Package 'Wats'

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Title Wrap Around Time Series graphics
Description Wrap-around Time Series (WATS) Plots for Interrupted Time Series Designs with Seasonal Patterns
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URL https://github.com/wibeasley/Wats,https://r-forge.r-project.org/projects/wats/
Depends R (>= 3.0.0),stats
Imports boot,colorspace,ggplot2,grid,lubridate,plyr,RColorBrewer,scales,testit,zoo
Suggests BayesSingleSub,devtools,knitr,testthat
License GPL (>= 2)
LazyData TRUE
VignetteBuilder knitr
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AnnotateData

Finds midpoints and bands for the within and between cycles.

Description

Finds midpoints and bands for the within and between cycles. This the second of two functions that needs to be called to produce WATS Plots. AugmentZZZ is the first.

Usage

```
AnnotateData(dsLinear, dvName, centerFunction, spreadFunction,
  cycleTallyName = "CycleTally", stageIDName = "StageID",
  stageProgressName = "StageProgress",
 proportionThroughCycleName = "ProportionThroughCycle",
 proportionIDName = "ProportionID",
  terminalPointInCycleName = "TerminalPointInCycle")
```

Arguments

dsLinear The data. frame to containing the detailed data. dvName The name of the dependent/criterion variable. centerFunction A function to calculate the center of a subsample. spreadFunction A function to calculate the bands of a subsample. cycleTallyName The variable name indicating how many cycles have been completed. stageIDName The variable name indicating the stage. In a typical interrupted time series, these

values are 1 before the interruption and 2 after.

stageProgressName

The variable name indicating the stage in a decimal form. This is mostly for internal uses.

proportionThroughCycleName

The variable name indicating how far the point is through a cycle. For example, 0 degrees would be 0, 180 degrees would be 0.5, 359 degrees would be 0.9972, and 360 degrees would be 0.

proportionIDName

The variable name indicating the ordinal position through a cycle.

terminalPointInCycleName

The variable name indicating the last point within a given cycle.

Value

Returns a data. frame with additional variables «Say what they are».

```
require(Wats)
dsLinear <- CountyMonthBirthRate2005Version
dsLinear <- dsLinear[dsLinear$CountyName=="oklahoma", ]</pre>
dsLinear <- AugmentYearDataWithMonthResolution(dsLinear=dsLinear, dateName="Date")</pre>
hSpread <- function( scores ) { return( quantile(x=scores, probs=c(.25, .75)) ) }
```

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```
portfolio <- AnnotateData(
   dsLinear = dsLinear,
   dvName = "BirthRate",
   centerFunction = median,
   spreadFunction = hSpread
)
head(portfolio$dsStageCycle)
head(portfolio$dsLinear)
head(portfolio$dsPeriodic)</pre>
```

AugmentCycleData

Calculates variables necessary for WATS Plots

Description

Calculates variables necessary for WATS Plots. This the first of two functions that needs to be called to produce WATS Plots. AnnotateData is the second.

Usage

```
AugmentYearDataWithMonthResolution( dsLinear, dateName, stageIDName )
AugmentYearDataWithSecondResolution( dsLinear, dateName, stageIDName )
```

Arguments

dsLinear The data. frame to containing the detailed data.

dateName The variable name in dsLinear containing the date or datetime value.

stageIDName The variable name indicating the stage. In a typical interrupted time series, these

values are 1 before the interruption and 2 after.

Value

 $Returns\ a\ data.\ frame\ with\ additional\ variables:\ CycleTally,\ ProportionThroughCycle,\ ProportionID,\ and\ TerminalPointInCycle.$

```
require(Wats)
dsLinear <- CountyMonthBirthRate2005Version
dsLinear <- dsLinear[dsLinear$CountyName=="oklahoma", ]
dsLinear <- AugmentYearDataWithMonthResolution(dsLinear=dsLinear, dateName="Date")
head(dsLinear)</pre>
```

4 CartesianPeriodic

Description

Shows the interrupted time series in Cartesian coordinates and its a periodic/cyclic components.

Usage

