1. Time Complexity

Algorithm	bubble sort	selection sort	insertion sort	merge sort	quick sort	random	counting sort	radix sort	stl:sort
						quick sort			
Average	O(N ²)	O(N ²)	O(N ²)	O(N log N)	O(N log N)	O(N log N)	O(N)	O(N)	O(N log N)
Sorted Ascending	O(N)	O(N ²)	O(N)	O(N log N)	O(N ²)	O(N log N)	O(N)	O(N)	O(N log N)
Sorted Descending	O(N ²)	O(N ²)	O(N ²)	O(N log N)	O(N ²)	O(N log N)	O(N)	O(N)	O(N log N)
Worst Ascending	O(N)	O(N ²)	O(N)	O(N log N)	O(N ²)	O(N log N)	O(N)	O(N)	O(N log N)
Worst Descending	O(N ²)	O(N ²)	O(N ²)	O(N log N)	O(N ²)	O(N log N)	O(N)	O(N)	O(N log N)
Stability ¹	yes	no	yes	yes	no	no	yes	yes	no
In place ²	yes	yes	yes	no	yes	yes	no	no	no
Recursive	no	no	no	yes	yes	yes	no	no	yes
Comparisons based	yes	yes	yes						
Divide & Conquer				yes	yes	yes			yes

Data Structure	Vector	Singly Linked List	Stack	Queue	Double Linked List	Deque
access i th element	O(1)	O(N)	O(N)	O(N)	O(N)	Not allowed
search(num)	O(N)	O(N)	Not allowed	Not allowed	O(N)	Not allowed
peek-front()/top()	O(1)	O(1)	O(1)	O(1)	O(1)	O(1)
peek-back()	O(1)	O(1)	Not allowed	O(1)	O(1)	O(1)
insert(0, num)	O(N)	O(1)	O(1)	Not allowed	O(1)	O(1)
insert(n, num)	O(1)	O(1)	Not allowed	O(1)	O(1)	O(1)
insert(i, num)	O(i)/O(N)	O(N)	Not allowed	Not allowed	O(N)	Not allowed
remove head	O(N)	O(1)	O(1)	O(1)	O(1)	O(1)
remove tail	O(1)	O(N)	Not allowed	Not allowed	O(1)	O(1)
remove(i)	O(i)/O(N)	O(N)	Not allowed	Not allowed	O(N)	Not allowed

¹ Stable: the relative order of elements with the same key value is preserved after sorting.

² In-place: it requires only a constant amount (e.g O(1)) of extra space during the sorting process. Not in-place sorting requires additional temporary array of size N.

2. Sorting Algorithm

A. Bubble sort

- 1. Pair-wise comparison of adjacent elements(a, b),
- 2. Swap the pair if (a>b),
- 3. Repeat step 1 & 2 until the end of the array,
- 4. Then reduce N by 1 and repeat step 1 until N = 1.

B. Insertion sort

- 1. Start with one element,
- 2. Pick the next element and insert it into its proper sorted order,
- 3. Repeat step 2 for all the elements.

```
void insertion_sort() {
    for(i=1; i<n; i++) {
        e = A[i]; j=i;
        while(j>0) {
            if(A[j-1]>e) A[j]=A[j-1];
            else break;
        }
    }
```

C. Selection sort

- 1. Find the position of the smallest element X in the range of [lowerbound L ~ N-1],
- 2. Swap X with the Lth element,
- 3. Increase the lowerbound L by 1 and repeat step 1 until L = N-2.

```
void selection_sort() {
    int i, j, min_idx;

    for(i=0; i<n-1; i++) {
        min_idx = i;
        for(j=i+1; j<n; j++) {
            if(arr[j]<arr[min_idx]) min_idx=j;
        }
        swap(&arr[min_idx], &arr[i]);
    }
}</pre>
```

D. Merge sort

- 1. Merge each pair of individual element into sorted arrays of 2 elements,
- 2. Merge each pair of sorted arrays of 2 elements into sorted arrays of 4 elements...
- 3. Merge 2 sorted arrays of N/2 elements to obtain a fully sorted array of N.
- 4. Not memory efficient.

```
void merge() {
   int N = high-low+1;
   int b[n];
   int left=low, right=mid+1, bIdx=0;

while(left<=mid && right<=high) //merging
   b[bIdx++] = (a[left]<=a[right]) ? a[left++]:a[right++];
   while(left<=mid) b[bIdx++] = a[left++];
   while(right<=high) b[bIdx++] = a[right++];

   for(int k=0; k<N; k++) a[low+k]=b[k];
}

void merge_sort() {
   if(low<high) {
      int mid=(low+high)/2;
      merge_sort(a, low, mid);
      merge_sort(a, mid+1, high);
      merge_sort(a, low, mid, high);
   }
}</pre>
```

E. Counting sort

- 1. Used for small range of inputs with duplicates,
- 2. O(N) is to count the frequencies of the elements and O(N+k) is to print out the output in sorted order where k is the range of the input integers.
- 3. If k is relatively big, counting sort is not feasible due to memory limitation.

