

**ECE 255 – Introduction to Digital Logic Design**  
**Homework Assignment 4**  
**Due October 13**

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1. Minimize the following functions using the Quine-McCluskey method.

(a)  $f(a, b, c, d) = \sum(m_0, m_2, m_4, m_5, m_7, m_9, m_{11}, m_{12})$

Table 1

Group I	$m_0, m_2$
Group II	$m_4, m_6$
Group III	$m_8, m_{10}$
Group IV	$m_{12}, m_{14}$

Table 2

$m_0, m_2$	$00x0$
$m_4, m_6$	$0x00$
$m_8, m_{10}$	$x00x$
$m_{12}, m_{14}$	$1x00$

msop =

$$a'b'd' + a'b'd + b'd' + a'b'd$$

$m_0, m_2$	$00x0$
$m_4, m_6$	$0x00$
$m_8, m_{10}$	$x00x$
$m_{12}, m_{14}$	$1x00$

Prime Implicant Chart

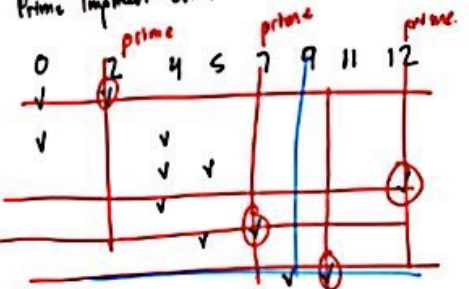


Table 1

Group I	$m_0, m_1$
Group II	$m_2, m_3$
Group III	$m_4, m_5$
Group IV	$m_6, m_7$
Group V	$m_8, m_9$
Group VI	$m_{10}, m_{11}$
Group VII	$m_{12}, m_{13}$
Group VIII	$m_{14}, m_{15}$

(b)  $f(a, b, c, d, e) = \sum(m_0, m_1, m_2, m_7, m_9, m_{11}, m_{12}, m_{23}, m_{27}, m_{28})$

Table 2

$m_0, m_1$	$0000x$
$m_2, m_3$	$000x1$
$m_4, m_5$	$0x001$
$m_6, m_7$	$0101x$
$m_8, m_9$	$x1100$
$m_{10}, m_{11}$	$1011x$
$m_{12}, m_{13}$	$11011$
$m_{14}, m_{15}$	$11101$

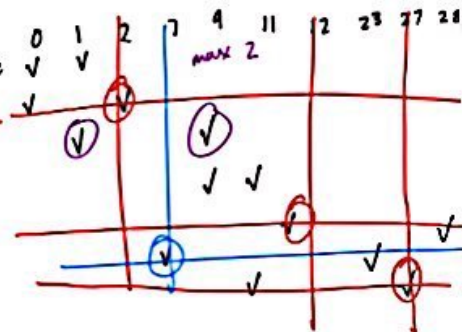
prime implicants

$$000x0, x1100, x1011$$

$$x0111, 0x001$$

$$msop = \bar{a}\bar{b}\bar{c}\bar{d}e + \bar{a}\bar{b}\bar{c}d\bar{e} + b\bar{c}d\bar{e} + \bar{b}cde + b\bar{c}de$$

$m_0, m_1$	$0000x$
$m_2, m_3$	$000x1$
$m_4, m_5$	$0x001$
$m_6, m_7$	$0101x$
$m_8, m_9$	$x1100$
$m_{10}, m_{11}$	$1011x$
$m_{12}, m_{13}$	$11011$
$m_{14}, m_{15}$	$11101$



2. Consider the following multi-output functions and minimize them using the Quine-McCluskey method.

$$f_a(a, b, c, d) = \sum(m_3, m_7, m_9, m_{14}) + \sum d(m_1, m_4, m_6, m_{11})$$

$$f_b(a, b, c, d) = \sum(m_6, m_7, m_{12}) + \sum d(m_3, m_{14})$$

Table 1

group 1	$m_1$ 0001
group 2	$m_3$ 0011
group 3	$m_7$ 0111
group 3	$m_{14}$ 1110

Table 2

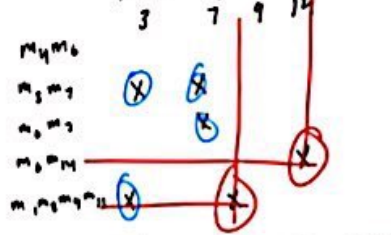
$m_3, m_7$	00x1
$m_3, m_7$	x001
$m_3, m_7$	01x0
$m_3, m_7$	0x11
$m_7, m_{14}$	x011
$m_7, m_{14}$	10x1
$m_7, m_{14}$	0x11
$m_7, m_{14}$	x110

$$b, b_c = m_3, m_7, m_{14}$$

$$= x0x1$$

$\Sigma d$  - don't cares.