```
CartesianPeriodic(dsLinear, dsPeriodic, xName, yName, stageIDName,
  periodicLowerName = "PositionLower", periodicUpperName = "PositionUpper",
  paletteDark = NULL, paletteLight = NULL, changePoints = NULL,
  changePointLabels = NULL, drawPeriodicBand = TRUE, jaggedPointSize = 2,
  jaggedLineSize = 0.5, bandAlphaDark = 0.4, bandAlphaLight = 0.15,
  changeLineAlpha = 0.5, changeLineSize = 3, title = NULL,
  xTitle = NULL, yTitle = NULL)
```

Arguments

dsLinear The data. frame to containing the simple linear data. There should be one

record per observation.

dsPeriodic The data. frame to containing the reoccurring/periodic bands. There should be

one record per observation per stage. If there are three stages, this data.frame

should have three times as many rows as dsLinear.

xName The variable name containing the date.

yName The variable name containing the dependent/criterion variable.

stageIDName The variable name indicating which stage the record belongs to. For example,

before the first interruption, the StageID is 1, and is 2 afterwards.

 ${\tt periodicLowerName}$

The variable name showing the lower bound of a stage's periodic estimate.

periodicUpperName

The variable name showing the upper bound of a stage's periodic estimate.

paletteDark A vector of colors used for the dark/heavy graphical elements. The vector should

have one color for each StageID value. If no vector is specified, a default will

be chosen, based on the number of stages.

paletteLight A vector of colors used for the light graphical elements. The vector should have

one color for each StageID value. If no vector is specified, a default will be

chosen, based on the number of stages.

changePoints A vector of values indicate the interruptions between stages. It typically works

best as a Date or a POSIXct class.

change Point Labels

The text plotted above each interruption.

drawPeriodicBand

A boolean value indicating if the bands should be plotted (whose values are take from the periodicLowerName and periodicUpperName.

jaggedPointSize

The size of the observed data points.

jaggedLineSize The size of the line connecting the observed data points.

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bandAlphaDark The amount of transparency of the band appropriate for a stage's x values.

bandAlphaLight The amount of transparency of the band comparison stages for a given x value. changeLineAlpha

The amount of transparency marking each interruption.

changeLineSize The width of a line marking an interruption.

title The string describing the plot.

xTitle The string describing the x-axis.

yTitle The string describing the y-axis.

Value

Returns a ggplot2 graphing object

Examples

```
require(Wats) #Load the package
changeMonth <- base::as.Date("1996-02-15")</pre>
dsLinear <- CountyMonthBirthRate2005Version</pre>
dsLinear <- dsLinear[dsLinear$CountyName=="oklahoma", ]</pre>
dsLinear <- AugmentYearDataWithMonthResolution(dsLinear=dsLinear, dateName="Date")</pre>
hSpread <- function( scores ) { return( quantile(x=scores, probs=c(.25, .75)) ) }
portfolio <- AnnotateData(</pre>
    dsLinear,
    dvName = "BirthRate";
    centerFunction = median,
    spreadFunction = hSpread
)
CartesianPeriodic(
  portfolio$dsLinear,
  portfolio$dsPeriodic,
  xName = "Date",
  yName = "BirthRate",
  stageIDName = "StageID",
  changePoints = changeMonth,
  changePointLabels = "Bombing Effect"
```

CartesianRolling

Linear Plot with Rolling Summaries

Description

Shows the interrupted time series in Cartesian coordinates without a periodic/cyclic components.

Usage

```
CartesianRolling(dsLinear, xName, yName, stageIDName,
  rollingLowerName = "RollingLower", rollingCenterName = "RollingCenter",
  rollingUpperName = "RollingUpper", paletteDark = NULL,
  paletteLight = NULL, colorSparse = grDevices::adjustcolor("tan1", 0.5),
```

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```
changePoints = NULL, changePointLabels = NULL, drawJaggedLine = TRUE,
drawRollingLine = TRUE, drawRollingBand = TRUE,
drawSparseLineAndPoints = TRUE, jaggedPointSize = 2,
jaggedLineSize = 0.5, rollingLineSize = 1, sparsePointSize = 4,
sparseLineSize = 0.5, bandAlpha = 0.4, changeLineAlpha = 0.5,
changeLineSize = 3, title = NULL, xTitle = NULL, yTitle = NULL)
```

