzer [DFA as Acceptors]



RELOP: Relational OP.

*: Backtrack when something other is read.

Transition Diagram for Relational Operator.

Lexical Analyzer is nothing but a big transition diagram

- If we fail on one TD we move on to the next TD.
- If we fail on all TD then error recovery must be invoked.
- The more frequently used symbols will be placed near the start state.

What is a Lexical Error?

- Any lexeme which does not match any pattern TD
i.e. No token is produced

Error Recovery

- Replace with correct
- Delete extra char
- Insert correct
- Transpose the two chars.

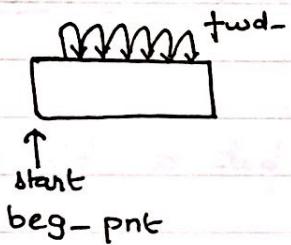
- See whether the prefix of remaining input can be transformed into a valid lexeme by single transformation.
- It may take multiple transformations.

Buffering Techniques (Compiler dependent)

- Single Buffer
- Two Buffer

Single Buffer

- We have 2 pointers, lexime_beginning_pointer & lexime_forward_pointer

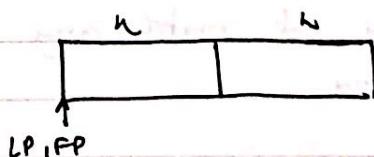


→ Initially both are @ start, then only fwd moves till it finds a match

Drawback

- Buffer size < Lexime size Then wrap around happens.
[common to both]

Two Buffer



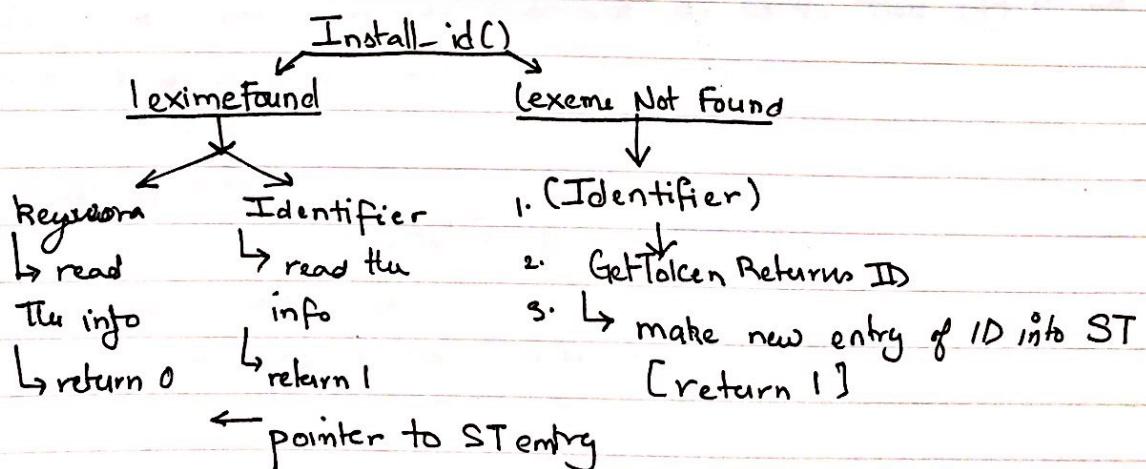
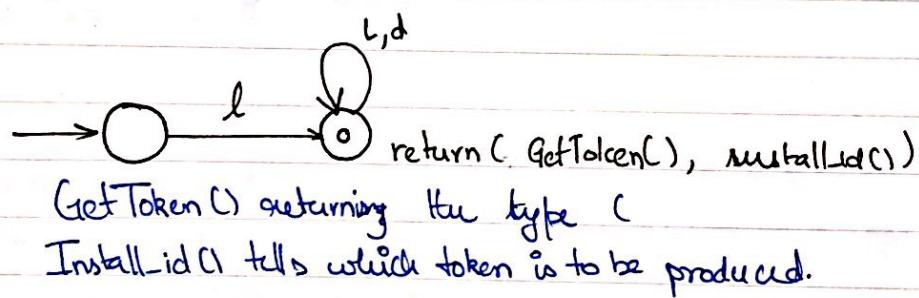
in one read, read n chars simultaneously into the 1st half of the buffer.

- When FP is about to reach halfway mark, then load the next buffer.

In some languages keywords are not reserved.

Keywords Vs Identifiers, How to tell them apart.

- 1) Make a TD and run a code to identify whether it is a identifier / keyword. On reaching the end state run code to check
- 2) Make use of symbol table intelligently. Pre enter all keywords into the symbol table.



Logic Behind `InstallId()`

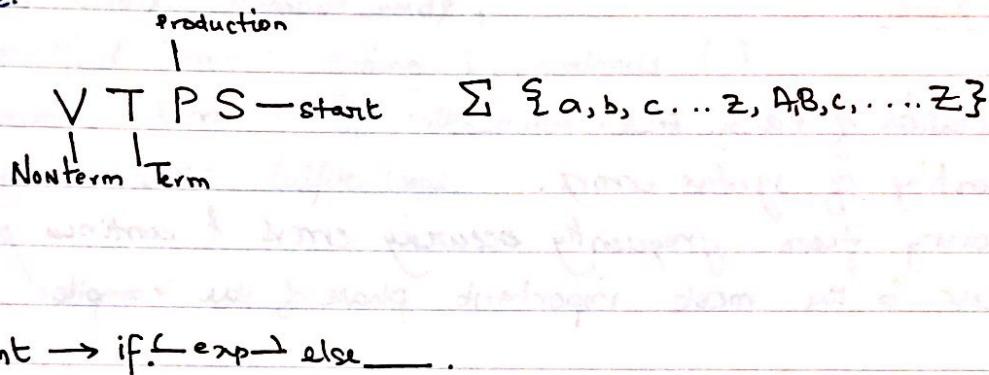
benifits :

> Allows easy changes for new keys as we only need to change the symbol table.

If some other method is used then multiple updates may be needed.

Syntax Analyzer (Parser)

The grammar (production rules) provide syntactic structure to the language.



This takes a sequence of tokens and converts it into a parse tree.

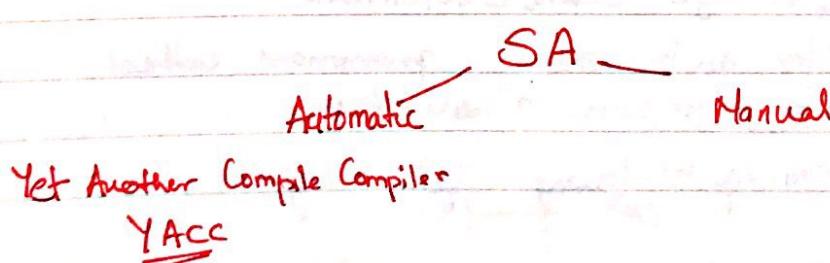
Q1: Give some example of constructs that cannot be expressed by RE.

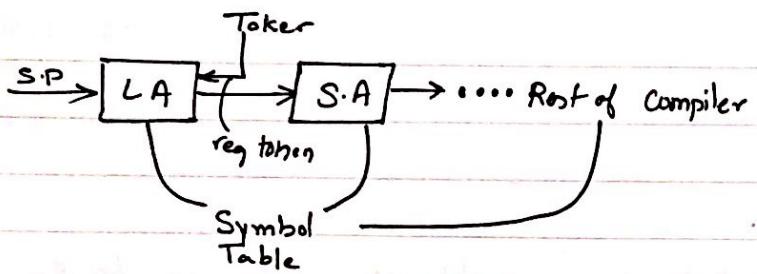
→ RE are incapable of representing program structure eg, loops, conditional
To express this we use CFG.

Q2: When everything can be expressed as CFG, then why do we have regular expressions.

Advantages of CFG :

- Gives precise specification of a language.
- Easy to understand.
- Easy to expand rules. (adding new rules)





Role of Parser

- 1) Generation of Parse tree.
- 2) Reporting of syntax errors.
- 3) Recovery from frequently occurring errors & continue parsing.
- 4) Parser is the most important phase of the compiler!

Types of Parsers

- 1) CYK Parsers 2) Top Down Parsers 3) Bottom Up Parsers

- CYK Parsers uses CYK algos, also called universal parser.
- It can parse any kind of language.
- 红旗 They are inefficient for producing compilers / compiler generation

Top Down Parsers

- (Topdown)
- They generate Ptree starting from the start state
 - Bottom up starts with the string and works it way up to the start state
 - The TD parser work for subclass of grammar called LL grammar. [L to Right Scan, L definition]
 - The BU parser work for subclass of grammar called LR grammar [L to Right Scan, R derivation]
 - We read the tree from top to down, left to right.

Error Handling in Parsing Phase

There are 4 classes of errors.

- 1) Lexical Errors : misspelt words,
- 2) Syntactical Error : missing ; , unbalanced {}]
- 3) Semantic Error : Type mismatch
- 4) Logical Error: infinite loops.

Role of error Handler

- 1) Report errors clearly & accurately.
- 2) Recovery from errors quickly
- 3) When program is correct, it also needs to check that program is not slow.

Error Handling & Recovery

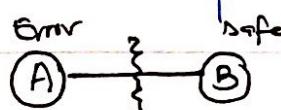
- 1) Report the error type/ diagnostic message and the location.
(if not exact then at least in the vicinity of the error)

Q3: On detecting error, how should a parser recover from it.

There are 4 strategies

- 1) Panic Mode Recovery
- 2) phased Recovery
- 3) Error Production
- 4) Global Correction

In order to recover, parser jumps from error to a state from where it can continue parsing.



Panic Mode Recovery

- In panic mode we skip the token and move to the next one till it reaches the delimiter. i.e. try find the next delimiter & then continue.
 - Look for a special token called ~~the~~ sync token eg delimiters.
 - The skipped part is not structurally checked by the parser.
- The simplest approach.

Phrase Recovery

- The parser adds some phrase that is expected for error free parsing
- This may lead to spurious errors. (due to addition & deletion by compiler) possibly ∞ errors.

Error Production

- Add Rule to handle the error into the grammar. These rules are called error productions.
eg to erase some chars. using ϵ moves.
- The most common

Global Correction

$$X \xrightarrow[G]{\text{state, grammar}} Y \quad \text{nearest correct}$$

- As minimum as possible no of transformations from an erroneous state X to Y using the Grammar G.

Notational Conventions

Grammar (Σ , NTPS)

- Nonterminals : Capital letters.
- terminals : initial small letters of the alpha (last letters used for string).
- Start : The LHS of 1st production, unless it's stated.
- Production

Grammatical Symbols (α, β, γ): These can be both NT, AP

$$S \xrightarrow{*} \alpha \quad (\text{sentential form } NT+T = \alpha\beta.\gamma)$$

[reach in k steps] sentence \rightarrow only terminals

$$S \rightarrow \alpha \quad [\text{reach in one step}]$$

Derivations & trees

At every step of derivation, we have 2 choices

1. which NT to expand.
2. Among all alternatives for NT in 1. which one to choose.