F. Radix sort

- 1. Used for a big range of inputs with w digits
- 2. For the least significant digit to the most significant digit, N items will be passed through and put according to the active digit into 10 queues ([0..9]).
- 3. Propotional to number of digits -> O(dN)
- 4. Can combine with counting sort for integers with large range but of few digits.

G. Quick sort

Divide step:

- 1. in arr[i..j], choose arr[i] as the pivot **p**
- 2. Partition the items of arr[i..j] into three parts: arr[i..m-1], arr[m], and arr[m+1...j].
- 3. arr[i..m-1] contains items smaller than **p**.
- 4. arr[m] is the pivot (index m is the position of **p**).
- 5. arr[m+1..j] contains items that a greater or equal to **p**.
- 6. Recurively sort the two parts.

Conquer step: do nothing:o

- 1. O(N) for partition(a, i, j) since there is only a single for-loop.
- 2. Time complexity depends on the number of times partition() is called.
- 3. Best case: quick sort splits the array into two equal halves -> gives the depth of recursion O(log N).
- 4. At each level of O(N) comparisons, the time comlexity is O(NlogN).

H. Random quick sort

- 1. Randomly select the pivot between arr[i..j].
- 2. This combination of randomness yiels partitions of lucky (half-pivot-half), somewhat lucky, somewhat unlucky and extremely unlucky (empty, pivot, the rest), which gives an average time complexity of O(N log N).

```
void quick_sort(int arr[], int low, int high) {
    if(low<high) {
        int pivotIdx = partition(a, low, high); //o(N)
            quick_sort(a, low, pivotIdx-1); //recursively sort left subarr
            quick_sort(a, pivotIdx+1, high); //then sort right subarr
    }
}

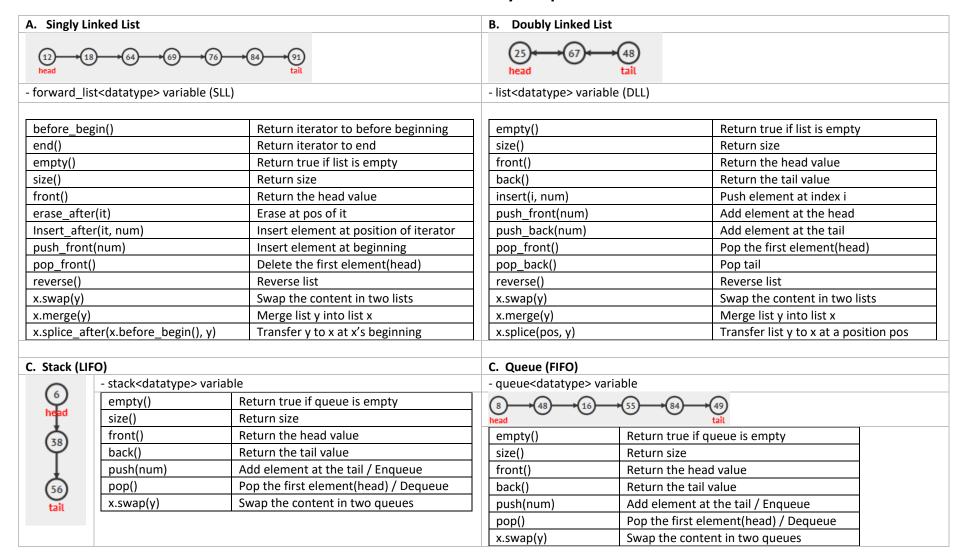
int random_pivoting(int arr[], int i, int j) {
    srand(time(NULL));
    int random = i + rand()%(j-i);

    swap(a[random], a[j]);

    return partition(arr, i, j);
}

void quick_sort(int arr[], int low, int high) {
    if(low<high) {
        int pivotIdx = random_pivoting(a, low, high); //o(N)
            quick_sort(a, low, pivotIdx-1); //recursively sort left subarr
            quick_sort(a, pivotIdx+1, high); //then sort right subarr
    }
}</pre>
```

