

Semana 4

Tarefa Básica

1. a) $\begin{vmatrix} 1 & a & 0 & 1 & a \\ 0 & 1 & 1 & 0 & 1 \\ 0 & -1 & 1 & -1 & -1 \end{vmatrix}$ $1+(-a)+0-0-(-1)-0=2$

b) $\begin{vmatrix} 1 & -1 & 4 & 1 & -1 \\ 0 & 0 & 3 & 0 & 0 \\ 1 & 1 & 4 & 1 & 1 \end{vmatrix}$ $0+(-3)+0-0-3-0=-6$

2) $\begin{vmatrix} x^2 & 0 & x & -1/10 \\ 7,5 & 0 & 5 & 2 \\ 10 & 0 & 4 & 2 \\ 1 & 1 & 1 & 1 \end{vmatrix} = 0$ $\begin{vmatrix} x^2 & x & -1/10 \\ 7,5 & 5 & 2 \\ 10 & 4 & 2 \end{vmatrix}$

$\therefore x^2 \cdot \det \begin{bmatrix} 5 & 2 \\ 4 & 2 \end{bmatrix} - x \det \begin{bmatrix} 7,5 & 2 \\ 10 & 2 \end{bmatrix} + \frac{-1}{10} \det \begin{bmatrix} 7,5 & 5 \\ 10 & 4 \end{bmatrix}$

$\det \begin{bmatrix} 5 & 2 \\ 4 & 2 \end{bmatrix} = 2$ $\det \begin{bmatrix} 7,5 & 2 \\ 10 & 2 \end{bmatrix} = -5$ $\det \begin{bmatrix} 7,5 & 5 \\ 10 & 4 \end{bmatrix} = -20$

$x^2 \cdot 2 - x(-5) + \frac{-1}{10}(-20)$
 $2x^2 + 5x + 2 = 0$

$\Delta = 5^2 - 4 \cdot 2 \cdot 2$ $x = \frac{-5 \pm \sqrt{9}}{2 \cdot 2}$ $x_1 = \frac{5-3}{4} = \frac{2}{4} = \frac{1}{2}$
 $\Delta = 25 - 16$ $x_2 = \frac{-5+3}{4} = \frac{-2}{4} = -\frac{1}{2}$
 $\Delta = 9$ $x_3 = \frac{5+3}{4} = \frac{8}{4} = 2$ $x_4 = \frac{-5-3}{4} = \frac{-8}{4} = -2$

$$3) \begin{bmatrix} x & 0 & 0 & 3 \\ -1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{bmatrix} = -1 \quad \begin{bmatrix} x \cdot (-1) & 0 \cdot (-1) & 0 \cdot (-1) & 3 \\ -1 & x \cdot (-1) & 0 \cdot (-1) & 0 \cdot (-1) \\ 0 \cdot (-1) & 0 \cdot (-1) & -1 & -2 \end{bmatrix}$$

$$\begin{bmatrix} -x & 0 & 0 & 3 \\ 1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{bmatrix} \xrightarrow{(-1)} \begin{bmatrix} -x & 0 & 0 & 3 \\ 1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{bmatrix} = \begin{bmatrix} -1 & x & 0 & 0 \\ -x & 0 & 0 & 3 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{bmatrix}$$

$$\begin{bmatrix} 0 - (-x) \cdot x & 0 - (-x) \cdot 0 & 3 - (-x) \cdot 0 \\ -1 - 0 \cdot x & x - 0 \cdot 0 & 1 - 0 \cdot 0 \\ 0 - 0 \cdot x & -1 - 0 \cdot 0 & -2 - 0 \cdot 0 \end{bmatrix} \begin{bmatrix} x^2 & 0 & 3 \\ -1 & x & 1 \\ 0 & -1 & -2 \end{bmatrix} = 2x^3 + x^2 + 3 //$$

$$4) \begin{bmatrix} x & 1 & 0 & 0 & 0 \\ 0 & x & 1 & 0 & 0 \\ 0 & 0 & x & 1 & 0 \\ 0 & 0 & 0 & x & K \\ 0 & 0 & 0 & 1 & x \end{bmatrix} = \begin{bmatrix} x & x \\ 1 & x \end{bmatrix} = x^2 - 1K = K^5$$

$$f(x) = x^5 - Kx^3$$

$$f(-2) = -32 + 8K = 8$$

$$8K = 40$$

$$K = 40/8 = 5 //$$