Ambiguity : A string for which multiple parse tree exist or more than one LMD or RND exist.

e.g.) $\alpha \xrightarrow[\text{LMD}]{*} \beta$ [α derives β using LMD]

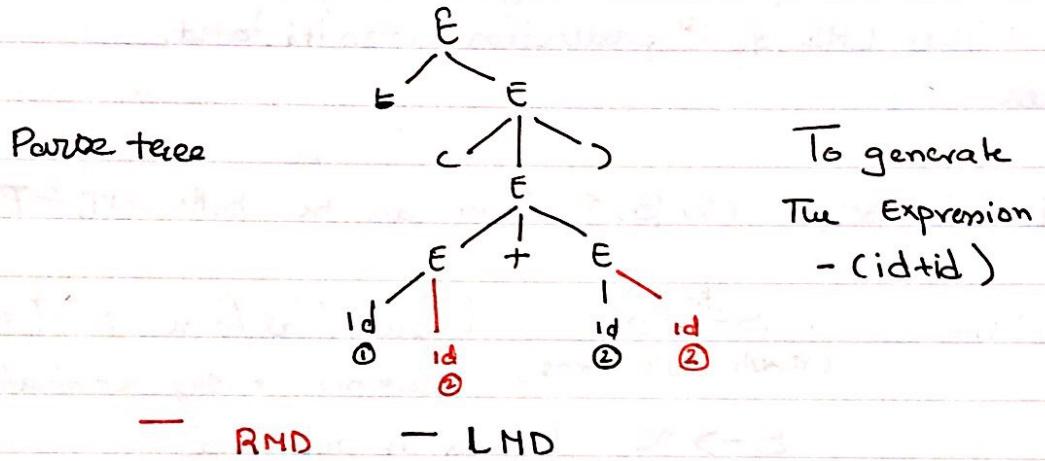
- o A parse tree ignores the variations in the order in which symbols are replaced.

e.g) $E \rightarrow E+E \mid (E) \mid -E \mid \text{id}$

$$E \rightarrow -E \rightarrow -(E) \rightarrow -(E+E) \xrightarrow{RMD} -(E+id) \rightarrow -(Id+Id)$$

LMD

$$\Downarrow -(Id+E) \rightarrow -(Id+Id)$$



- Every Parse tree has a unique leftmost derivation & unique RND but every sentence does not have
 - only ~~one~~ one parse tree
 - only one LMD
 - only one RMD

Eg : $E \rightarrow E+E \mid E*E \mid id$
 To generate $id + id * id$

LMD

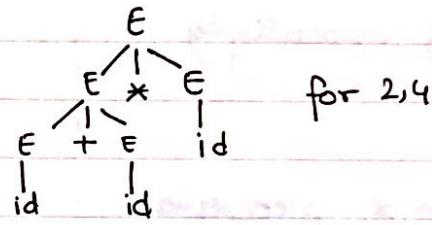
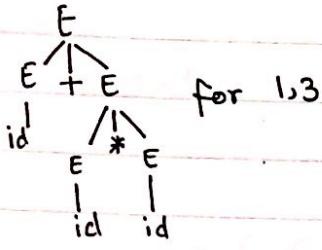
$$1. E \Rightarrow E+E \Rightarrow id+E \Rightarrow id + E*E \Rightarrow id + id * E \Rightarrow id + id * id$$

$$2. E \Rightarrow E*E \Rightarrow E+E*E \Rightarrow id + E*E \Rightarrow id + id * E \Rightarrow id + id * id.$$

RMD

$$3. E \Rightarrow E+E \Rightarrow E+E*E \Rightarrow E+E*id \Rightarrow E + id * id \Rightarrow id + id * id$$

$$E \Rightarrow E*E \Rightarrow E*id \Rightarrow E+E*id \Rightarrow E + id * id \Rightarrow id + id * id.$$



// Ambiguous Situation //

parser cannot decide which eee to pick.

Each tree has only one LND / RND, but not v.v.

Ambiguous if

1. more than one Parse Tree
2. more than one LND / RND

No parser can handle an ambiguous grammar except the operator precedence parser.

An ambiguous grammar can be converted to an unambiguous representation.

$$AG \xrightarrow[\text{Rules.}]{\text{disambiguation}} \bigcup_{\alpha} AG^{\alpha}$$

Reasons for Ambiguity

e.g. $id_1 + id_2 * id_2$

when we have operand b/w two operators parser cannot decide to which operator we can assign this operand to.

⇒ 1. The problem of associativity

2. ~~precedence~~

2. The problem of precedence

when multiple operands exists which to evaluate first.

Solution :

1. define correct associativity , "recursion" help in defining associativity
 2. Introduce levels in the grammar.
- # recursion → Left Recursion | Right Recursion
in order to remove ambiguity in associativity we put recursion but that can have problem of its own

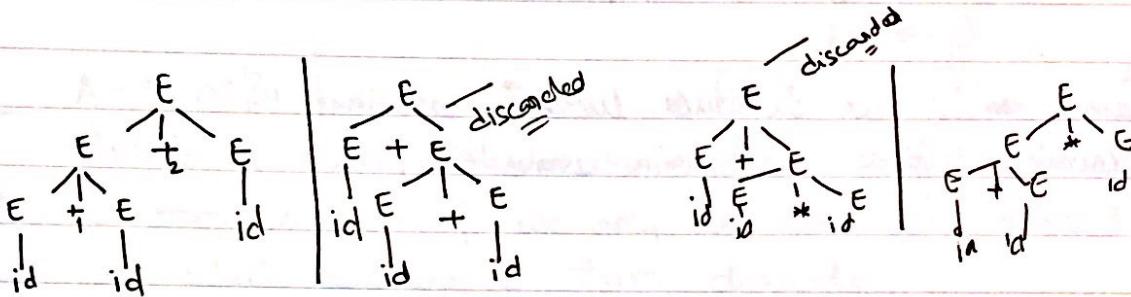
due to Left Recursion, Top DownParser goes into ∞ loop
this is solved by changing to Right Recursion.

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eg $id + id * id$

$id + id * id$

$$E \rightarrow E+E \mid E*E \mid id.$$



- # There are some operators which are both associative to left/right
- # \div is not both associative.
- # Left Associativity in a seq of ops L As means the leftmost operand is evaluated first. then next...
- # Generation vs Evaluation.
- # Every operator has a predefined associativity.

"How to enforce associativity?" (in ambiguous grammar)

"How to enforce precedence?" (" " " ")

"if we want an op to be left asso , we'll use left recursion & the Right recursion of Right asso."

1. $A \rightarrow A\alpha \quad || \text{Left recursion}$
2. $A \rightarrow \alpha A \quad || \text{Right "}$

To mala + Lasso.

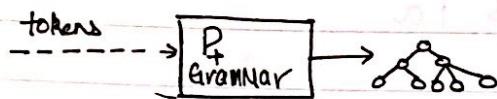
$$\begin{aligned}
 E &\rightarrow E + F \\
 = E &\rightarrow E + T \mid T \quad // \text{ now we have LHS} \\
 = T &\rightarrow T * F \mid F \\
 F &\rightarrow \text{id.} \quad G^* F \mid E \\
 G &\rightarrow \text{id.}
 \end{aligned}$$

To handle precedence : we introduce levels in grammar.
 generate highest level to evaluate it first.

$$\begin{array}{c}
 E \rightarrow E + E \mid E * E \mid \text{id.} \\
 E \rightarrow E + T \mid T \\
 E \rightarrow T * F \mid F \\
 F \rightarrow \text{id.}
 \end{array}$$

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Non-determinism



e.g. $A \rightarrow \alpha\beta_1 \mid \alpha\beta_2 \mid \alpha\beta_3$ (A)
this is an example of nondeterminism.

at a state (say A) if we only see some α ahead then we can't select any one of them directly.

N.D Left Factoring \rightarrow Determinism.

all A productions have a common prefix.

\therefore this is also called the common prefix problem

then we come to decision by delaying the selection of Right factor as

$$\begin{aligned} A &\rightarrow \alpha A' \\ A' &\rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \end{aligned}$$

Non determinism

- ↳ only the path is checked & we don't have the ans

Amiguity

- ↳ Two or more ways to reach the solution
- ↳ we have the answer.

$$D \not\Rightarrow UA$$

Ques $s = "iEtEtSeS"$.

$S \rightarrow iEtS \mid iEtSeS \mid a$
 $E \xrightarrow{a} b$

$S \rightarrow iEtS \rightarrow iEt iEtSeS \quad \textcircled{1}$

$S \rightarrow iEtSeS \rightarrow iEt iEtSeS \quad \textcircled{2}$

$\therefore Q$ is ambiguous.

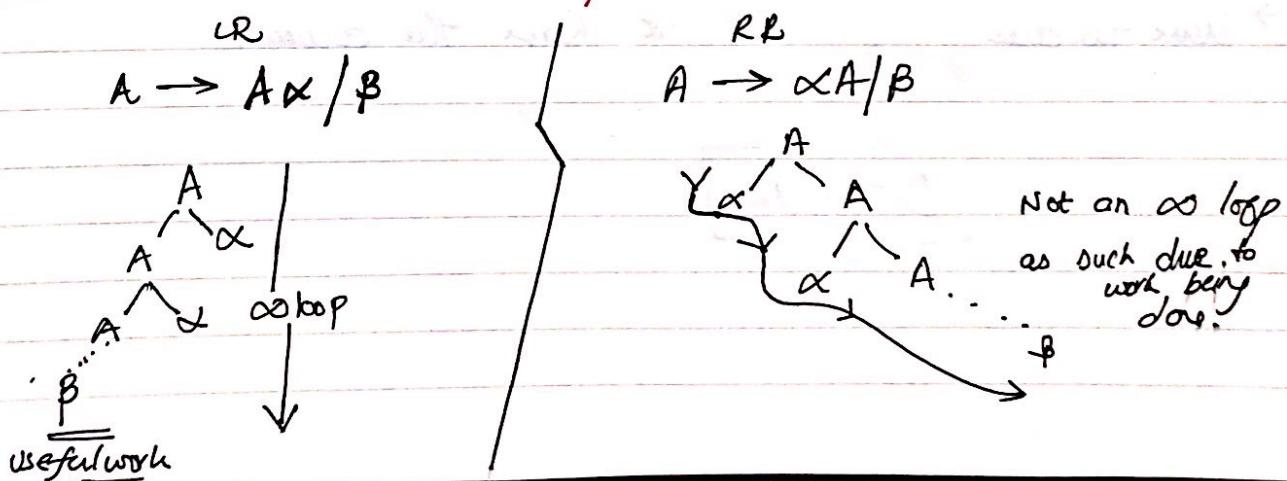
$S \rightarrow iEtSS' \mid a$
 $S' \rightarrow eS \mid \cancel{eSeS} \mid e$
 $E \rightarrow b$

$\begin{cases} \textcircled{1} \quad S \rightarrow iEtSS' \rightarrow iEt iEtSS' \rightarrow iEt iEtSeS \\ \textcircled{2} \quad S \rightarrow iEtSS' \rightarrow \cancel{iEt iEtSeS} iEtSeS \rightarrow iEt iEtSS'eS \rightarrow iEt iEtSeS \\ \hookrightarrow \text{Ambiguous.} \end{cases}$

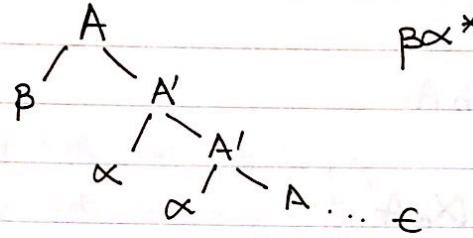
"Determinism doesn't imply unambiguity"

"Non determinism is a problem from parser that cannot backtrack."

• How does LR become a problem?



$$\begin{array}{l} A \rightarrow \beta A' \\ A' \rightarrow \alpha A' \mid \epsilon \end{array}$$



Left recursion is converted Right Recursion.

eg) $\begin{array}{l} E \rightarrow E + T \mid T \\ T \rightarrow T * F \mid F \\ F \rightarrow \text{id} \end{array}$

$$\begin{array}{l} E \rightarrow \alpha E \beta \mid \text{id} \\ E \rightarrow \end{array}$$

$$\begin{array}{l} E \rightarrow E \alpha \mid \beta T \\ T \rightarrow T \beta \mid F \\ F \rightarrow \text{id} \end{array}$$

Solution

$$\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow +TE'/\epsilon \\ T \rightarrow FT' \\ T \rightarrow *FT'/\epsilon \\ F \rightarrow \text{id.} \end{array}$$

$$\begin{array}{l} T \rightarrow TB \mid \text{id.} \\ T \rightarrow FT' \\ T \rightarrow *FT'/\epsilon \\ F \rightarrow \text{id.} \end{array}$$

Eg $A \rightarrow A\alpha_1 | A\alpha_2 | \dots | A\alpha_n | \beta_1 | \beta_2 | \dots | \beta_m$

\Rightarrow

$A \rightarrow \beta_1 A' | \beta_2 A' | \dots | \beta_m A'$

$A' \rightarrow \alpha_1 A' | \alpha_2 A' | \dots | \alpha_n A' | \epsilon$

This was an example of immediate left recursion.
There can also be ~~immediate~~ non immediate.