3. List + Binary Heaps



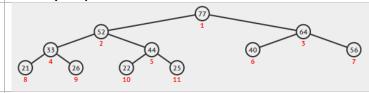
E. Deque



- deque<datatype> variable

begin() Return iterator to beginning end() Return iterator to end empty() Return true if deque is empty size() Return size at(index) Access the element at the index front() Return the head value back() Return the tail value insert(i, num) Push element at index i push front(num) Add element at the head push_back(num) Add element at the tail pop_front() Pop the first element(head) pop_back() Pop tail Erase the content in deque clear()

F. Binary Heaps



- priority_queue<datatype, vector<datatype>, greater<datatype>> min_heap;
- priority_queue<datatype, vector<datatype>, less<datatype>> max_heap;

empty()	Return true if container is empty
size()	Return size
top()	Return the head value / top / max / min
push(num)	Insert elements.
pop()	Pop the top element and calls heap sort
	functions in pop()
x.swap(y)	Swap the content in two queues
empty()	Return true if container is empty

Algorithm	Average	Worst
build heap / create	O(N)	O(N log N)
search	O(N)	O(N)
Insert – bubble sort upwards in O(log N) heighet	O(1)	O(log N)
top – max element	O(1)	O(1)
extractmax / pop – bubble sort downwards in O(log N) height	O(log N)	O(N)
heap_sort – remove all N from the heap	O(N log N)	O(N log N)

4. Hash Table

A. General Information

Properties	Definitions
1) Map some non-integer keys to integers keys. Map large integers to smaller	1) M = HT.length = the current hash table size.
integers.	2) base = (key%HT.length).
2) The key must be mapped to non-negative integer values. The range of keys must	3) step = the current probing step starting from 1.
be small. Otherwise the memory usage will be very large.	4) secondary = smaller_prime – key%smaller_prime, which is computed by another
3) The keys must be dense (i.e. not many gaps in the kay values).	hash function.
4) Fast to compute, uses as minimum slots as possible, scatter the keys into	
different base addresses as uniformly as possible together with minimum	
collisions.	

B. Collision Resolution

	Open Addressing		Closed addressing
- Always find an empty slot if it exists. Th	us the storing depends on other objects in t	the hash table.	- Storing of the object is completely
- More cache friendly.			dependent on the hash function.
- Give different probes sequences when 2	2 different keys collide		- Easy to obtain elements with same
- Require deleted markers and inefficient	if there are many deletions and insertions.		hash.
Linear Probing	Quadratic Probing	Double Hashing	Separate Chaining
Index = (base+step*1)%M	Index = (base+step*step)%M	Index = (base+step*secondary)%M	
- Forward one index at a time for the next empty slot search(v) function stops when its encountered an empty cell if there's no lazy deletion primary cluster -> covers the base address of a key which increase the running time beyond O(1) Long sequences of filled slots increase search and insert time.	- Secondary cluster -> clusters formed along the path of probing instead of around the base address not all cells are examined when looking for an insertion index may stuck in an infinite loop searching increase time taken if collision occurs may result in a waste of memory.	- reduce primary and secondary clustering search(v) and remove(v) are O(1+a)	- If two keys x and y both have the same hash value I, both will be appended to the front/back of a doubly linked list i Thus remove(v) requires search(v) whose time complexity depends on the load factor a ³ -> best O(1) insert(v) will be O(1) - Unable to fully utilize unused slots

 $^{^{3}}$ Load factor **a** = N/M where M is the number of copies of DLL

C. STL Maps

map		unodered_map						
- Associative containers that store el	ements formed by a combination of a key	- Associative containers that store	elements formed by the combination of a key					
value and a mapped value, following	a specific order.	value and a mapped value.						
- Slow access to individual elements	by its key.	- Allows for fast retrieval of individual elements based on their keys						
- Allows for direct iteration of the su	bsets based on their order.	- The elements are not sorted in any order.						
- Implemented as a binary search tre	e	- Less efficient for range iteration through a subset of their elements.						
	T .	- Uses separate chaining.						
at(index) / operator[index]	Access element	at(index) / operator[index]	Access element					
rbegin / rend	Reverse beginning / end	equal_range(X)	Return the pair of iterators to the lower					
crbegin / crend	Const reverse beginning / end		bound & upper bound+1 of that element					
lower_bound (X)	Return the iterator to X	equal_range(v.begin(), v.end())	Return the pair of iterators to the lower					
upper_bound (X)	Return the iterator to 1 element > X		bound & upper bound+1 of that range					
lower_bound (v.begin, v.end(), X)	Return the iterator to pos X via BST	key_eq	?					
upper_bound (v.begin, v.end(), X)	Return the iterator to pos X via BST	hash_function	?					
key_comp	Define the order of the keys	bucket	?					
value_comp	Define the order of the values	bucket_count	?					
equal_range(X)	Return the pair of iterators to the lower	bucket_size	?					
	bound & upper bound+1 of that element	rehash	?					
equal_range(v.begin(), v.end())	Return the pair of iterators to the lower	load_factor	?					
	bound & upper bound+1 of that range	insert(first, second)	O(1)					
find(X)	Return the iterator point to X							
erase(X) / erase(it)	Erase all occurrence of X / delete *it							
Insert(first, second)	O(log N)	7						
multimap		unordered_multimap						
- Allow multiple elements to have eq	uivalent keys	- Allow multiple elements to have e	equivalent keys.					
		- Elements with equivalent keys are	grouped together in the same bucket and					
		requires an iterator (equal_range) t	to iterate through.					

