

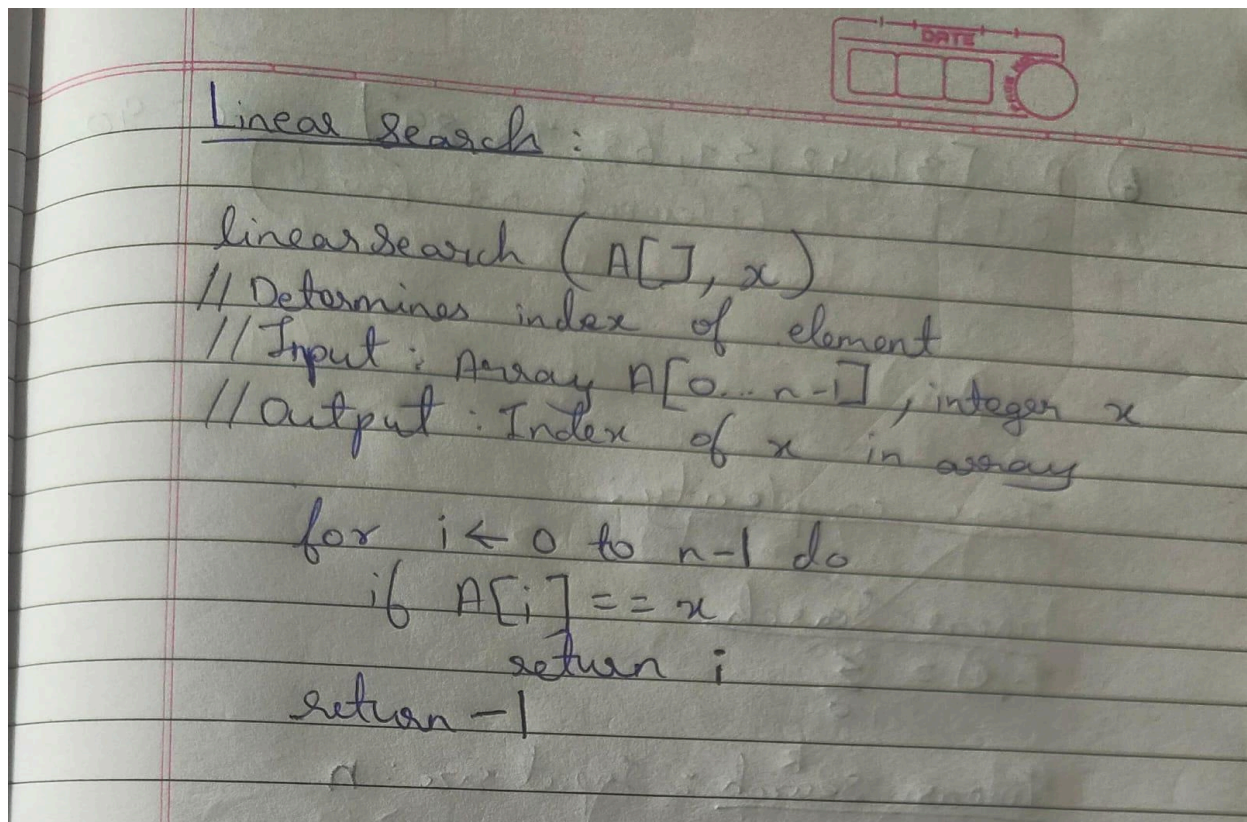
DAA Assignment 2

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Q. Write an algorithm for Linear Search and Binary Search. Write a program to solve the given problem using your algorithms. Apply coding style in your programs.

Algorithm:

Linear Search:



Binary search:

Binary Search :

binarysearch($A[0 \dots n-1]$, x , low, high)

// Determines index of element

// Input: Array $A[0 \dots n-1]$, integer x ,
low start of search array low,
end of search array high

// Output: Index of x in array

if low > high
return -1

mid $\leftarrow (low + high) / 2$

if $A[mid] == x$
return mid

else if $A[mid] < x$
return binarysearch($A, x, mid+1, high$)

else
return binarysearch($A, x, low, mid-1$)

Test cases:

Test cases:

1) $A = [3, 5, 9, 10, 18, 21]$ $x = 9$
Output: 2

2) $A = [1, 10, 20, 42, 57, 99]$ $x = 41$
Output: -1 (element not found)

3) $A = [12, 14, 20, 37, 41, 58]$ $x = 15$
Output: -1 (element not found)