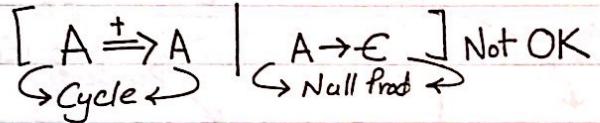
$\frac{A \rightarrow A\alpha | \beta | C}{C \rightarrow A\alpha | d}$
 \downarrow direct
 \downarrow non immediate recursion.

" We have an algo for converting LRG to RRG. "

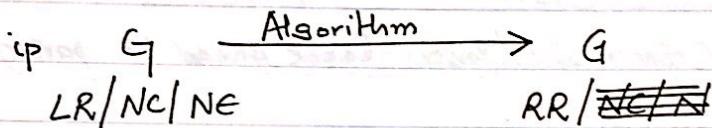
- It handles both immediate & non immediate recursions.
- When there are cycles in the grammar then this Algo fails & we cannot convert LRG to RRG.

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Algorithm to Convert Left Recursion / Remove Left Recursion



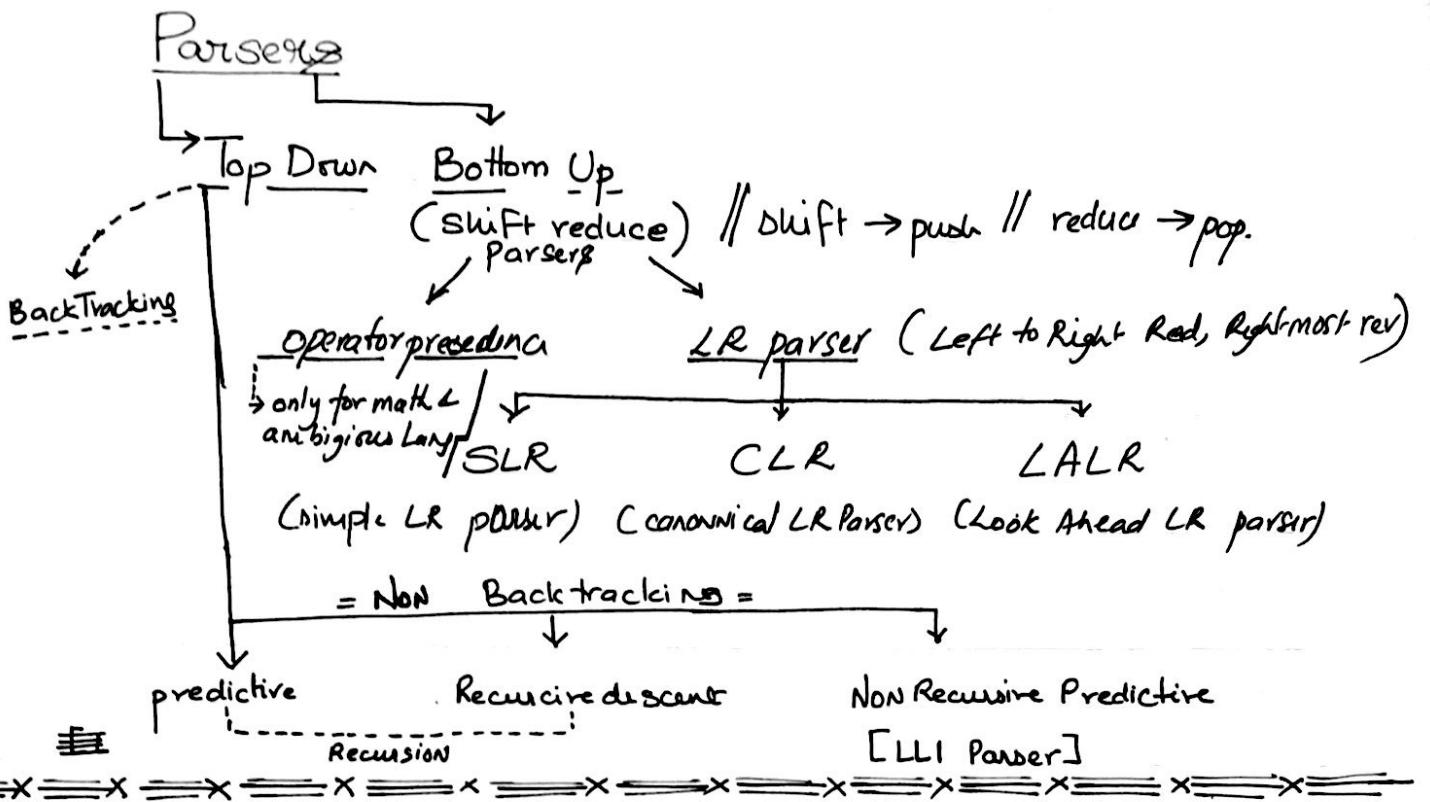
1. There Should Not be any cycles.
2. There Should Not be any ϵ production.



1. Arrange NT as A_1, \dots, A_n
2. for $i = 0$ to n do begin
 - 2.1 for $j = 1$ to $i-1$ do begin
 - 2.1.1 $\boxed{ }$
 - 2.2 end
 - 2.3 eliminate the immediate LR among the A_i productions.

2.1.1 Replace each $A_i \rightarrow A_j \gamma$ by the Prod $A_i \rightarrow \delta_1 \gamma | \delta_2 \gamma | \dots | \delta_k \gamma$
 where $A_j \rightarrow \delta_1 | \delta_2 | \dots | \delta_k$ are all current A_j prods.

eg) $S \rightarrow Aa | b$
 $A \rightarrow Ac | Sd | \epsilon$ [ϵ doesn't introduce recursion]



(eg) $S \rightarrow aABe \rightarrow A \rightarrow A \overset{1}{\rightarrow} \overset{2}{\rightarrow} \overset{3}{\rightarrow} \overset{4}{\rightarrow} \text{input} \rightarrow abb cde$

Top Down
CLL

$$\begin{aligned} S &\overset{1}{\Rightarrow} aABe \overset{2}{\Rightarrow} aAbcBe \\ &\overset{3}{\Rightarrow} abbcBe \overset{4}{\Rightarrow} abbcd \end{aligned}$$

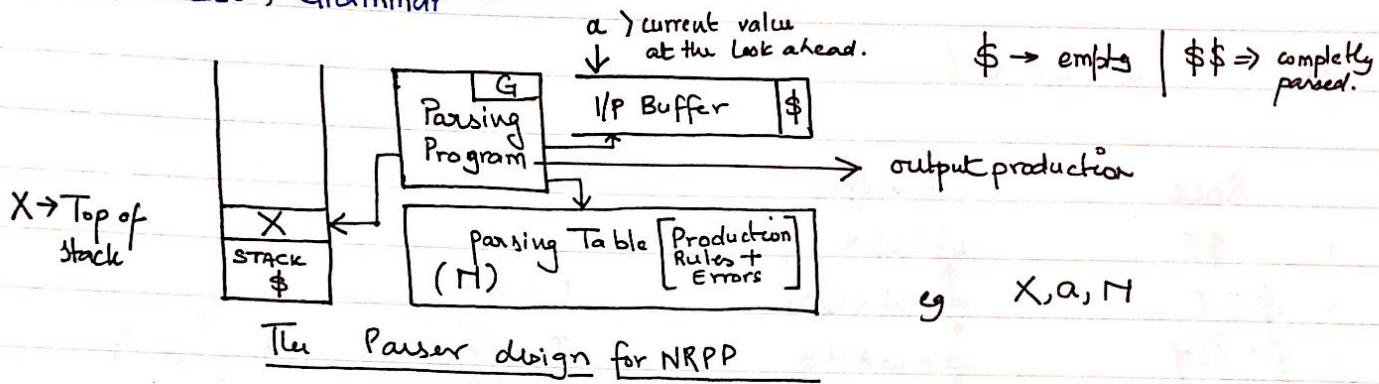
Bottom Up
CLR

$$\begin{aligned} S &\overset{1}{\Rightarrow} aABe \overset{2}{\Rightarrow} aAbcde \\ &\overset{3}{\Rightarrow} aAbcde \overset{4}{\Rightarrow} abbcde \\ &\overset{5}{\Rightarrow} abbcde \Rightarrow a \underline{Abc} de \Rightarrow a \underline{A} de \Rightarrow a ABe \Rightarrow S \end{aligned}$$

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Non Recursive Predictive Parser (LL(1) Parser)

- Unambiguous, Deterministic, Right Recursive.
- For LL(1) Grammar -



G:

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +TE' \quad / \quad -E \\ T &\rightarrow FT' \\ T' &\rightarrow *FT' \quad / \quad E \\ F &\rightarrow \text{id} \quad / \quad (E) \end{aligned}$$

M:	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \emptyset$	$E' \rightarrow E$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow +FT'$	$T' \rightarrow *FT'$		$T' \rightarrow E$	$T' \rightarrow E$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		

$T' \rightarrow E \quad T' \rightarrow *FT'$

Rules for making NRPP

- if $X = a = \$$ [X : Top of Stack a : input]
parser halts & announces success
- if $X = a \neq \$$
pop(X) and advance I/P to next symbol // only time IP is moved
- $F \quad X = NT$
consult $M[X, a]$

The entry will be X production of grammar / blank entry. $\xrightarrow{\text{error}}$

if the entry is blank, error recover is involved

if $M[X, a] = \{ X \rightarrow UVW \}$

Parser will replace X by W, V, U ($U @ \text{Top}$)

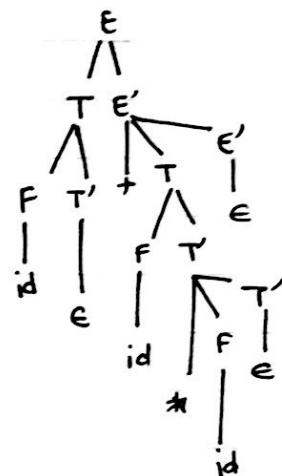
Since the parser has used some rule from the table.