D. STL Sets

set		unordered_set				
- Container that stores unique eleme	ents following a specific order.	- Container that stores unique elem	nents in no particular order, and which allow for			
- The value is itself the key and each	value is unique.	fast retrieval of individual elements	s based on their value.			
- The elements cannot be modified o	once in the container but can be inserted or	- The value of an element is also its key.				
remove from the container.		- Keys are immutable and the elements cannot be modified once in the container				
- Slower than unordered_set to acce		but can be inserted and removed.				
- Allow for direct iteration on subsets	s based on their order	_	o allow for fast access to individual elements			
- Traversal using iterators		directly by their value but less effic	ient for range iteration.			
- Implemented as binary search trees	S	- Hash table used				
at(index) / operator[index]	Access element	at(index) / operator[index]	Access element			
rbegin / rend	Reverse beginning / end	_ equal_range(X)	Return the pair of iterators to the lower			
crbegin / crend	Const reverse beginning / end		bound & upper bound+1 of that element			
lower_bound (X)	Return the iterator to X	equal_range(v.begin(), v.end())	Return the pair of iterators to the lower			
upper_bound (X)	Return the iterator to 1 element > X		bound & upper bound+1 of that range			
lower_bound (v.begin, v.end(), X)	Return the iterator to pos X via BST	key_eq	?			
upper_bound (v.begin, v.end(), X)	Return the iterator to pos X via BST	hash_function	?			
key_comp	Define the order of the keys	bucket	?			
value_comp	Define the order of the values	bucket_count	?			
equal_range(X)	Return the pair of iterators to the lower	bucket_size	?			
	bound & upper bound+1 of that element	rehash	?			
equal_range(v.begin(), v.end())	Return the pair of iterators to the lower	load_factor	?			
	bound & upper bound+1 of that range	insert(first, second)	O(1)			
find(X)	Return the iterator point to X	_				
erase(X) / erase(it)	Erase all occurrence of X / delete *it					
Insert(first, second)	O(log N)					
multiset		unordered_multiset				
- Container that stores elements follow	owing a specific order and where multiple	- Containers that store elements in	no particular order, allowing fast retrieval of			
elements can have equivalent values	s (duplicates).	individual elements based on their	value.			
- Allow for direct iteration on subsets	s based on their order.	- Allow different elements to have equivalent values (duplicates).				

5. Binary Search Tree

A. General Properties

Query		Update		Others		
Search(v) $O(h) \sim O(N)$		Insert(v) $O(h) \sim O(N)$		Rank(v)	rank(Min())=1, rank(Max())=N	
Predecessor(v) / Successor(v)	O(h)	Remove(v)	O(h) ~ O(N)	Select(k)	Get the element at rank k	
Inorder traversal	O(logN) / O(N)	Create BST		BST Height	Floor(logN) ~ N	
Min / Max	O(h) ~ O(N)			AVL Height	log₂N < h < N	

B. Definition

Internal vertices	Leaf
- Nodes that are not leaf	- Nodes that have no other children
Successor	Predecessor
- If V has right subtree -> get min in the right subtree	- If V has left subtree -> get max in the left subtree
- If V has no right subtree -> traverse the ancestor until a right turn	- If V has no left subtree -> traverse the ancestor until a left turn
Remove	Insert
- O(1) for deletion of leaf / deletion of internal vertex that has only 1 child	- Insert at the last node and do bubble up/down
- O(h) for deletion of internal vertices that have 2 children	