4) $A = [105, 210, 321, 410, 500]$ $x = 105$
Output: 0

5) $A = [7, 10, 11, 19, 25, 33]$ $x = 33$
Output: 5

6) $A = [31, 42, 57, 68, 73, 89]$ $x = 90$
Output: -1 (element not found)

Time Complexity:

Linear Search: Input size: n

$$C_{\text{worst}}(n) = \sum_{i=0}^{n-1} 1 = [(n-1) + 1]$$

$$= n$$
$$\therefore T.C \in O(n)$$

Binary Search:

Input size: n

Basic operation: Check conditions and make a recursive call

Let $A(n)$ be time complexity of algorithm

$$A(n) = A(n/2) + c, \quad A(1) = c$$

where c is the time required to check the conditions.

$$A(n/2) = A(n/4) + c$$

$$\therefore A(n) = A(n/4) + 2c$$

$$A(n) = A(n/8) + 3c \quad [A(n/4) = A(n/8) + c]$$

$$\therefore A(n) = A(1) + kc, \quad k = \text{constant}$$

$$A(n) = A(n/2^k) + kc$$

$$A(n) = A(1) + C, \quad C = \text{constant}$$

$$A(n/2^k) = A(1)$$

$$n/2^k = 1$$

$$\therefore n = 2^k$$

$$\therefore \log_2 n = k$$

$$A(n) = A(n/2^{\log_2 n}) + c \log_2 n$$

$$= A(n/n) + c \log_2 n$$

$$= c + c \log_2 n$$

$$A(n) = c(1 + \log_2 n)$$

$$\therefore \text{Time complexity} \in O(\log_2 n)$$

Program:

```
def linear_search(arr, x):
    for i in range(len(arr)):
        if arr[i] == x:
            return i
    return -1

def binary_search(arr, x, low, high):
    if low > high:
        return -1
    mid = (high + low) // 2
    if arr[mid] == x:
        return mid
    elif arr[mid] > x:
        return binary_search(arr, x, low, mid - 1)
    else:
        return binary_search(arr, x, mid + 1, high)

def main():
    arr = []
    n = int(input("Enter number of elements: "))
    for i in range(n):
        arr.append(int(input(f"Enter element {i + 1}: ")))
    x = int(input("Enter element to search: "))
    print(f"Index of {x} using linear search: {linear_search(arr, x)}")
    print(f"Index of {x} using binary search: {binary_search(arr, x, 0, len(arr) - 1)}")

if __name__ == "__main__":
    main()
```

Output:

1.

```
Enter number of elements: 6
Enter element 1: 3
Enter element 2: 5
Enter element 3: 9
Enter element 4: 10
Enter element 5: 15
Enter element 6: 21
Enter element to search: 9
Index of 9 using linear search: 2
Index of 9 using binary search: 2
```

2.

```
Enter number of elements: 6
Enter element 1: 1
Enter element 2: 10
Enter element 3: 20
Enter element 4: 42
Enter element 5: 57
Enter element 6: 99
Enter element to search: 41
Index of 41 using linear search: -1
Index of 41 using binary search: -1
```

3.

```
Enter number of elements: 6
Enter element 1: 12
Enter element 2: 14
Enter element 3: 20
Enter element 4: 37
Enter element 5: 41
Enter element 6: 58
Enter element to search: 15
Index of 15 using linear search: -1
Index of 15 using binary search: -1
```

4.

```
Enter number of elements: 5
Enter element 1: 105
Enter element 2: 210
Enter element 3: 321
Enter element 4: 410
Enter element 5: 500
Enter element to search: 105
Index of 105 using linear search: 0
Index of 105 using binary search: 0
```

5.

```
Enter number of elements: 6
Enter element 1: 7
Enter element 2: 10
Enter element 3: 11
Enter element 4: 19
Enter element 5: 25
Enter element 6: 33
Enter element to search: 33
Index of 33 using linear search: 5
Index of 33 using binary search: 5
```

6.

```
Enter number of elements: 6
Enter element 1: 31
Enter element 2: 42
Enter element 3: 57
Enter element 4: 68
Enter element 5: 73
Enter element 6: 89
Enter element to search: 90
Index of 90 using linear search: -1
Index of 90 using binary search: -1
```

Conclusion: Hence, in this practical, we have studied what coding style is and how to write code using a specific coding style. We have also studied

and analysed the time complexity of linear search and binary search algorithms.