← output the rule.

g) $id + id * id$

Stack	i/p buffer
1 \$E	id + id * id \$
2 \$ET	id + id * id \$
3 \$ETF*	id + id * id \$
4 \$ET'i*	id + id * id \$
5 \$E'	+ id * id \$
6 \$ET+	+ id * id \$
7 \$ET	id * id \$
8 \$ET'F	id * id \$
9 \$ET'i*	id * id \$
10 \$ETF*	* id \$
11 \$ET'i*	id \$
12 \$ET'	\$
13 \$E'	\$
14 \$	\$
→ <u>Paused</u>	

o/P
$E \rightarrow ET'E'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow E$
$E' \rightarrow +TE'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow *FT'$
$F \rightarrow id$
$T' \rightarrow e$
$E' \rightarrow e$
—



The o/p:

~~E / / / / / / / / E'~~

Computation first and follow
Construction of table using
first and follow

$$\begin{aligned}
 E &\Rightarrow TE' \\
 &\Rightarrow FT'E' \\
 &\Rightarrow idT'E' \\
 &\Rightarrow idE' \\
 &\Rightarrow id + TE' \\
 &\Rightarrow id + FT'E' \\
 &\Rightarrow id + idT'E'
 \end{aligned}$$

$(id + id \xrightarrow{*} FT'E')$
 $id + id \xrightarrow{*} idT'E'$
 $id + id \xrightarrow{*} idE'$
 $\underline{id + id \xrightarrow{*} id}$

A \rightarrow Bay | α

B \rightarrow CD

C \rightarrow Afc ($C \rightarrow A|_c$)

D \rightarrow d

20/2/18

Apply the rules to calculate first(X) until no more terminals or ϵ can be added to

First(X) (First(X))
↳ can be anything Better Method

Rule 1: if X is a terminal, then First(X) = { X }

Rule 2: if $X \xrightarrow{*} \epsilon$ is a production, then add ϵ to First(X)

Rule 3: if X is a non-terminal and $X \rightarrow Y_1, Y_2 \dots Y_n$ is a production then place 'a' in First(X) if for some i , a is in First(Y_i) and ϵ is in all of first(Y_1) to first(Y_{i-1}) i.e. $Y_1, Y_2 \dots Y_{i-1} \xrightarrow{*} \epsilon$

if ϵ is in First(Y_j) for all $j = 1, k$ then add ϵ to First(X)

- if α is any string then First(α) is the set of terminals that begins the strings derived from α
- if $\alpha \xrightarrow{*} \epsilon$ then ϵ will also be in First(α).

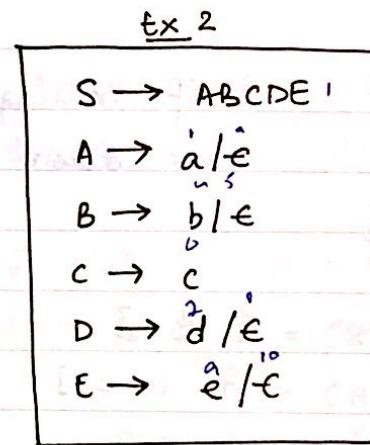
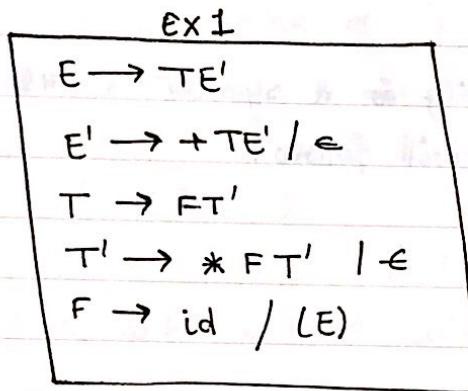
→ N.T only.

Follow(X)

- place \$ in follow(S) where ' S ' is the start symbol and \$ is the end marker
- If there is a production $A \rightarrow \alpha B \beta$ then everything in First(B) except ϵ is placed in follow(B)
- If there is a production $A \rightarrow \alpha B \beta$ or $A \rightarrow \alpha B$ where First(B) contains ϵ then everything in follow(A) is in follow(B).

Follow (X) for Non-terminal X is the set of terminals that appear immediately to the right of X in some substituted form

Example



$$\text{First}(+) = \{ + \}$$

$$\text{First}(\ast) = \{ \ast \}$$

$$\text{First}(id) = \{ id \}$$

$$\text{First}(,) = \{ , \}$$

$$\text{First}()) = \{) \}$$

}

First of all terminals.

①

$$\text{First}(S) = \{ a, b, c \}$$

$$\text{First}(A) = \{ A, \epsilon \}$$

$$\text{First}(B) = \{ B, \epsilon \}$$

$$\text{First}(C) = \{ C \}$$

$$\text{First}(D) = \{ D, \epsilon \}$$

$$\text{First}(E) = \{ E, \epsilon \}$$

②

$$\text{First}(E') = \{ +, \epsilon \} \quad \{ id, (\}$$

$$\text{First}(E') = \{ +, \epsilon \}$$

$$\text{First}(T) = \{ id, (\}$$

$$\text{First}(T') = \{ *, \epsilon \}$$

$$\text{First}(F) = \{ id, (\}$$

$\text{Follow}(E) = \{ \$,) \}$

$\text{Follow}(E') = \{ \$,) \}$

$\text{Follow}(T) = \{ +, \$,) \}$

$\text{Follow}(T') = \{ +, \$,) \}$

$\text{Follow}(F) = \{ *, +, \$,) \}$

if nothing is following ~~is~~ a symbol in RHS
that doesn't mean \$ will follow.



$\text{Follow}(S) = \{ \$ \}$

$\text{Follow}(A) = \{ b, c \}$

$\text{Follow}(B) = \{ c \}$

$\text{Follow}(C) = \{ d, e, \$ \}$

$\text{Follow}(D) = \{ e, \$ \}$

$\text{Follow}(E) = \{ \$ \}$

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Construction of predictive parsing table

Input grammar 'G', the output is 'N'

1. For each $A \rightarrow \alpha$ of G do 2., 3.
2. For each terminal 'a' in $\text{First}(\alpha)$ add $A \rightarrow \alpha$ to $N[A, a]$
3. if ϵ is in $\text{First}(\alpha)$, then add $A \rightarrow \alpha$ to $N[A, \epsilon]$ for each terminal 'b' in $\text{Follow}(A)$
if ϵ is in $\text{First}(\alpha)$ and $\$$ is in $\text{Follow}(A)$ add $A \rightarrow \alpha$ to $N[A, \$]$
4. Make each undefined entry of N to be an error (blank)

	id	+	*	()	\$	
E	$E \rightarrow TE'$			$E \rightarrow TE'$			$E \rightarrow TE'$
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$	$E' \rightarrow +TE'/\epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$			$T \rightarrow FT'$
T'		$T' \rightarrow *ET'$	$T' \rightarrow xFT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$	$F \rightarrow id / ($
F	$F \rightarrow id$			$F \rightarrow (\epsilon)$			

	a	b	c	d	e	\$
S	$S \rightarrow ABCDE$	$S \rightarrow ABCDE$	$S \rightarrow ABCD\epsilon$			
A	$A \rightarrow a$	$A \rightarrow \epsilon$	$A \rightarrow \epsilon$			
B		$B \rightarrow b$	$B \rightarrow \epsilon$			
C			$C \rightarrow c$			
D				$D \rightarrow d$	$D \rightarrow \epsilon$	$D \rightarrow \epsilon$
E					$E \rightarrow e$	$E \rightarrow \epsilon$

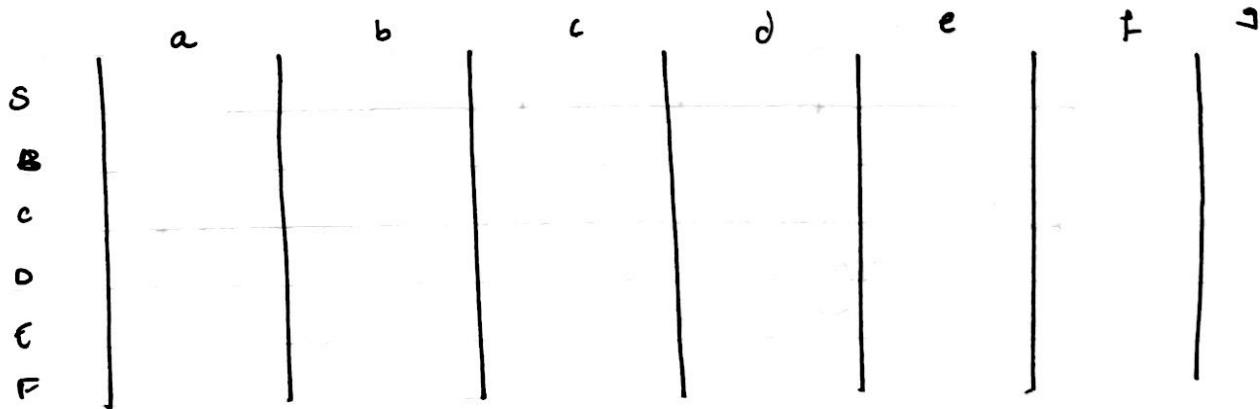
Example

$$\begin{aligned}
 S &\rightarrow a \text{ BD } h \\
 B &\rightarrow cC \\
 C &\rightarrow bC / \epsilon \\
 D &\rightarrow EF \\
 E &\rightarrow g / \epsilon \\
 F &\rightarrow f / \epsilon
 \end{aligned}$$

$$\begin{aligned}
 \text{first}(S) &= \{ a \} \\
 \text{First}(B) &= \{ c \} \\
 \text{First}(C) &= \{ b, \epsilon \} \\
 \text{First}(D) &= \{ g, f, \epsilon \} \\
 \text{First}(E) &= \{ g, \epsilon \} \\
 \text{First}(F) &= \{ f, \epsilon \}
 \end{aligned}$$

Mid: ~~NP~~ Predictive Parser (NRPP)
 Top down complete C-recursion complete
 Ambiguity | PDA
 UNIT - 1 \oplus Test for LL₁ ::
 UNIT - 2 (General theory)
 \neq [[DFA (minimize/solve)]]
 NFA \rightarrow DFA (possible)!
 [CFG \oplus (PPA)]

$$\begin{aligned}
 \text{Follow}(S) &= \{ \$, \} \\
 \text{Follow}(B) &= \{ g, f, h \} \\
 \text{Follow}(C) &= \{ g, f, h \} \\
 \text{Follow}(D) &= \{ \} \\
 \text{Follow}(E) &= \{ f, \epsilon \} \\
 \text{Follow}(F) &= \{ \} \Sigma
 \end{aligned}$$

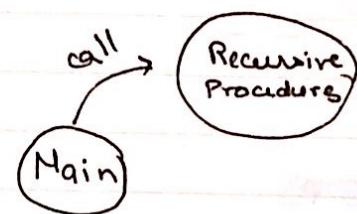


Recursive Descent Parser

- No backtracking.
- Top down.
- Use of recursive procedures for each N.T.
- Predictive.

$$E \rightarrow id E'$$

$$E' \rightarrow *id E' / -e$$



```
main ()
{
    E();           //①
    if (l == $) //②
        print "success"; //③
}
```

// l → lookahead pointer

```
E()
{
    if (l == id)
        {
            Advance('id');
            E();
        }
}
```

```
E'
{
    if (l == *)
        {
            Advance('*'); ← Add if
            Advance('id');
            E();
        }
    else
        return
}
```

Advance (t)

{

```
if (l==t)
    l = getchar();
else
    print(error);
```

}

// call the LA for the next
// token.