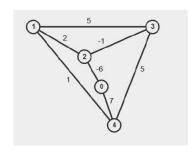
C. Adelson-Velskii & Landis Tree	D. Tree Traversal
- Height-balanced if v.left.height - v.right.height <= 1	Inorder:
- Compare the difference between left and right subtrees	1. Traverse the left subtree.
	2. Visit the root.
	3. Traverse the right subtree
1) bf(x) == +2; bf(x.left) == 1; right_rotate(x);	Preorder:
2) bf(x) == -2; bf(x.right) == -1; left_rotate(x);	1. Visit the root.
3) bf(x) == +2; bf(x.left) == -1; left_rotate(x.left); right_rotate(x);	2. Traverse the left subtree
4) bf(x) == -2; bf(x.right) == -1; right_rotate(x.right); left_rotate(x)	3. Traverse the right subtree
	Postorder:
	1. Traverse the left subtree
	2. Traverse the right subtree
	3. Visit the root

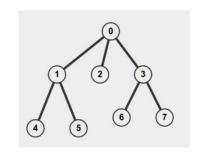
6. STL Containers

Container	Vecto	r	Stac Que		Deque	e	List		Priori	ty Queue	Set		Мар						
Insert	push_back	O(1)	push	O(1)	push_back push_front	O(1)	push_back push_front	O(1)	push	O(logN)	insert	O(logN)	[] operator	O(logN)					
Delete	pop_back	O(1)	рор	O(1)	pop_front pop_back	O(1)	pop_front pop_back	O(1)	pop	O(logN)	erase	O(logN)	erase	O(logN)					
Random Access	[] operator	O(1)	NIL		[] operator	O(1)	Loop Through	O(N)		NIL	find	O(logN)	[] operator	O(logN)					
Access	front back	O(1)	s.top q.front	O(1)	front back	O(1)	front back	O(1)	top	O(1)	NIL (Use iterators)								
Sorted	No (Use STL	sort)	No		No (Use STL :	sort)	No (Use List.s	sort)		Yes	Yes		Yes						
Binary Search	lower_bound upper_bound	O(logN)	NIL		lower_bound upper_bound	O(logN)	NIL			NIL	lower_bound upper_bound	O(logN)	lower_bound upper_bound	O(logN)					
Unique	No		No		No		No		No		No		No No		No	Yes (Use Multis non-unique		Unique l Non-unique (Use Multin non-unique	values nap for
Iterators	Yes		No		Yes		Yes			No	Yes		Yes						

7. General Properties of Graphs

A. Graph Representation





Edge List
Vertex u , Vertex v , Edge/weight w
(0, 2, -6)
(0, 4, 7)
(1, 2, 2)
(1, 3, 5)
(1, 4, 1)
(2, 3, -1)
(3, 4, 5)

vector stupic sint, int, inte	- vector <tup< th=""><th>le<int,< th=""><th>int,</th><th>int>></th></int,<></th></tup<>	le <int,< th=""><th>int,</th><th>int>></th></int,<>	int,	int>>
-------------------------------	---	---	------	-------

- Space Complexity O(E)

Adjacency	/ List
Vertex	List (neighbour, weight)
0	(2, -6), (4, 7)
1	(2, 2), (3, 5), (4, 1)
2	(0, -6), (1, 2), (3, -1)
3	(1, 5), (2, -1), (4, 5)
4	(0, 7), (1, 1), (3, 5)

- vector<vector<pair<int, int>>>
- Space Complexity O(V+E)

Adjace	ncy Ma	atrix			
-	0	1	2	3	4
0	-	-	-6	-	7
1	-	-	2	5	1
2	-6	2	1	-1	-
3	ı	5	-1	1	5
4	7	1	-	5	-

- Symmetric if bidirectional
- Space Complexity O(V²)
- 2D array
- O(1) checking

Tree Represen	tation
Vertex	Parent Node
0	-
1	0
2	0
3	0
4	1
5	1
6	3
7	3
- V-1 edges	

B. Directed Acyclic Graph	C. Complete Graph	D. Bipartite Graph
Definition: A graph whose edges are not bi-directional	Definition: A simple graph that is the densest.	Definition: Undirected graph with V vertices that can
and has no cycles or self-loops.		be partitioned into 2 disjoint set of vertices m , n
	Properties:	where V = m + n . There is no edge between members
Properties:	1) There is an edge between any pair of vertices.	of the same set.
•	2) A graph of V vertices and E = V(v-1)/2 edges	
1) Maximum number of directed edges of a graph	(E=O(V ²))	Properties:
with V number of vertices - V(V-1)/2.	3) No multi-edges, self-loops, unweighted,	2) Free from odd-length cycle
2) Adding more than V(V-1)/2 edges will form a bi-	undirected.	3) Complete graph if there's an edge from any m to all
directional edge.	4) Space complexity O(V ²)	n.

