

# Final Answer

$$A) = 1067 \text{ kg}$$

$$B) = 10.64 \%$$

$$C) = 91.85^\circ\text{C}$$

# Problem Statement

A) Calculate water at  $100^\circ\text{C}$

B) Calculate water loss

C) Calculate equilibrium temperature.

D) Calculate ice needed to chill drink.

E) Calculate volume of tea to the end.

## Represent the Problem and Organize Information

3 Liters of water starting at  $15^\circ\text{C}$

assume water coefficients.

boiling point:  $100^\circ\text{C}$

freezing point:  $0^\circ\text{C}$

$$F \text{ to } C \text{ conversion: } \frac{9}{5}^\circ\text{C} + 32; \frac{5}{9}(F - 32)$$

temp change conversion

1° temp change in C = 1 K in change

Change in  $1.8^\circ\text{F}$  is a change in C

Specific heat of water.

$$= 1.0 \text{ cal/g}^\circ\text{C}$$

$$\text{or } 4186 \dots$$

Formula:

$$Q = mc\Delta T$$

$$Q = mL$$

$$\Delta L = \alpha L_0 \Delta T$$

$$Q = \alpha E \Delta T$$

$$\Delta V = \beta V_0 \Delta T$$

## Calculations

$$A) Q = mc\Delta T$$

$$Q = (3 \text{ L}) (4186) (100 - 15) = 1067130 \text{ J/kg}$$

$$B) 1067 \text{ J/kg} + 720 \text{ kg} = 1787 \text{ kg} @ 100^\circ\text{C}$$

Latent heat Vaporization

$$L_f = L_v = 540 \text{ cal/g} \text{ or } 334 \text{ kJ/kg}$$

$$720 \text{ kg} / 4.186 = 172001 \text{ calories constant}$$

$$\frac{Q}{L_v} = \frac{172001}{540} = 318.5$$

% of tea boiled away

$$\frac{m_x}{m} \times 100 = \frac{318.5 \text{ g}}{3000 \text{ g}} = 0.106 \times 100$$

$$= 10.6 \%$$

C) equilibrium Calculation.

mass of boiling

water = 3 Liters - 10.6 water loss

$$= 3000 \text{ g} - (3000 \cdot 10.6 \%) = 2682 \text{ g} = 2.682 \text{ L}$$

$$2.682 \text{ L @ } 100^\circ\text{C} + 0.3 \text{ kg water at } 15^\circ\text{C}$$

equilibrium = constant 0.3 kg to boil = 0.3 L

$$Q = (2.682 \cdot 4186 \cdot 100) = (0.3 \cdot 4186 \cdot T) = T(100 + 273)$$

$$= (2.682 - (373 - T)) = (0.3 - (T - 273))$$

$$= 1000.346 - 2.682T = 0.3T - 81.6$$

$$= 2.982T = 1081.986$$

$$= T = 364.85 \text{ Kelvin}$$

$$-273 \text{ K} = 91.85^\circ\text{C}$$

$$D) Q_{\text{ice from } -11^\circ\text{C} \rightarrow 0^\circ\text{C}} = (0.5)(M) \text{ mass}_{\text{ice}}$$

$$Q_{\text{melt}} = M_{\text{ice}} (79.6)$$

$$Q_{\text{ice at } 0^\circ\text{C} \rightarrow 4^\circ\text{C}} = M_{\text{ice}} (1)(4)$$

$$Q_{\text{ice at } 91.85^\circ\text{C} \rightarrow 4^\circ\text{C}} = M_{\text{ice}} (1)(4)$$

$$\begin{aligned} \text{Mass of water} &= 3000 \text{ g} \cdot 10.64\% \\ &= 2681 \text{ g @ } 100^\circ\text{C} \\ &300 \text{ g @ } 100^\circ\text{C} \end{aligned}$$

$$91.85 + m_{\text{ice}} = 4^\circ\text{C}$$

$$m_{\text{ice}} @ -11^\circ\text{C}$$

$$91.85^\circ\text{C} + m_{\text{ice}} (-11) = 4^\circ\text{C}$$

$$Q_{\text{warm ice}} \rightarrow Q_{\text{melt ice}}$$

$$\rightarrow Q_{\text{equilibrium}} \rightarrow Q_{\text{final}}$$

$$\downarrow \quad \downarrow$$

$$91.85^\circ\text{C} \quad 4^\circ\text{C}$$

$$Q_{\text{wi}} = \text{mass}_{\text{ice}} \cdot (1.5) (0 - (-11))$$

$$(m_{\text{ice}} \cdot 0.5 \cdot 11) = Q_{\text{wi}}$$

$$Q_{\text{ice at } 0^\circ\text{C}} = \text{ice}_{\text{mass}} \cdot (1) (79.6)$$

$$Q_{\text{final}} = \text{ice}_{\text{mass}} \cdot (1) (4)$$

$$Q = \text{ice}_{\text{mass}} (89.1)$$

$$955837610.1 / 89.1$$

$$= 11064395.74$$

## Evaluate

✓ My units are consistent and cancel through the calculations.

✓ My equations are appropriate for the physical system being evaluated and are written in variable form.

✓ My answer is reasonable given the magnitude of the values in the problem.

✓ My final solution answers the problem statement.

✓ My final solution is in the appropriate form (vector or scalar) and has appropriate units

$$Q = mc\Delta T$$



# Final Answer

$$D = 2.934 \text{ g}$$

$$E = 5.920 \text{ L}$$

# Problem Statement

- D) Calculate the mass  
E) Calculate final volume

# Represent the Problem and Organize Information

3 liters of water.  $61.5^\circ\text{C}$

$$Q = 1067 \text{ kJ}$$

% of water lost 10.64%

equilibrium temperature:  $91.85^\circ\text{C}$

# Calculations

D)  $Q = m_{\text{ice}} \cdot \overset{\text{added}}{(89.1)}$

$$(11^\circ\text{C} \cdot 5) \cdot 55$$

$$5.5^\circ + 4^\circ + 79.6^\circ = 89.1$$

$$m_{\text{ice}} = \frac{261793}{89.1} = 2938 \text{ grams}$$

Calculate Q

$$Q = m \Delta T$$

$$Q = 1067 \text{ kJ} + 720 \text{ kJ} = 1787$$

$$\overset{\text{L}}{3000 \text{ g}} \cdot \overset{10.64\%}{\downarrow} 10.64$$

$$= 3000 - 319.2$$

$$= 2680.8$$

+ 300g of water added

$$= 2980.8 \text{ mass}$$

$$-(2980 \cdot (1 \text{ g/cm}^3) \cdot (4^\circ - 91.85^\circ))$$

$$= +261793$$

E)  $2980 + 2938 = 5918 \text{ g}$

$$= 5918 \text{ g} \cdot \frac{1}{1000} \cdot \frac{1}{1000} = 0.005918 \text{ m}^3$$

$$\text{or } 5.920 \text{ L}$$

# Evaluate

- ☐ My units are consistent and cancel through the calculations.
- ☐ My equations are appropriate for the physical system being evaluated and are written in variable form.
- ☐ My answer is reasonable given the magnitude of the values in the problem.
- ☐ My final solution answers the problem statement.
- ☐ My final solution is in the appropriate form (vector or scalar) and has appropriate units