// t = expected input

Example

input : id * id \$

Advance

id * id \$
↑
→ id * id \$

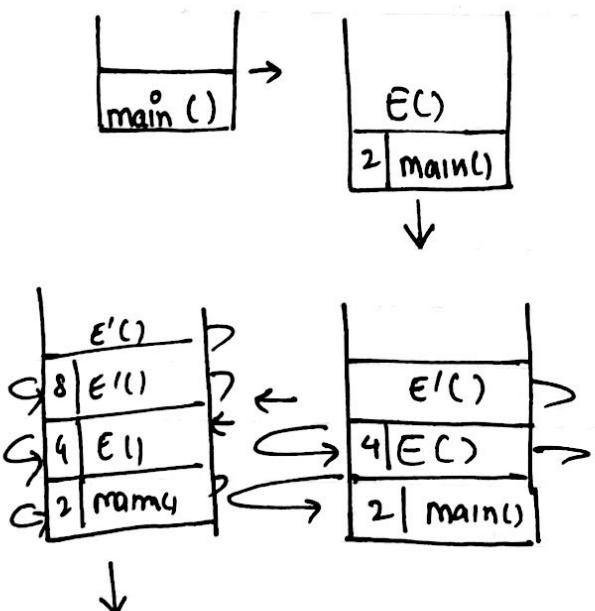
i = *

Advance

id * id \$
↑
→ id * id \$

Advance

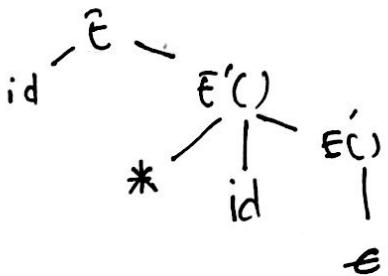
id * id \$
↑
→ id * id \$



E'
8 | E()
4 | E()
2 | main()

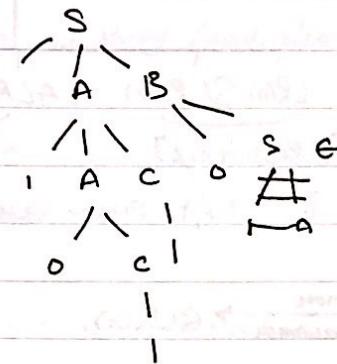
E'
4 | E()
main

E'
2 | main() $\rightarrow \times$



1101

1101 1101000 110100
x xx xxy
main() → S() → A() → C() →



17 Error Recovery in LL(1) Parser (Top Down Parser)

$$E \rightarrow TE'$$

$$E' \rightarrow +TE' \mid \epsilon$$

$$T \rightarrow FT'$$

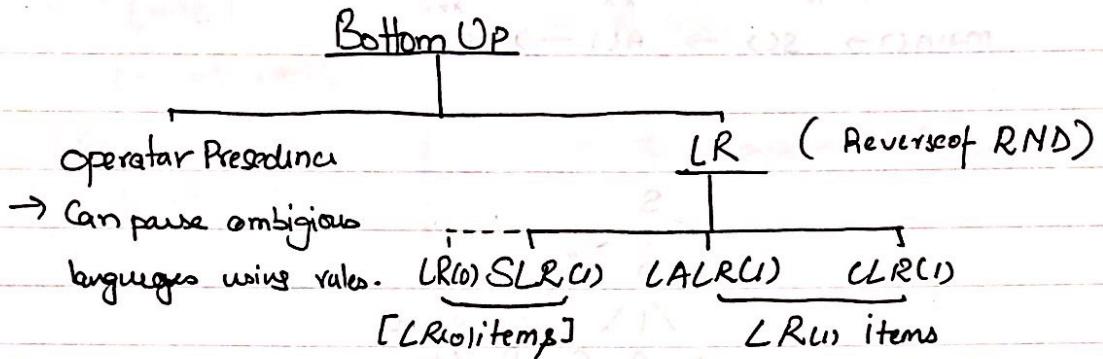
$$T' \rightarrow *FT' \mid \epsilon$$

$$F \rightarrow id \mid (E)$$

eg) $S \rightarrow TA/PQ/\epsilon$

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Bottom-Up Parsers



They're also called SR parser i.e Shift (Push) and reduce (Pop).

$\underline{LR(0)}$ $\xrightarrow[\text{Drawback}]{\text{Remove}} \text{SLR}(1)$.

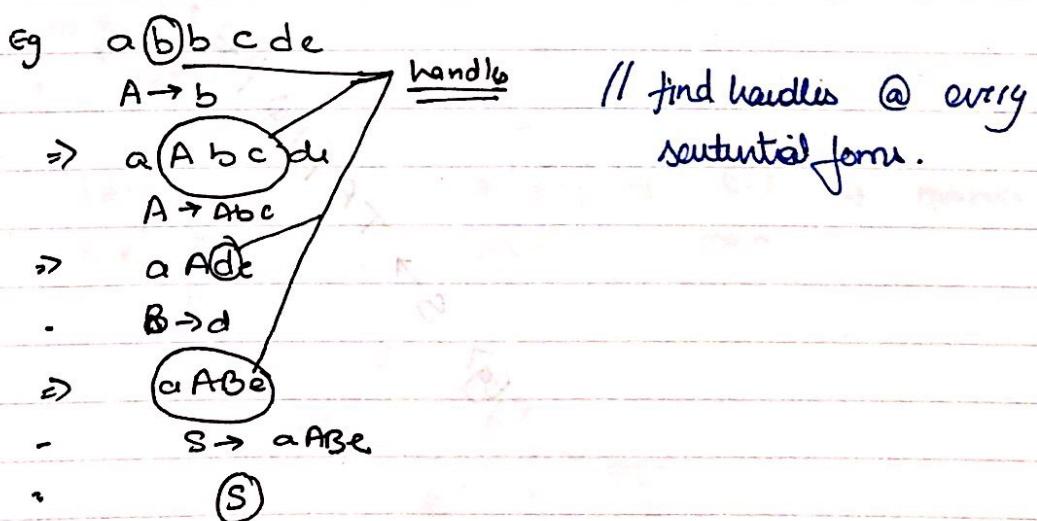
$$S \rightarrow aABe$$

$$A \rightarrow Abc$$

$$A \rightarrow b$$

$$B \rightarrow d$$

given abbode // Handle
 aA b c de The substring which is chosen
 a A de for reduction.
 a ABe
 S // RHS is reduced to LHS



// The grammar must be unambiguous.

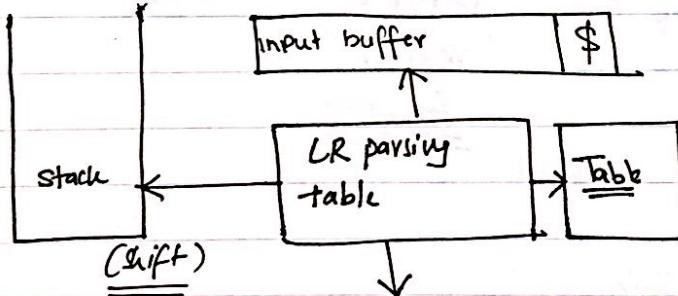
Goals of LR parser

1. When to reduce
2. What to use i.e. what Reduction to do.

// handle a name given to a substring / production which will ultimately give S //

Construction is such that the handle will automatically be on top of the stack.

Stack implementation for LR parsers



State	action								Goto	handle (reduction)		
-	id	+	x	()	\$	E	T	F			
0	S ₅						1	2	3			
1	S ₆					Acc						
2	q ₂	S ₂		q ₁₂	q ₁₂							
3	q ₄	q ₄		q ₄	q ₄							
4	S ₃		S ₄				8	2	S			
5	q ₆	q ₆	q ₆	q ₆	q ₆							
6	S ₅		S ₄					9	3			
7	q ₅	S ₃						10				
8	S _L			S ₁₁								
9	q ₁	S ₇		q ₁	q ₁₁							
11	q ₃	q ₃		q ₃	q ₃							
12	q ₅	q ₅		q ₅	q ₅							

r₂ → reduce using 2.

S₅ → Shift with 5 state on top.

more input buffer curr to top

E → E + T → ①

E → T - ②

T → T * F - ③

T → F - ④

F → (E) - ⑤

F → id - ⑥

Stack	Input	Output
O	id + id * id \$	Shift
0 id 5	↑ id + id * id \$	reduce $F \rightarrow id$
0 F 3	↑ + id * id \$	reduction ④ $T \rightarrow F$
0 T 2	+ id * id \$	reduce ② $E \rightarrow T$
0 E 1	+ id * id *	Shift
0 E 1 + 6	id * id \$	Shift
0 E 1 + 6 id 5	* id \$	reduce ⑥
0 E 1 + 6 F 3	* id \$	reduce ④
0 E 1 + 6 T 9	* id \$	Shift
0 E 1 + 6 T 9 * 7	id \$	Shift
0 E 1 + 6 T 9 * 7 id 5	\$	reduce 6
0 E 1 + 6 T 9 * 7 F 10	\$	reduce ⑧ $T \rightarrow \underline{T * F}$
0 E 1 + 6 T 9	\$	reduce ①
0 E 1	\$	<u>Accept</u>

- ▷ Construction of SLR(1)
- ▷ Canonical derivation diagram.

2/4/18

Construction of SLR(1) parse table

Items & Closures

"Canonical Collection of LR(0) items"

Items: A production having a '.' in the RHS of the production.
The dot tells what we have seen and what is left.

$S \rightarrow \cdot AA$ [AN ITEM]

$S \$$ or $E \$$ is our accepting condition

To support this we have augmented grammar.

Grammar + Start' { $G + S' = Aug_1$ }

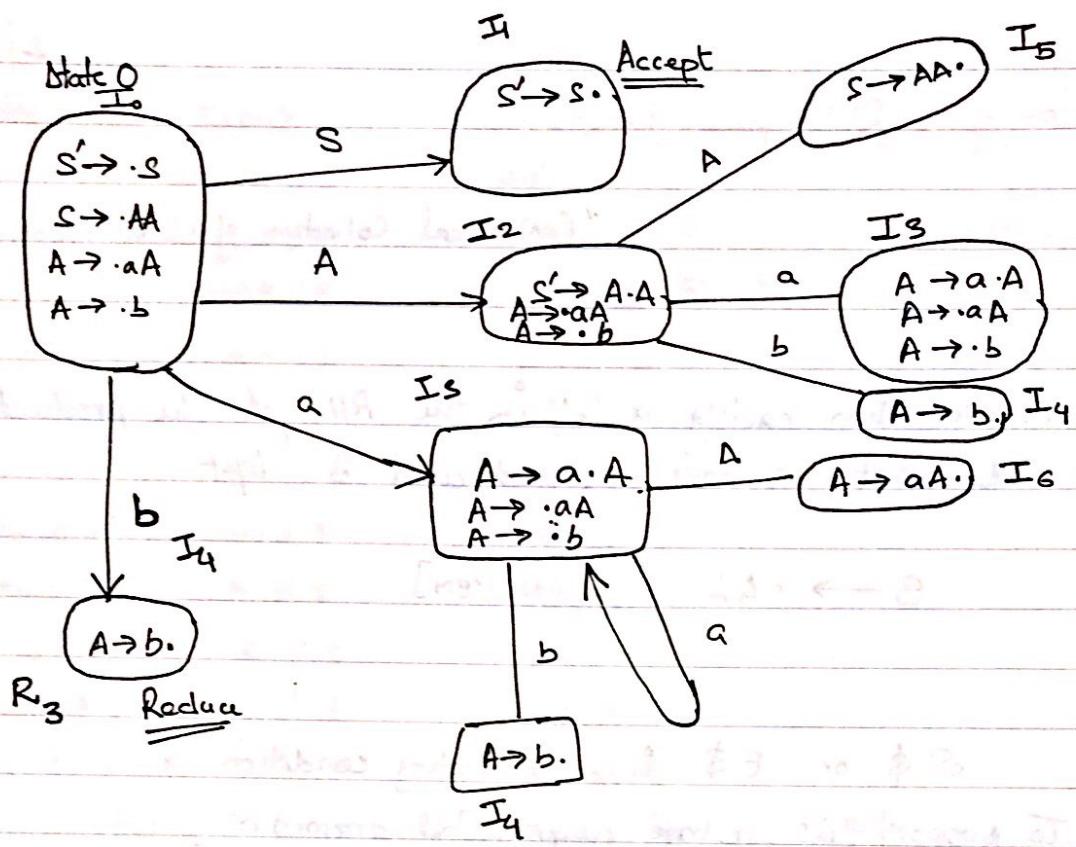
$S \rightarrow AA$] make SLR(1) table
 $A \rightarrow aA \mid b$

1. Make Aug grammar

$S' \rightarrow S$] Aug
① $S \rightarrow AA$ ② $A \rightarrow aA \mid b$

Closure If there is "•" immediate left to N.T then add all prod of that N.T by putting a "•" in the extreme of RHS of production





Stat	a	Action	b	\$	A ^{Look}	S
0	S3					
1				Accept		
2	S3		S4			
3	S3		S4			
4	q3		q3	q3		
5				q1		
6	q2		q2	q2		1

Filling Reduction rule in SLR(1) table

Fill the reduce moves in follow of non-terminal on LHS of the production used in reduction

$$\text{follow}(A) = \{a, b, \$\}$$

productions with $c \rightarrow$ in extreme right are called final items.