8. Graph Traversal

A. Depth First Search (DFS)

Definition: Starts from a source vertex s which has X neighbours. It then recursively (or with stack) explores all reachable vertices from the first neighbour u and backtrack to vertex u, then do the same for other neighbours until It finishes exploring the last neighbour and its reachable vertices.

Properties:

- 1) Time complexity O(V+E) -> adjacency list
- 2) Find connected components one DFS per CC. (still O(V+E))
- 3) Detecting cycle status[u] to update {unvisited, explored, visited}.
- 4) Bipartite checker (alternate colouring)
- 5) Find strongly connected components

B. Breadth First Search (BFS)

Definition: Starts from a source vertex s and uses a queue to order the visitation sequence as breadth as possible before going deeper. Every vertex of the same level order is enqueued and then dequeued to explore its neighbours which are then enqueued from the queue. Then dequeue the next one from the queue.

Properties:

- 1) Time complexity O(V+E) -> adjacency list
- 2) Spanning tree (in 2040C) a connected set of directed edges that form a rooted tree covering all vertices.
- 3) Topological sort
- 4) Find connected components
- 5) Bipartite checker
- 6) Applications: BitTorrent, social network, crawlers in search engines, GPS.

```
void dfs(int vertex_id) {
   if (visited[vertex_id]) return;
   visited[vertex_id] = true;

   for(int i=0; i<adjList[Vertex_id].size(); i++) {
       dfs(adjList[vertex_id][i]);
   }
}</pre>
```

```
void bfs(int source_v) {
   queue<int> q;
   visited[source_v] = 1;

   q.push(source_v);
   while(!q.empty()) {
      int v = q.front(); q.pop();
      for(auto& it : adjList[v]) {
        if(visited[it]) continue;
        q.push(it);
        visited[it] = 1;
      }
   }
}
```

9. Graph Traversal Application

A. Detecting cycles

DFS for a connected graph produces a tree. There is a cycle in a graph only if there is a back-edge present in the graph. Back-edge always point from a vertex to one of its ancestors. We need to track 3 states in the DFS – status[u] = {unvisited, exploring/explored, visited}.

B. Finding connected components

Enumerate all vertices v that are reachable from an **unvisited** vertex s in an undirected graph and enumerate all vertex v with status updated to **visited**.

```
void dfs(string place) {
    status[place] = 1; //exploring
    //cout << "mom at a newly explored city " << place <<endl; //test

for(auto &neighbours: cities[place]) {
    //cout << "mom is exploring this neighbour " << neighbours <<endl;

    if(status[neighbours]==0) dfs(neighbours); //to visit the neighbours
    else if(status[neighbours]==1) { //explored
        found = true;
        //cout << "mom found a cycle at " <<neighbours <<endl;
    }
}

status[place] = 2; //fully visited
    //cout << "mom finish visitng this city " <<place <<endl;
}</pre>
```

C. Topological Sort / Kahn's Algorithm

Linear ordering in directed acyclic graph in which each vertex comes before all vertices to which it has outbound edges.

- 1) Min number of topological ordering: 1
- 2) Max number of topological ordering: V! (for V disjoint vertices which gives O(V!))

D. Bipartite Checker

Check whether the set of vertices can be divided into two sets such that there is an edge between set 1 and set 2 but no edges belonging to the same set.

- Use BFS to 'colour' the vertices. Adjacent vertices should have different colours.

10. Single-Source Shortest Paths

Algorithm	Bellman Ford	Dijkstra	Modified Dijkstra	DFS	BFS	Dynamic
						Programming
Time Complexity	O(VE) - very very slow	O((V+E)*logV)	O((V+E)*logV)	O(V+E)	O(V+E)	O(V+E)
Negative weight	Yes	No	Yes	No	No	Yes
Negative cycle	No -INF	No	No	No	No	No
Faster Algorithm	- Detect negative	- Graph without	- Graph without	-Tree	- Unweighted graphs	- Directed Acyclic
for SSSP	cycle	negative weight	negative weight cycle		- Tree	Graphs
All Pairs Shortest	lol	-O(V(V+E)logV)	- O(V(V+E)logV)	- O(V(V+E))	- O(V(V+E))	- Floyd Warshall
Path (APSP)						- O(V ³)

A. Bellman Ford's Algorithm

```
Algorithm

void bellman_ford() {
    dist[s]=0;

    for(int i=1; i<V-1; i++) {
        for(auto&x : egdeList) {
            //if tuple is used
            u = get<0>(x);
            v = get<1>(x);
            w = get<2>(x);

            //relax
            dist[v] = min(dist[v], dist[u]+w);
        }
    }
}
```

Application – finding negative cycles (run once will do)

Bellman Ford Killer (VisuAlgo processes edges in decreasing order)



B. Dijkstra

Time Complexity Explanation

The implementation of min heap extractMin() runs in O(logV). Since V vertices will be extracted, it will be O(VlogV). Also, all the edges will be relaxed and updated in the min heap with the previous value deleted, giving O(ElogV). Thus O((V+E)logV).