Prime implicant chart.



$$\text{prime implicants} = x0x1, x011, 0x11$$

$$msop = \bar{b}d + b\bar{c}d + \bar{a}cd$$

Table 1

group 2	$m_6$ 0110
	$m_3$ 0011
	$m_{12}$ 1100
group 3	$m_7$ 0111
	$m_{14}$ 1110

Table II

$m_6, m_7$	011x	✓
$m_6, m_{12}$	x110	✓
$m_7, m_{14}$	0x11	✓
$m_{12}, m_{14}$	11x0	✓

group

Table III

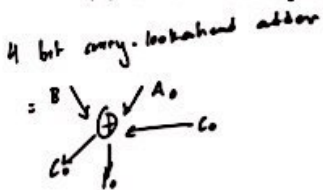
$m_6, m_7$	011x
$m_6, m_{12}$	x110
$m_7, m_{14}$	0x11
$m_{12}, m_{14}$	11x0

$$\text{extracted} = 11x0, 011x$$

$$\therefore msop = ab\bar{c} + a\bar{b}c$$

3. Design a 3-bit adder using a single carry-lookahead circuit (one 3-bit carry-lookahead group) and provide a schematic

(a) Show all key logical expressions (HINT: see example for 4-bit carry-lookahead).



Logical Expression

Carry output:

$$C_1 = b_0 + P_0 C_0$$

$$C_2 = b_1 + P_1 C_1 = b_1 + P_1 C_0 + P_1 b_0$$

$$C_3 = C_2 + P_2 C_2 = b_2 + P_2 b_1 + P_2 P_1 b_0 + P_2 P_1 C_0$$

need a carry generator and carry propagate

$$P_i = A_i \oplus B_i$$

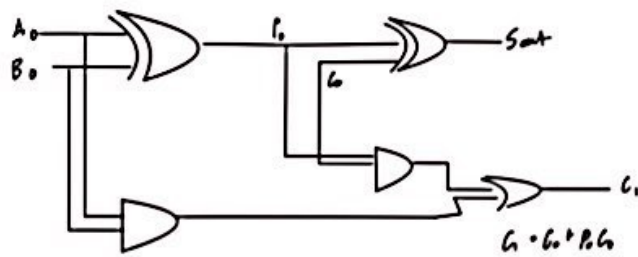
$$G_i = A_i B_i$$

$$\text{output } P_i \oplus C_i$$

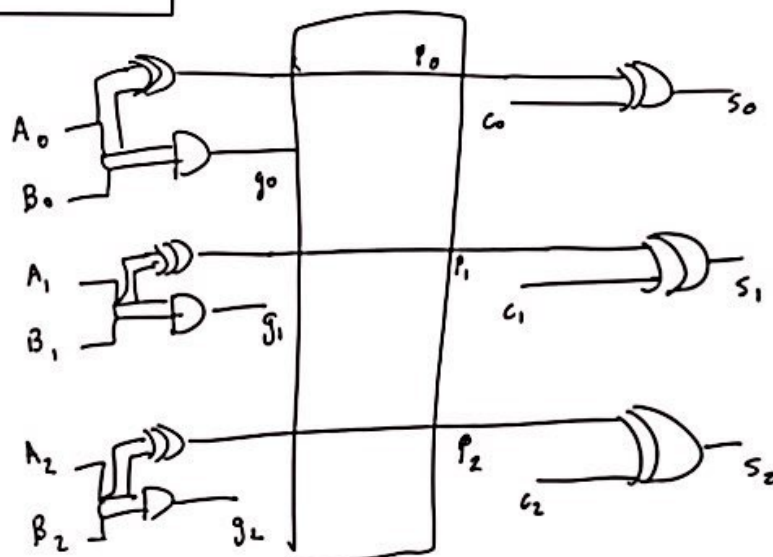
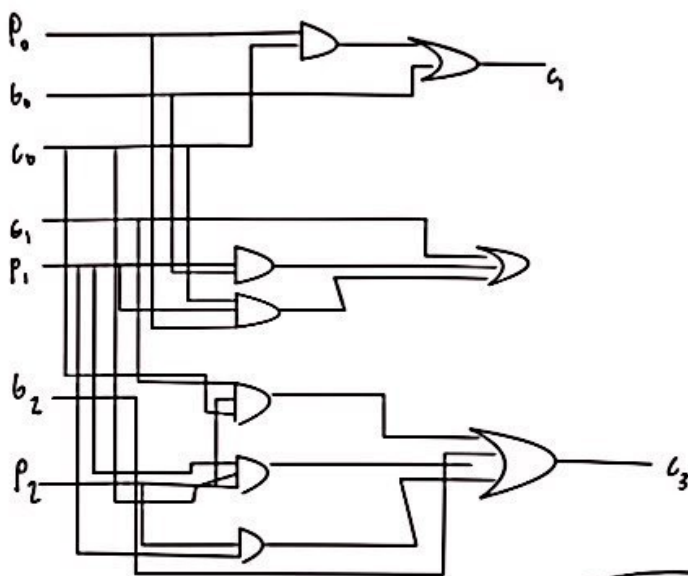
$$\text{Carry } C_i = b_i + P_i C_{i-1}$$

- (b) Draw a schematic of your 3-bit adder, showing the carry-lookahead circuit. You can sketch by hand or use a tool such as Logisim to produce your schematic.

Adder propagation



full logic gates



roughly with  
adder.