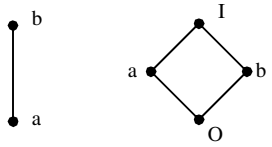
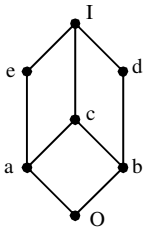
Tutorial Sheet – IX
(Boolean algebra, Language and Grammar)

1. Which of the following lattices are Boolean algebra?
   (a) D_{20} (b) D_{55} (c) D_{99} (d) D_{130} (e) D_{210}
2. Which of the following are Boolean algebra

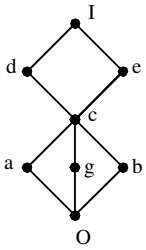


(Fig 1.a)

(Fig 1.b)



(Fig 1.c)



(Fig 1.d)

3. Consider the words $u = a^3bab^2$ and $v = baba^2$. Find:
   (i) uvu (ii) λu (iii) λv (iv) $u\lambda v$ (v) $|\lambda|$ (vi) $|u|$ (vii) $|uvu|$
4. Consider the language $L = \{ab, c\}$ over $A = \{a, b, c\}$. Find:
   (i) L^0 (ii) L^2 (iii) L^{-1}
5. For the finite state machine M given in the table A, find out the string among the following strings, which are accepted by M : (a) 101101 (b) 11111 (c) 000000

	Inputs	
States	0	1
q_0	q_2	q_1
q_1	q_3	q_0
q_2	q_0	q_3
q_3	q_1	q_2

Accepting states are q_0, q_2

Table A

	Inputs	
States	a	b
s_0	s_0	s_1
s_1	s_1	s_2
s_2	s_2	s_2

Table B

6. Let M be the automaton with the following input set A, state set S , and accepting or final ("yes") state set Y: $A = \{a, b\}$, $S = \{s_0, s_1, s_2\}$, $Y = \{s_1\}$. Suppose s_0 is the initial state of M , and next state function F of M is given by the table B. Draw the state diagram $D = D(M)$ of the automaton M .

7. Construct the state diagram for the finite-state machine with the state table shown below**.**

8. Construct the state table for the finite-state machine with the state diagram shown in **Figure 1.**

F	Inputs	
States	0	1
s_0	$s_1, 1$	$s_0, 0$
s_1	$s_3, 1$	$s_0, 1$
s_2	$s_1, 0$	$s_2, 1$
s_3	$s_2, 0$	$s_1, 0$

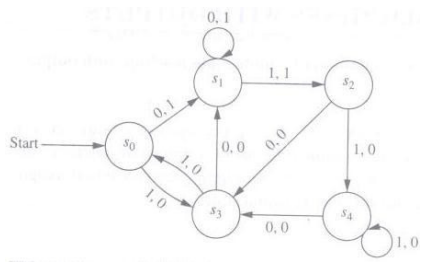


Table C

9. Find the output string generated by the finite state machine in **Figure 1** if the input string is (i) 000000 (ii) 111111 (iii) 101011 (iv) 110101
10. Describe the language $L = L(G)$, where G has the productions $S \to aSb, Sb \to bA, abA \to c$.