Arguments

dsLinear The data. frame to containing the data.

xName The variable name containing the date.

yName The variable name containing the dependent/criterion variable.

stage IDName The variable name indicating which stage the record belongs to. For example,

before the first interruption, the StageID is 1, and is 2 afterwards.

rollingLowerName

The variable name showing the lower bound of the rolling estimate.

rollingCenterName

The variable name showing the rolling estimate.

rollingUpperName

The variable name showing the upper bound of the rolling estimate.

paletteDark A vector of colors used for the dark/heavy graphical elements. The vector should

have one color for each StageID value. If no vector is specified, a default will

be chosen, based on the number of stages.

paletteLight A vector of colors used for the light graphical elements. The vector should have

one color for each StageID value. If no vector is specified, a default will be

chosen, based on the number of stages.

colorSparse The color of the 'slowest' trend line, which plots only one value per cycle.

changePoints A vector of values indicate the interruptions between stages. It typically works

best as a Date or a POSIXct class.

changePointLabels

The text plotted above each interruption.

drawJaggedLine A boolean value indicating if a line should be plotted that connects the observed

data points.

drawRollingLine

A boolean value indicating if a line should be plotted that connects the rolling

estimates specified by rollingCenterName.

drawRollingBand

A boolean value indicating if a band should be plotted that envelopes the rolling estimates (whose values are take from the rollingLowerName and rollingUpperName.

 ${\tt drawSparseLineAndPoints}$

A boolean value indicating if the sparse line and points should be plotted.

jaggedPointSize

The size of the observed data points.

jaggedLineSize The size of the line connecting the observed data points.

rollingLineSize

The size of the line connecting the rolling estimates.

sparsePointSize

The size of the sparse estimates.

```
sparseLineSize The size of the line connecting the sparse estimates.

bandAlpha The amount of transparency of the rolling estimate band.

changeLineAlpha The amount of transparency marking each interruption.

changeLineSize The width of a line marking an interruption.

title The string describing the plot.

xTitle The string describing the x-axis.

yTitle The string describing the y-axis.
```

Value

Returns a ggplot2 graphing object

Examples

```
require(Wats) #Load the package
changeMonth <- base::as.Date("1996-02-15")</pre>
dsLinear <- CountyMonthBirthRate2005Version</pre>
dsLinear <- dsLinear[dsLinear$CountyName=="oklahoma", ]</pre>
dsLinear <- AugmentYearDataWithMonthResolution(dsLinear=dsLinear, dateName="Date")</pre>
hSpread <- function( scores ) { return( quantile(x=scores, probs=c(.25, .75)) ) }
portfolio <- AnnotateData(</pre>
    dsLinear,
    dvName = "BirthRate",
    centerFunction = median,
    spreadFunction = hSpread
)
CartesianRolling(
    portfolio$dsLinear,
    xName = "Date",
    yName = "BirthRate",
    stageIDName = "StageID";
    changePoints = changeMonth,
    changePointLabels = "Bombing Effect"
)
```

 ${\it County Month Birth Rate } {\it Monthly Growth Fertility Rates (GFR) for 12 urban Oklahoma counties}$

Description

Monthly Growth Fertility Rates (GFR) for 12 urban counties in Oklahoma between January 1990 and December 1999. The GFR is defined as the number of births divided by the number of females (ages 15-44), multiplied by 1,000.

There are two datasets in this package that are almost identical. The 2014 version is better suited for substantive researchers in the areas of fertility and traumatic cultural events. The 2005 version recreates the 2005 article and, therefore is better suited for the graphical aims of the 2014 manuscript.

The difference is that the 2005 version uses constant estimate for a county population –specifically the US Census 1990 estimates. The 2014 version uses different estimates for each month –specifically the US intercensal annual estimates, with linear interpolation for February through December of each year.