The \circ in SLR(0) item means look ahead does not matter.

aabb\$ check LR₁ parser.

stk

0 aabb\$ out

0 a³

0 a³ a³ b⁴

There are certain problems called conflicts i.e. to shift/reduce.
(shift + reduce in same state) and reduce/reduce conflicts.

These are done using conflict resolution regimes.

"Construct SLR(1) for the grammar in Assignment 1"

Unit : Memory Allocation (4)
Ch : Symbol Table Management
from Rajni Jindal Book

4/4/18

Construction of CLR(1) parse table

- Here we use a LR(1) item = LR(0) item + look-ahead.

$A \rightarrow \cdot Bb, a/b \rightarrow \text{LR}(1) \text{ item.}$

Reduction is based on the look-ahead.

$$S' \rightarrow S$$

$$S \rightarrow AA$$

$$A \rightarrow aA$$

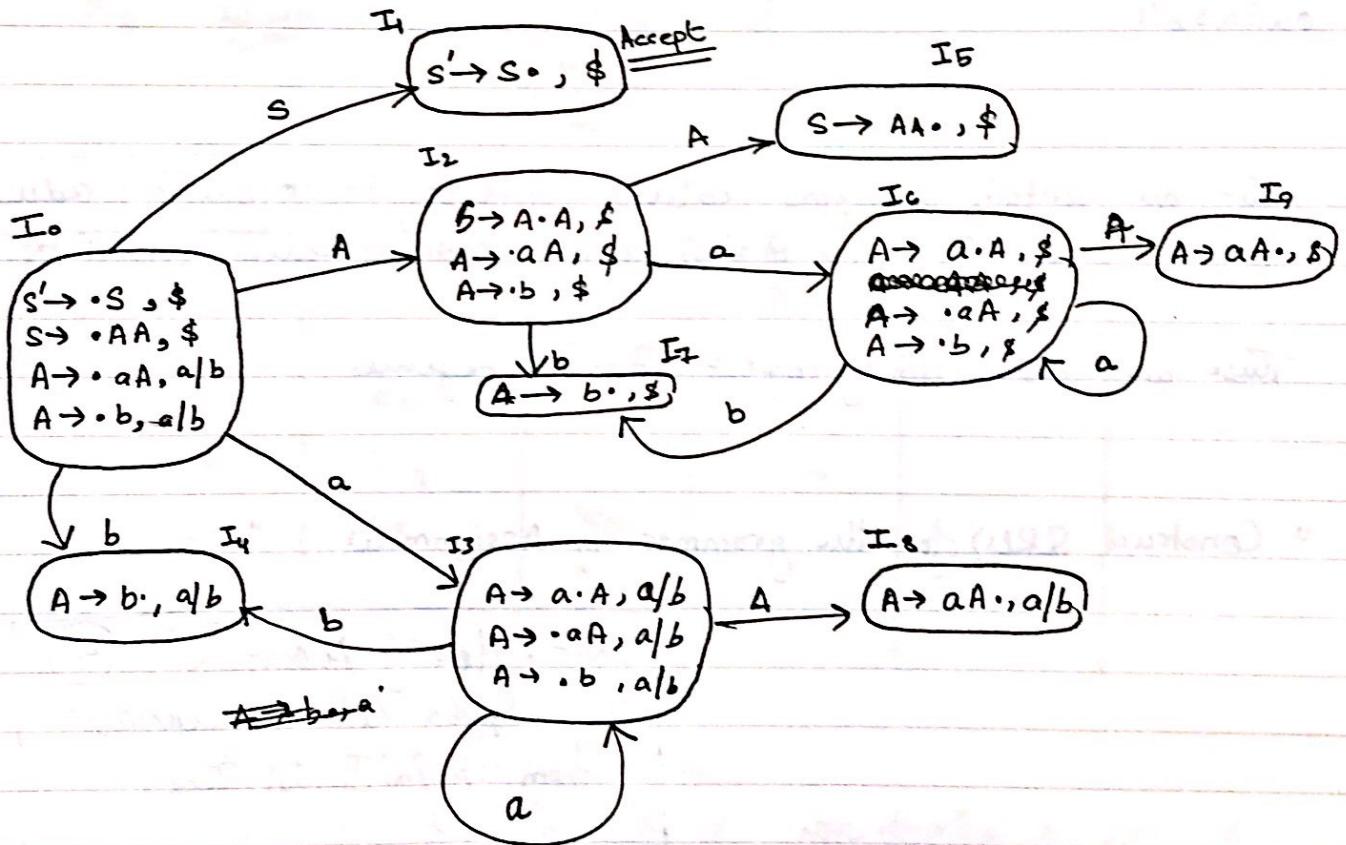
$$A \rightarrow b$$

1. Look ahead does not change on transition between states.

2. If look ahead, it is while computing closure.

if there is $A \rightarrow \alpha \cdot B \beta, a/b$, ~~B~~ = $\text{LL}(1)$

To find closure B , LC is first of RHS of B



State	a	Action b	#	A Goto	S
0	S_3	S_4		2	1
1			Acc		
2	S_6	S_7		5	
3	S_3	S_4		8	
4	q_3	q_3			
5			q_4		
6	S_6	S_7		9	
7			q_3		
8	q_2	q_2			
9			q_2		

"There is a conflict in CLR(1) parser."

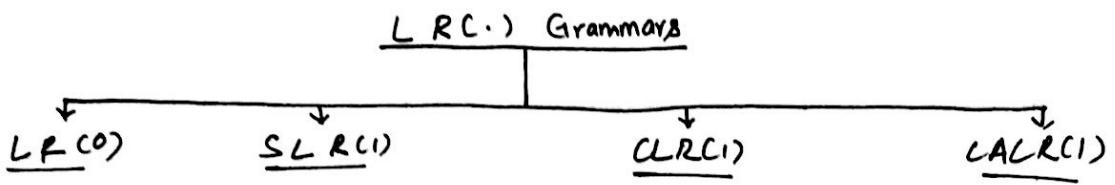
$$\# A \rightarrow C \\ ikm = A \rightarrow \cdot$$

Construction of LALR(1) Parse Table.

1. combine state 6 & 3 & replace all instances with combined.
2. combine 4, 7.
3. combining criteria: if the LR(0)s are same then combine.

	a	b	#	A	S
0	S_{3C}	S_{47}		2	1
1			Acc		
2	S_{36}	S_{47}		5	
3,6	S_{36}	S_{47}		8,9	
4,7	q_3	q_3	q_3		
5			q_4		
8,9	q_2	q_2	q_2		

If there is a conflict, then the grammar is not that type.



Eg> $S \rightarrow AaBb$
 $S \rightarrow BbBa$
 $A \rightarrow \epsilon$
 $B \rightarrow \epsilon$

$I_0 =$

$S' \rightarrow \cdot S$
 $S \rightarrow AaBb$
 $S \rightarrow BbBa$
 $\begin{cases} A \rightarrow \cdot \\ B \rightarrow \cdot \end{cases}$

→ R/R conflict

SLR(1)

I_0

$S' \rightarrow \cdot S, \$$
 $S \rightarrow \cdot AaBb, \$$
 $S \rightarrow \cdot BbBa, \$$
 $\begin{cases} A \rightarrow \cdot, a \\ B \rightarrow \cdot, b \end{cases}$

→ NoConflict

CLR(1)

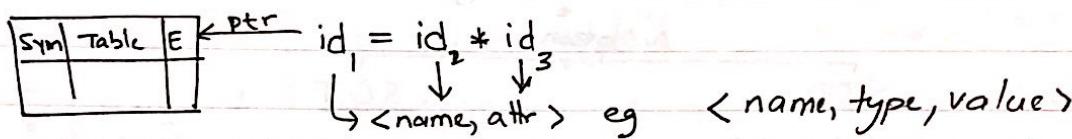
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Semantic Analysis

- ↳ CFG
- ↳ Semantic Rules

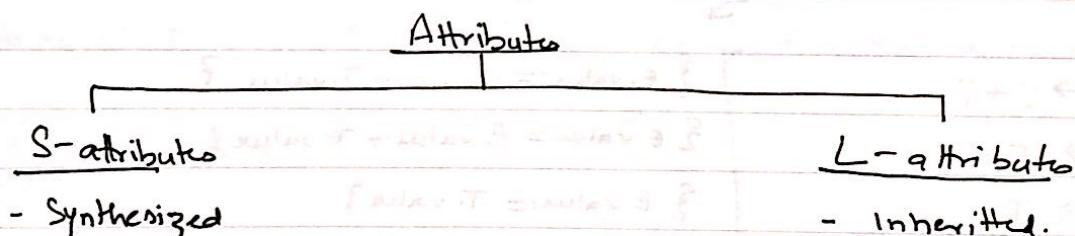
For info which cannot be covered by CFG & eg types, scopes.

"Attributes" each element has one.



- Attaching meaning to the productions.

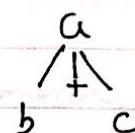
For attaching extra info with prog construct we associate semantic attr/ rules with grammar symbols/ production



With every symbol there is at least one attribute. But exception do exist depending on implementation

S-Attributes

The value of S attributes depends on the attributes of children



a depends (b, c)

S-attributes def can evaluated bottom up.

L-attribute

The value depends on value of parent or left siblings.

→ can be done by both TD and BC parser

There are two notations for associating semantic rules.

Notation

SDD

SDT

→ syntax Directed Def

→ syntax directed Translation

Sem Ana is not an independent phase but happens with the parser.

S.D.D

Action
↓

$E \rightarrow E + T$

$E \rightarrow E - T$

$E \rightarrow T$

$T \rightarrow T/F \quad [\div]$

$T \rightarrow T * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow \text{num}$

{
 $E.\text{value} := E.\text{value} + T.\text{value}$
 $E.\text{value} := E.\text{value} - T.\text{value}$
}
 $E.\text{value} := T.\text{value}$
 $T.\text{value} := T.\text{value} \div F.\text{value}$
 $T.\text{value} := T.\text{value} * F.\text{value}$
 $F.\text{value} := F.\text{value}$
 $F.\text{value} := E.\text{value}$
 $F.\text{value} := \text{num.value / or / lexical value}$

The syntax → Defines Action

we always write the action extreme right

S.D.D does not specify the time of execution of action.
It is only an abstract way to show action.

S.D.T specifies the time of execution of instruction

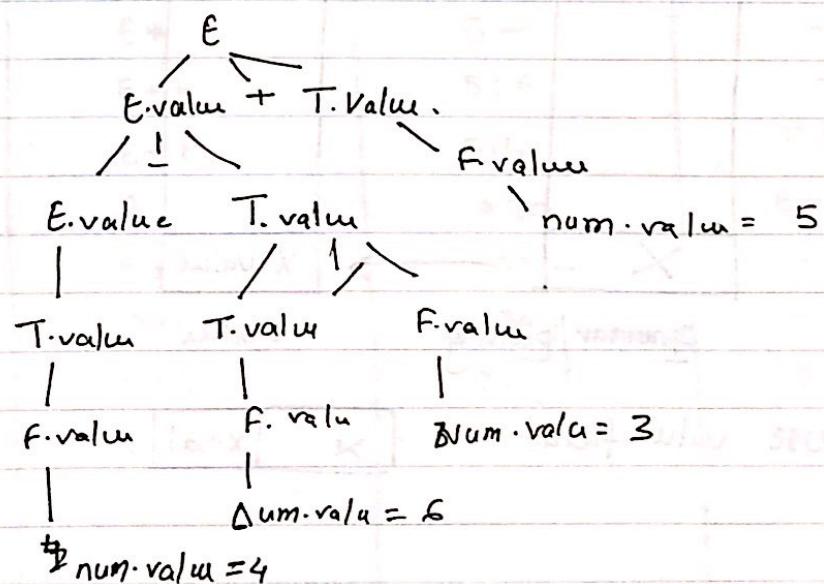
Grammar for Declarative statements

$D \rightarrow T \text{ list } \{ \text{list.type} := T.\text{type} \}$ [inherited] [Sibling]
 $\text{list} \rightarrow \text{list},, \text{id} \{ \text{list.type} := \text{list.type} \} \{ \text{id.type} = \text{list.type} \}$
 $\text{list} \rightarrow \text{id.} \{ \text{id.type} := \text{list.type} \}$ [parent]
 $T \rightarrow \text{int} \{ T.\text{type} = \text{int} \}$
 $T \rightarrow \text{float} \{ T.\text{type} := \text{float} \}$

Every S-att definition is always an L-attributed defⁿ.