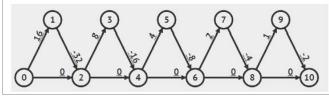
Dijkstra Algorithm

Real Life Application

- Electric car loses (positive) energy on uphill and gains (negative) energy on
- Money exchanger (where negative cycle possibly exists)

Modified Dijkstra Algorithm (Lazy Update)

Dijkstra / Modified dijkstra killer (wrong answer / TLE)



C. Floyd Warshall

Algorithm

Find the length of all the shortest paths between all pairs of vertices.

11. Sample Question

- **1.** In DFS/BFS, compare stack/queue implementation with recursion?
- Stack/Queue consumes memory and is cache-friendly, recursive calls might take up a huge portion of RAM
- Stack uses only one traversal at a time
- 2. Find the second shortest path with at least a differing edge
- Solvable by Floyd Warshall
- Select one edge from U -> V; Find the shortest path from Source->U and V-> Destination by enumerating all edges.
- **3.** Set intersection/union between two sorted arrays A and B.
- If binary search is used: intersection -> O(N log M); union -> O(N log M + M log N) for arrA[N] and arrB[N].
- Use 2 pointers method -> if *pointer A > *pointer B, pointer B increases; if *pointer B > *pointer A, pointer A increases; if they are equal, intersection is found.
- This results in a time complexity of O(N+M).
- **4.** Finding a target pair x and y such that x+y equals to a target z in the same array.
- If binary search is used: O(N log N).
- Use 2 pointers method -> set pointer X = arr.begin() and pointer Y = arr.end() 1; if *pointer X + *pointer Y < Z, pointer X + *pointer X + *pointer Y > Z, pointer Y --; if the sum equals to Z, keep it and move the two pointers towards the centre.
- **5.** Array v.s. vector
- Array: specific number of elements of a data type + may result in unused extra space.
- Vector: dynamic memory allocation + no declaration of array size.
- **6.** Array v.s. linked list implementation

Array	Linked List
- Collection of elements having same data type.	- An ordered collection of elements which are linked by pointers.

- Array provides fast and random access in O(1) operation	- Elements can only be accessed sequentially in O(N) operation
- Elements are stored in consecutive manner in memory	- Dynamic allocation of nodes.
- Insertion and deletion takes O(N) time	- Fast insertion and deletion.
- Can be single dimension or multidimensional	- Singly, doubly or circular linked list
- No requirement of extra space to store pointer	- Extra memory is needed for the pointers in each node.

7. Reverse a SLL?

- Loop through L, store pointers to every element in an array. Then loop through the array in reverse order, construct the reversed linked list.
- This results in O(N). We only can do this in O(N) time since there are N elements in total.

8. Reverse a queue?

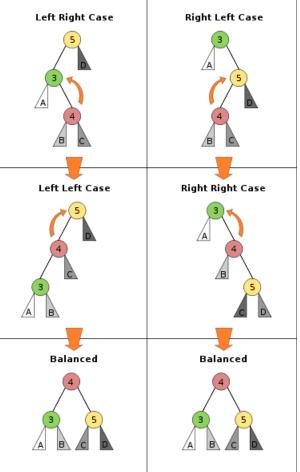
- Push the front of the queue into stack and then de-queue. After every element is transferred to the stack, push/enqueue the top of the stack into the queue and then pop the top of the stack.
- This results in O(N) operation. We only can do this in O(N) time since there are N elements in total.
- 9. Why is quick sort recommended for array but merge sort for linked list?
- Quick sort is an in-place sort which does not require any extra storage whereas merge sort requires O(N) extra storage. The N denoting the array size can be quite expensive. Allocating and de-allocating the extra space used for merge sort increases the running time of the algorithm. Unlike arrays, linked list nodes may not be adjacent in memory so we cannot do random access in the linked list. Random quick sort requires a lot of this random access while merge sort accesses the data sequentially. Inserting items in the middle in the linked list requires O(1) extra space and O(1) time.

