

## ASSIGNMENT 10

APL106

1. Air flows isentropically through a converging nozzle into a receiver in which the absolute pressure is 240 kPa. The air enters the nozzle with negligible speed at a pressure of 406 kPa (abs) and a temperature of 95°C. Determine the flow rate through the nozzle for a throat area of 0.01 m<sup>2</sup>.
2. A large tank supplies air to a converging nozzle that discharges to atmospheric pressure. Assume the flow is reversible and adiabatic. For what range of tank pressures will the flow at the nozzle exit be sonic? If the tank pressure is 600 kPa (abs) and the temperature is 600 K, determine the mass flow rate through the nozzle, if the exit area is  $1.29 \times 10^{-3}$  m<sup>2</sup>.
3. A large insulated tank, pressurized to 620 kPa (gage), supplies air to a converging nozzle which discharges to atmosphere. The initial temperature in the tank is 127°C. When flow through the nozzle is initiated, what is the Mach number in the exit plane of the nozzle? What is the pressure in the exit plane when the flow is initiated? At what condition will the exit-plane Mach number change? How will the exit-plane pressure vary with time? How will flow rate through the nozzle vary with time? What would you estimate the air temperature in the tank to be when flow through the nozzle approaches zero?
4. Air is to be expanded through a converging-diverging nozzle by a frictionless adiabatic process, from a pressure of 1.10 MPa (abs) and a temperature of 115°C, to a pressure of 141 kPa (abs). Determine the throat and exit areas for a well-designed shockless nozzle, if the mass flow rate is 2 kg/s.

5. A converging-diverging nozzle is attached to a large tank of air, in which  $T_{01} = 300 \text{ K}$  and  $p_{01} = 250 \text{ kPa (abs)}$ . At the nozzle throat (section of minimum area) the pressure is  $132 \text{ kPa (abs)}$ . In the diverging section, the pressure falls to  $68.1 \text{ kPa}$  before rising suddenly across a normal shock. At the nozzle exit the pressure is  $180 \text{ kPa}$ . Find the Mach number immediately behind the shock. Determine the pressure immediately downstream from the shock. Calculate the entropy change across the shock. Sketch the  $Ts$  diagram for this flow, indicating static and stagnation state points for conditions at the nozzle throat, both sides of the shock, and the exit plane.
  
6. Air flows adiabatically from a reservoir, where  $T_{01} = 60^\circ\text{C}$  and  $p_{01} = 600 \text{ kPa (abs)}$ , through a converging-diverging nozzle. The design Mach number of the nozzle is  $2.94$ . A normal shock occurs at the location in the nozzle where  $M = 2.42$ . Assuming isentropic flow before and after the shock, determine the back pressure downstream from the nozzle. Sketch the pressure distribution.
  
7. A stationary normal shock stands in the diverging section of a converging-diverging nozzle. The Mach number ahead of the shock is  $3.0$ . The nozzle area at the shock is  $500 \text{ mm}^2$ . The nozzle is fed from a large tank where the pressure is  $1000 \text{ kPa (gage)}$  and the temperature is  $400 \text{ K}$ . Find the Mach number, stagnation pressure, and static pressure after the shock. Calculate the nozzle throat area. Evaluate the entropy change across the shock. Finally, if the nozzle exit area is  $600 \text{ mm}^2$ , estimate the exit Mach number. Would the actual exit Mach number be higher, lower, or the same as your estimate? Why?