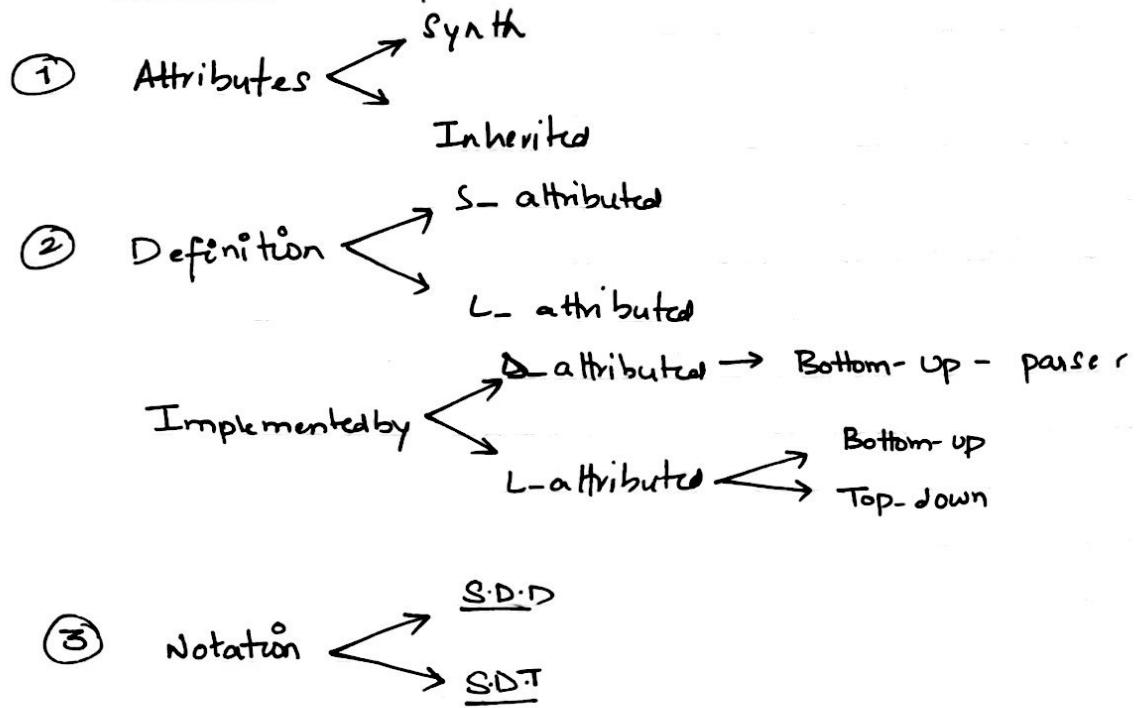
Annotated Parse Tree: Parse tree but with actions.

Eg $4 - 6 / 3 + 5$



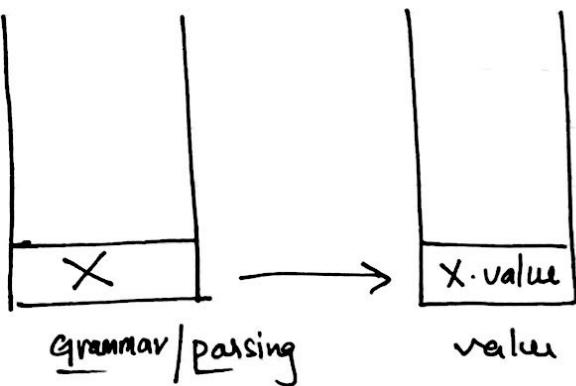
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Semantic Analysis



- S-attributed B-U Parser

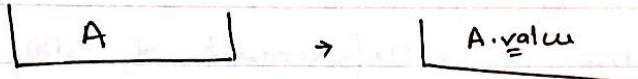
⇒ USE TWO STATES



⇒ USE value field



After Reduction



Blank entries in value stack (due to operators) are not errors

If we have K symbol on RHS of production Then p Top is $(Top - K + 1)$

$S \rightarrow id := E$	{ value [n-top] := value [top] }
$E \rightarrow E_1 + E_2$	{ value [top'] = value [Top-2] + value [Top] }
$E \rightarrow E_1 * E_2$	{ value [top'] = value [top-2] + value [Top] }
$E \rightarrow -E_1$	{ value [top'] = -value [top] }
$E \rightarrow id$	{ value [top] = value [id] }

i/p	a=5 b=6 c=2	Pass	value	Reduce.
a * b + c		-	-	-
a * b + c		a	5	-
* b + c		E	5	$\epsilon \rightarrow id$
* b + c		$\epsilon *$	5 -	-
b + c		$E + b$	5 6	-
+ c		$E + E$	5 6	$E \rightarrow id$
+ c		E	5 6	$E \rightarrow E * E$
c		$E +$	30 ~	-
-		$E + C$	30 2	-
		$E + E$	30 2	$E \rightarrow id$
		E	32	$E \rightarrow E + E$
-	-	-	-	-

Translation Schemes (S.D. Translation)

A translation scheme is a refinement of SDD, in which semantic actions are enclosed b/w braces & inserted within RHS of production to specify the exact time when actions are to be executed.

Eg - $E \rightarrow E + T \{ \text{Print}(+) \} \alpha$
 $E \rightarrow T \{ \}$
 $T \rightarrow id \{ \text{print}(id.value) \}$

} S.D.D for Post fix

Algo generate IC

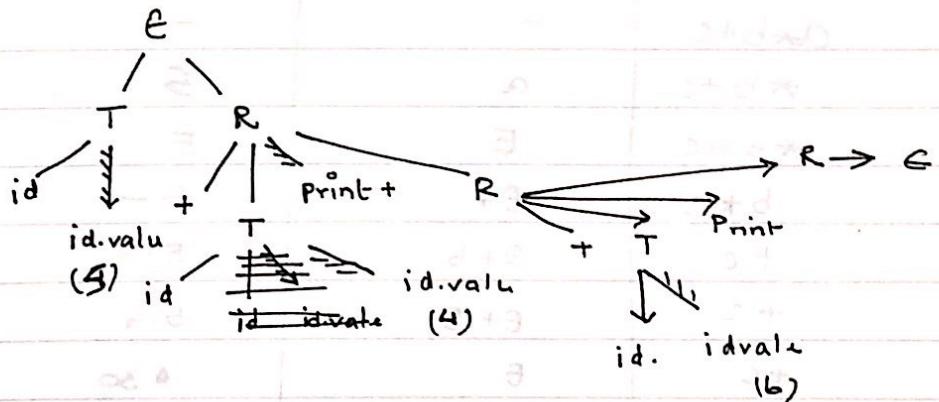
$E \rightarrow TR$

$R \rightarrow +T \{ \text{print}(+) \} R / E$

$\overline{\overline{T \rightarrow id \{ id.value \}}}$

$T \rightarrow id \{ id.value \}$

Eg: $5 + 4 + 6$



5 4 + 6 +

Guidelines for writing translation Schemes

Pg 136 ~~≡~~ Rajni

// Top-Down - L no longer with us RIP //

11/4/18

Implementation of L-attributed with Bottom-Up

'Marker Non-Terminal' whenever there is an action [Inherit] b/w

X_{k-1} and X_k we will put a Marker NT in the place
of the action & add $\underline{N} \rightarrow \in \{\}$ N is marker.

$$E \rightarrow X Y$$

$$Y \rightarrow + X \{ \} Y / \in$$

$$X \rightarrow \text{id } \{ \text{ print(id.value) } \}$$

Changing to Marker augmented

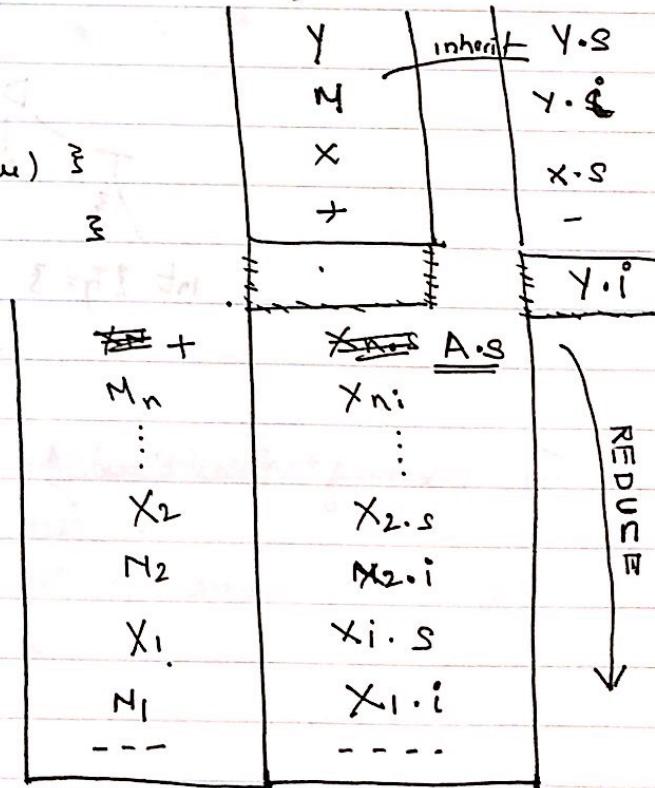
$$E \rightarrow X Y$$

$$Y \rightarrow + X N_1 Y / \in$$

$$X \rightarrow \text{id } \{ \text{ print(id.value) } \}$$

$$N_1 \rightarrow - \in \{ \}$$

eg) $A \rightarrow N_1 X_1 \dots N_n X_n$



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$$D \rightarrow T \{ L_{in} = T.type \} L$$

$L \rightarrow \{ id.type := L.type \} \{ id \in L \} \{ L.i = L.in \} L$

L → ←

$T \rightarrow \text{int} \quad \{ T.\text{type} = \text{int} \}$

Marlony

D → THIL

$$L \rightarrow M_2 \text{ id } M_3 L_1$$

L → e

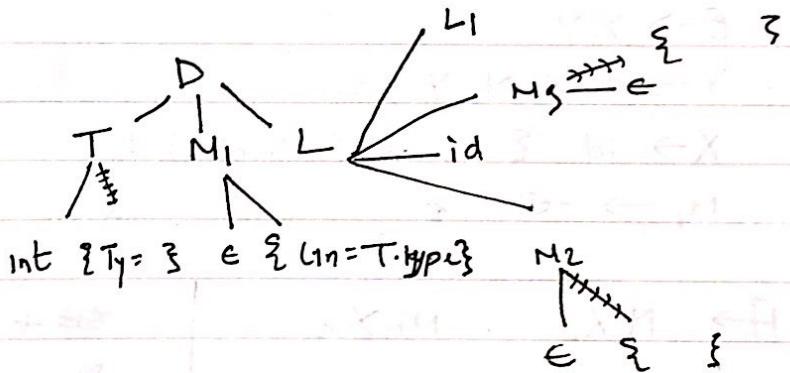
$T \rightarrow \text{int}$

$H_1 \rightarrow e^- \{ L_{lh} = T, \text{type } 3 \}$

$\text{H}_2 \rightarrow \epsilon \quad \{ \text{id} \cdot \text{Type} := \text{L-Type} \}$

$$M_3 \rightarrow \epsilon \quad \{ L_{1,m} = L_{1,n} \}$$

$M_4 \rightarrow \epsilon$ { T.type = int } [Not NEEDED]