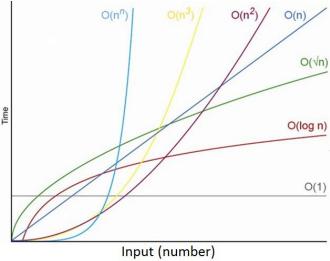
10. Simulate a calculator

- Use stack A to store brackets and numbers and stack B to store the operators. Whenever the closing bracket is read, operate the numbers with the operator from the top of stack B until an opening bracket is read in stack A.

DEC HEX 00 00h 01 01h 02 02h	O2h	SIX SIX	HEX Simbolo ASCII Oth NULL (carácter nulo) Oth SOH (inicio encabezado) OZIX (finicio texta)	33 S R	C HEX 20h 21h	DEC HEX Simbolo DEC 2 20h espacio 64 33 24h " 65 34 22h " 65	olo DEC HEJ cio 64 401 65 411	40: HE
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3	12h	DC2	(device control 2)	50		2	82	52
20	141	3 2	(device control 3)	5 5	34h	. ۵	3 2	54
21	15h	NAK	(negative acknowle.)	53		5	85	
22	16h	SYN	(synchronous idle)	54		6	86	
23	17h	B	(end of trans, block)	2 25		7	87	
24	9 8	E A	(end of medium)	57 00		۰ ۵	8 8	
26	1Ah	SUB	(substitute)	58			90	5AH
27	1Bh	ESC	(escape)	59		٠.	91	58
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characters	ers								Exte	Extended ASCII characters	CII ch	aract	ers			
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Members		set	multiset	map	multimap	unordered_set	unordered_multiset	unordered_map	unordered_multimap
	constructor	set	multiset	map	multimap	unordered_set	unordered_multiset	unordered_map	unordered_multimap
	destructor	~set	~multiset	~map	~multimap	~unordered_set	~unordered_multiset	~unordered_map	~unordered_multimap
	assignment	operator=	operator=	operator=	operator=	operator=	operator=	operator=	operator=
	begin	begin	begin	begin	begin	begin	begin	begin	begin
iterators	end	end	end	end	end	end	end	end	end
iterators	rbegin	rbegin	rbegin	rbegin	rbegin				
	rend	rend	rend	rend	rend				
	cbegin	cbegin	cbegin	cbegin	cbegin	cbegin	cbegin	cbegin	cbegin
const	cend	cend	cend	cend	cend	cend	cend	cend	cend
iterators	crbegin	crbegin	crbegin	crbegin	crbegin				
	crend	crend	crend	crend	crend				
	size	size	size	size	size	size	size	size	size
	max_size	max_size	max_size	max_size	max_size	max_size	max_size	max_size	max_size
capacity	empty	empty	empty	empty	empty	empty	empty	empty	empty
	reserve					reserve	reserve	reserve	reserve
element	at			at				at	
access	operator[]			operator[]				operator[]	
	emplace	emplace	emplace	emplace	emplace	emplace	emplace	emplace	emplace
modifiers	emplace_hint	emplace_hint	emplace_hint	emplace_hint	emplace_hint	emplace_hint	emplace_hint	emplace_hint	emplace_hint
	insert	insert	insert	insert	insert	insert	insert	insert	insert
modifiers	erase	erase	erase	erase	erase	erase	erase	erase	erase
	clear	clear	clear	clear	clear	clear	clear	clear	clear
	swap	swap	swap	swap	swap	swap	swap	swap	swap
	count	count	count	count	count	count	count	count	count
	find	find	find	find	find	find	find	find	find
operations	equal_range	equal_range	equal_range	equal_range	equal_range	equal_range	equal_range	equal_range	equal_range
	lower_bound	lower_bound	lower_bound	lower_bound	lower_bound				
	upper_bound	upper_bound	upper_bound	upper_bound	upper_bound				
	get_allocator	get_allocator	get_allocator	get_allocator	get_allocator	get_allocator	get_allocator	get_allocator	get_allocator
	key_comp	key_comp	key_comp	key_comp	key_comp				
observers	value_comp	value_comp	value_comp	value_comp	value_comp				
	key_eq					key_eq	key_eq	key_eq	key_eq
	hash function					hash_function	hash_function	hash_function	hash_function
	bucket					bucket	bucket	bucket	bucket
	bucket_count					bucket_count	bucket_count	bucket_count	bucket_count
buckets	bucket_size					bucket_size	bucket_size	bucket_size	bucket_size
buckets	max bucket count						max_bucket_count		max_bucket_count
	rehash					rehash	rehash	rehash	rehash
hash	load factor					load_factor	load_factor	load_factor	load_factor
policy	max_load_factor					max_load_factor	max_load_factor		max_load_factor