Format

A data frame with 1,440 observations on the following 11 variables.

Fips The county's 5-digit value according to the Federal Information Processing Standards. integer

CountyName The lower case name of the county. character

Year The year of the record, ranging from 1990 to 1999. integer

Month The month of the record, ranging from 1 to 12. integer

FecundPopulation The number of females in the county, ages of 15 to 44. numeric

BirthCount The number of births in a county for the given month. integer

Date The year and month of the record, with a date of the 15th. Centering the date within the month makes the value a little more representative and the graphs a little easier. date

DaysInMonth The number of days in the specific month. integer

DaysInYear The number of days in the specific years integer

StageID The 'Stage' of the month. The pre-bombing records are '1' (accounting for 9 months of gestation); the post-bombing months are '2'. integer

BirthRate The Growth Fertility Rate (GFR). numeric

Details

«Joe, can you please finish/edit this sentence?» The monthly birth counts were copied from county records by Ronnie Coleman during the summer of 2001 from state vital statistics records. It was collected for Rodgers, St. John, & Coleman (2005).

The US Census' intercensal estimates are used for the January values of FecundPopluation. Values for February-December are interpolated using approx.

The datasets were manipulated to produce this data frame by the two R files IsolateCensusPops-ForGfr.R and CalculateGfr.R.

Author(s)

Will Beasley

References

Rodgers, J. L., St. John, C. A. & Coleman R. (2005). Did Fertility Go Up after the Oklahoma City Bombing? An Analysis of Births in Metropolitan Counties in Oklahoma, 1990-1999. *Demography*, 42, 675-692.

Intercensal estimates for 199x.

Intercensal estimates for 200x.

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Examples

```
require(ggplot2)
##2005 Version (see description above)
ds2005 <- CountyMonthBirthRate2014Version
ggplot(ds2005, aes(x=Date, y=BirthRate, color=factor(Fips))) +
geom_line() +
labs(title="County Fertility - Longitudinal")
ggplot(ds2005, aes(x=BirthRate, color=factor(Fips))) +
geom_density() +
labs(title="Distributions of County Fertility")
##2014 Version (see description above)
ds2014 <- CountyMonthBirthRate2014Version
ggplot(ds2014, aes(x=Date, y=BirthRate, color=factor(Fips))) +
geom_line() +
labs(title="County Fertility - Longitudinal")
ggplot(ds2014, aes(x=BirthRate, color=factor(Fips))) +
geom_density() +
labs(title="Distributions of County Fertility")
```

PolarizeCartesian

Manipulate Cartesian data to use in the WATS polar plot

Description

Three operations are performed. First, within each stage, the first row is repeated at the end, to close the loop. Second, multiple points are interpolated (still in a Cartesian coordinates) so that the polar graph doesn't have sharp edges. These sharp edges would be artifacts of the conversion, and not reflect the observed data. Third, the Cartesian points are coverted to polar coordinates.

Usage

```
PolarizeCartesian(dsLinear, dsStageCycle, yName, stageIDName,
  cycleTallyName = "CycleTally",
  proportionThroughCycleName = "ProportionThroughCycle",
  periodicLowerName = "PositionLower",
  periodicCenterName = "PositionCenter",
  periodicUpperName = "PositionUpper", plottedPointCountPerCycle = 120,
  graphFloor = min(base::pretty(x = dsLinear[, yName])))
```

Arguments

dsLinear The data. frame to containing the simple linear data. There should be one

record per observation.

dsStageCycle The data. frame to containing the reoccurring/periodic bands. There should be

one record per observation per stage. If there are three stages, this data.frame

should have three times as many rows as dsLinear.

yName The variable name containing the dependent/criterion variable.