= Type Checking [self Study]

Intermediate code generation (SDD)

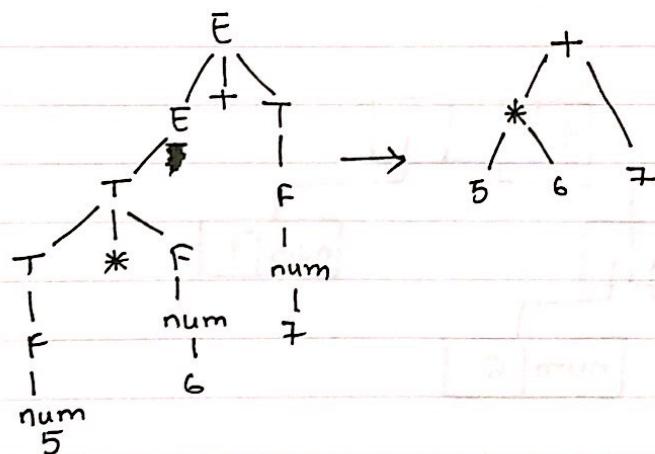
Representation of IC

- Postfix
- Syntax tree
- 3 address code

{ Triple } { direct triple.
 { Quadruple. indirect triple.

Syntax tree is a condensed form of parse tree, operators and keyword @ interior and do not appear as leaf.

$5 * 6 + 7$

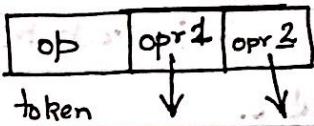


Construction of syntax tree

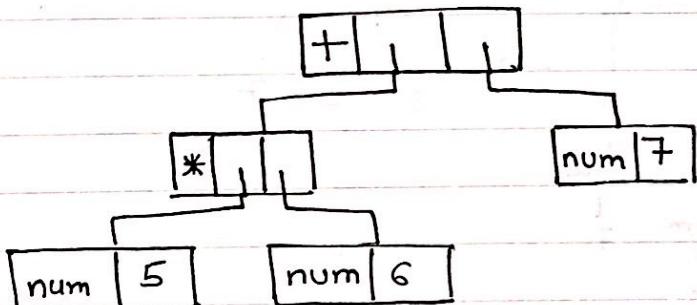
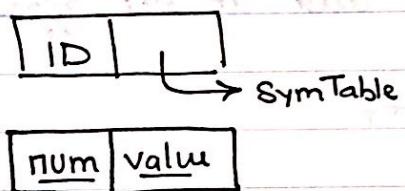
1. Create a leaf for all ids and consts.
2. Create subtrees for subexpression
3. Op are @ root of subtrees with operands and children
(children = id/ Num/ subtree.)

We make use of structures for nodes $\in \{ \text{id}, \text{Num}, \text{op} \}$

Node corresponding to operator



Node corresponding to ID



A function creating this node is added as an action
to the grammar #

1. $\text{CidLeaf}(\text{id}, \text{spt})$
2. $\text{CnumLeaf}(\text{num}, \text{value})$
3. $\text{CopNode}(\text{op}, \text{opr1}, \text{opr2})$

S attributed definition for making syntax tree

$E \rightarrow E + T$	$\{ E.np := \text{CopNode}(+, E_{np}.np, T.np) \}$	$ np = \text{new pointer}$
$E \rightarrow T$	$\{ E.np := T.np \}$	
$T \rightarrow T * F$	$\{ T.np := \text{CopNode}(*, T.np, F.np) \}$	
$T \rightarrow F$	$\{ T.np := F.np \}$	
$F \rightarrow \text{num}$	$\{ F.np := \text{CnumLeaf}(\text{num}, \text{value}) \}$	
$S \rightarrow \text{id} := E$	$\{ \text{id}.np = \text{Cidleaf}(\text{id}, \text{str}), S := \text{CopNode}(:=, \text{id}.np, E.np) \}$	

3 Address Code

Every statement is written comprising of maximum 3 addresses.

$$a + b * 9$$

$$t_1 = b * 9$$

$$t_2 = a + t_1$$

Pg 158 [list of operators]

relop (a,b) goto L_i (if relop(a,b) is true goto L_i or gotoNextstmt)

Triple it has 3 parts



for each expr we have a triple, and all these are in a triple table, this is the intermediate code.

$$x := a + b * c + c * d * e$$

Table	Tno	OP	opr ₁	opr ₂	
	(0)	*	b	c	• helps to find common sequences
	(1)	*	c	d	• This structure is inflexible
	(2)	*	(1)	e	
	(3)	(+)	a	(0)	esp with <u>loops</u>
	(4)	(+)	(3)	(2)	
	5	:=	x	(4)	

To add code movement capabilities we add another column.

Op	Op1	Op2	Res
*	b	c	t ₁
*	c	d	t ₂
*	t ₂	e	t ₃
+	t ₁	a	t ₄
+	t ₄	t ₃	t ₅
=	t ₅	-	-

Generally quadruple allows for better optimization, thus is done by making a list of temporaries.

Indirect and Direct

SDD for 3 add code.

SDD for generating 3 address code

$S \rightarrow id := E$

$E \rightarrow E_1 + E_2$

$E \rightarrow E_1 * E_2$

$E \rightarrow -E_1$

$E \rightarrow id.$

$E.place = E.name = E.value$

[all the same.]

functions : gen() ; gentemp(); lookup(); E.name
gen() : generates temporary check if id is in symbol table or not.
gentemp() : generates a temporary synth attr of E.
lookup() : E.name
not. for error handling

lookup(id.entry). { value → found entry.
Nil → Error }

$S \rightarrow id := E$	{ genC(id.name ':= E.name) }
$E \rightarrow E_1 + E_2$	{ $E = \text{genterm}()$ gen(E.name ':= E1.name + E2.name) }
$E \rightarrow E_1 * E_2$	{ $E = \text{gentemp}()$ gen(E.name ':= E1.name * E2.name) }
$E \Rightarrow - E_1$	{ $E.name = \text{genTemp}()$ gen(E.name ':= (-) E1.name) }
$E \Rightarrow id$	{ $E.name = \text{id.name}$ lookup(id.entry) }

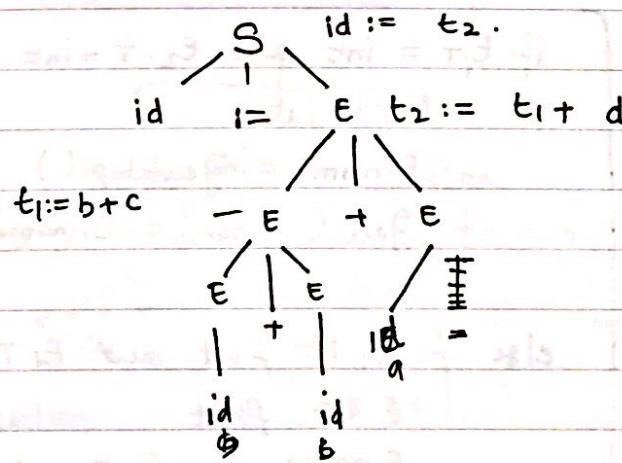
Example

$a := b + c + d$

$$t_1 = b + c$$

$$t_2 = t_1 + d$$

$$a = t_2$$



$x =$
 |
 int
 $y * 3 + y *$
 |
 float
 float.

$t_1 := \text{int} \rightarrow \text{float } y$
 $t_2 := t_1 * 3$
 $t_3 := / \text{int} \rightarrow \text{float} / *$
 $t_4 := y \text{int} \rightarrow$
 $t_4 := \text{int} \rightarrow \text{float } (t_3)$
 $t_5 := t_4 . \text{float} * t_2$
 $x := t_5$

Adding Type

$E.T \rightarrow \text{Type}$.

$E \rightarrow E_1 + E_2$
 $\left\{ \begin{array}{l} \text{if } E_1.T = \text{int} \text{ and } E_2.T = \text{int} : \\ \quad E.T = \text{int} \\ \quad E.name = \text{integerTemp}() \\ \quad \text{gen}(E.name := 'E_1.name' + E_2.name) \\ \\ \text{else if } E_1.T = \text{float} \text{ and } E_2.T = \text{float} \\ \quad E.T = \text{float} \\ \quad E.name = \text{floatGentemp}() \\ \quad \text{gen}(E.name := 'E_1.name' float + E_2.name) \\ \\ \text{else if } E_1.T = \text{float} \text{ and } E_2.T = \text{int} \\ \quad E.name = \text{float Gentemp}() \\ \quad \text{gen}(t.name := 'int to float' E.name) \end{array} \right.$

[5]

else if $E_1.T = \text{int}$ and $E_2.T = \text{float}$.

[else : t_error]

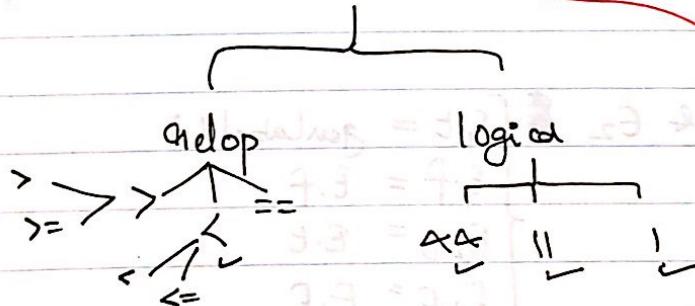
for tu := gen(id.name' := t.name) // only when id and type match.

Note

'Back Patching' = SDD for boolean (numerical) Exp =

20/4/18

SDD for Boolean expressions



* Partial Evaluation [a & b] if a is false, jump out

if E else E

eg if a & b goto L₁
else goto L₂

If has two exits, true / False.

Each ~~node~~ ^{sym} node has a true/false attribut. for T/F.

here we use genLabel() generates a new label.

& & & $a < b \wedge c < d$

if $a < b$ goto L
else goto E.false

E.code = 3 add code

$E \rightarrow E_1 \wedge E_2$

$E \rightarrow E_1 \text{relop } E_2$

L: if $c < d$ goto E.true.
else goto E.false.

1. $E \rightarrow E_1 \wedge E_2$

$$\begin{cases} E.t = \text{genLabel}() \\ E.f = E.f \\ E_1.t = E.t \\ E_2.f = E.F \end{cases}$$

$E.\text{code} = E_1.\text{code} \parallel \text{generate}(E_1.t, ':') \parallel E_2.\text{code}$

$E.\text{code} := \text{generate}(\text{if } E.\text{name} \text{ "relop" } E_2.\text{name} \text{ "goto" } E.t) \parallel$
 $\text{gen}('goto', E.f)$

$E \rightarrow E_1 \text{relop } E_2$

" Support to program for execution : runtimeEnv"

$$E \rightarrow E_1 || E_2 = \begin{cases} E_1 \cdot t - E \cdot t \\ E_1.F = \text{genLabel} \\ E_2.\text{true} = E \cdot t \\ E_2.F = E \cdot f \\ E.\text{code} = E_1.\text{code} || \text{gen}(E_1 \cdot t') || E_2.\text{code} \end{cases}$$

" Code optimization : defn and Examples [~14-15]

- Redundant LD and ST operations — ✓ ✓
- + Dead code elimination " — ✓ ✓
- Const propagation. — ✓ ✓