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stageIDName The variable name indicating which stage the record belongs to. For example, before the first interruption, the StageID is 1, and is 2 afterwards.

cycleTallyName The variable name indicating how many *complete* cycles have occurred at that observation.

proportionThroughCycleName

The variable name showing how far through a cycle the observation (or summarized observations) occurred.

periodicLowerName

The variable name showing the lower bound of a stage's periodic estimate.

periodicCenterName

The variable name showing the center estimate of a stage's periodic estimate.

periodicUpperName

The variable name showing the upper bound of a stage's periodic estimate.

plottedPointCountPerCycle

The number of points that are plotted per cycle. If the polar graph has 'sharp corners', then increase this value.

graphFloor

The value of the criterion/dependent variable at the center of the polar plot.

Value

Returns a data. frame.

```
require(Wats)
dsLinear <- CountyMonthBirthRate2005Version
dsLinear <- dsLinear[dsLinear$CountyName=="oklahoma", ]</pre>
dsLinear <- AugmentYearDataWithMonthResolution(dsLinear=dsLinear, dateName="Date")</pre>
hSpread <- function( scores ) { return( quantile(x=scores, probs=c(.25, .75)) ) }
portfolio <- AnnotateData(</pre>
  dsLinear = dsLinear,
  dvName = "BirthRate"
  centerFunction = median,
  spreadFunction = hSpread
rm(dsLinear)
polarized <- PolarizeCartesian(</pre>
  dsLinear = portfolio$dsLinear,
  dsStageCycle = portfolio$dsStageCycle,
  yName = "BirthRate",
  stageIDName = "StageID"
)
require(ggplot2)
ggplot(polarized$dsStageCyclePolar, aes(color=factor(StageID))) +
  geom_path(aes(x=PolarLowerX, y=PolarLowerY), linetype=2) +
  geom_path(aes(x=PolarCenterX, y=PolarCenterY), size=2) +
  geom_path(aes(x=PolarUpperX, y=PolarUpperY), linetype=2) +
  geom_path(aes(x=ObservedX, y=ObservedY), data=polarized$dsObservedPolar) +
  coord_fixed(ratio=1) +
  guides(color=FALSE)
```

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PolarPeriodic	Polar Plot with Periodic Elements

Description

Shows the interrupted time series in Cartesian coordinates and its a periodic/cyclic components.

Usage

```
PolarPeriodic(dsLinear, dsStageCyclePolar, xName, yName, stageIDName, periodicLowerName = "PositionLower", periodicUpperName = "PositionUpper", paletteDark = NULL, paletteLight = NULL, changePoints = NULL, changePointLabels = NULL, drawObservedLine = TRUE, drawPeriodicBand = TRUE, jaggedPointSize = 2, jaggedLineSize = 0.5, bandAlphaDark = 0.4, bandAlphaLight = 0.15, colorLabels = "gray50", colorGridlines = "gray80", changeLineAlpha = 0.5, changeLineSize = 3, tickLocations = base::pretty(x = dsLinear[, yName]), graphFloor = min(tickLocations), graphCeiling = max(tickLocations), cardinalLabels = NULL, originLabel = paste0("The origin represents ", graphFloor, ";\nthe perimeter represents ", graphCeiling, "."), plotMargins = c(3.5, 2, 0.5, 2))
```

Arguments

dsLinear The data.frame to containing the simple linear data. There should be one

record per observation.

dsStageCyclePolar

The data.frame to containing the bands for a single period. There should be one record per theta per stage. If there are three stages, this data.frame should have three times as many rows as dsLinear.

xName The variable name containing the date.

yName The variable name containing the dependent/criterion variable.

stageIDName The variable name indicating which stage the record belongs to. For example,

before the first interruption, the StageID is 1, and is 2 afterwards. #

periodicLowerName

The variable name showing the lower bound of a stage's periodic estimate. #

periodicUpperName

The variable name showing the upper bound of a stage's periodic estimate.

paletteDark A vector of colors used for the dark/heavy graphical elements. The vector should

have one color for each StageID value. If no vector is specified, a default will

be chosen, based on the number of stages.

paletteLight A vector of colors used for the light graphical elements. The vector should have

one color for each StageID value. If no vector is specified, a default will be

chosen, based on the number of stages.

changePoints A vector of values indicate the interruptions between stages. It typically works

best as a Date or a POSIXct class.

changePointLabels

The text plotted above each interruption.

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drawObservedLine

A boolean value indicating if the longitudinal observed line should be plotted (whose values are take from dsLinear.

drawPeriodicBand

A boolean value indicating if the bands should be plotted (whose values are take from the periodicLowerName and periodicUpperName fields.

jaggedPointSize

The size of the observed data points.

jaggedLineSize The size of the line connecting the observed data points.

bandAlphaDark The amount of transparency of the band appropriate for a stage's x values.

bandAlphaLight The amount of transparency of the band comparison stages for a given x value.

changeLineAlpha

The amount of transparency marking each interruption.

colorLabels The color for cardinalLabels and originLabel.

colorGridlines The color for the gridlines.

changeLineSize The width of a line marking an interruption.

tickLocations The desired locations for ticks showing the value of the criterion/dependent vari-

able.

graphFloor The value of the criterion/dependent variable at the center of the polar plot.

 ${\tt graphCeiling} \qquad {\tt The \ value \ of \ the \ criterion/dependent \ variable \ at \ the \ outside \ of \ the \ polar \ plot.}$

cardinalLabels The four labels placed where 'North', 'East', 'South', and 'West' typically are.

originLabel Explains what the criterion variable's value is at the origin. Use NULL if no

explanation is desired.

plotMargins A vector of four numeric values, specifying the number of lines in the bottom,

left, top and right margins.

Value

Returns a grid graphical object (ie, a grob.)

```
require(grid)
require(Wats)
dsLinear <- CountyMonthBirthRate2005Version
dsLinear <- dsLinear[dsLinear$CountyName=="oklahoma", ]
dsLinear <- AugmentYearDataWithMonthResolution(dsLinear=dsLinear, dateName="Date")
hSpread <- function( scores ) { return( quantile(x=scores, probs=c(.25, .75)) ) }
portfolio <- AnnotateData(
    dsLinear = dsLinear,
    dvName = "BirthRate",
    centerFunction = median,
    spreadFunction = hSpread
)
rm(dsLinear)

polarized <- PolarizeCartesian(
    portfolio$dsLinear,
    portfolio$dsStageCycle,</pre>
```

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```
yName = "BirthRate",
  stageIDName = "StageID"
grid.newpage()
PolarPeriodic(
  dsLinear = polarized$dsObservedPolar,
  dsStageCyclePolar = polarized$dsStageCyclePolar,
  yName = "Radius".
  stageIDName = "StageID",
  cardinalLabels = c("Jan1", "Apr1", "July1", "Oct1")
grid.newpage()
PolarPeriodic(
  dsLinear = polarized$dsObservedPolar,
  dsStageCyclePolar = polarized$dsStageCyclePolar,
  yName = "Radius",
  stageIDName = "StageID",
  drawPeriodicBand = FALSE
grid.newpage()
PolarPeriodic(
  dsLinear = polarized$dsObservedPolar,
  dsStageCyclePolar = polarized$dsStageCyclePolar,
  yName = "Radius",
  stageIDName = "StageID";
  drawObservedLine = FALSE,
  cardinalLabels = c("Jan1", "Apr1", "July1", "Oct1")
```

Wats

Wrap Around Time Series graphics

Description

Wrap-around Time Series (WATS) Plots for Interrupted Time Series Designs with Seasonal Patterns

Author(s)

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Joseph Lee Rodgers - Vanderbilt University, Nashville'

Matthew Schuelke, League of Justice.

References

Rodger, J.L., Beasley, W.H., and Schuelke, M. (in submission). Wrap-around Time Series Plots (WATS Plots) for Interrupted Time Series Designs: Applications to Fertility Rates and the Oklahoma City Bombing.

Rodgers, J. L., St. John, C. A. & Coleman R. (2005). Did Fertility Go Up after the Oklahoma City Bombing? An Analysis of Births in Metropolitan Counties in Oklahoma, 1990-1999. *Demography*, 42, 675-692.

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