

Chapter 2

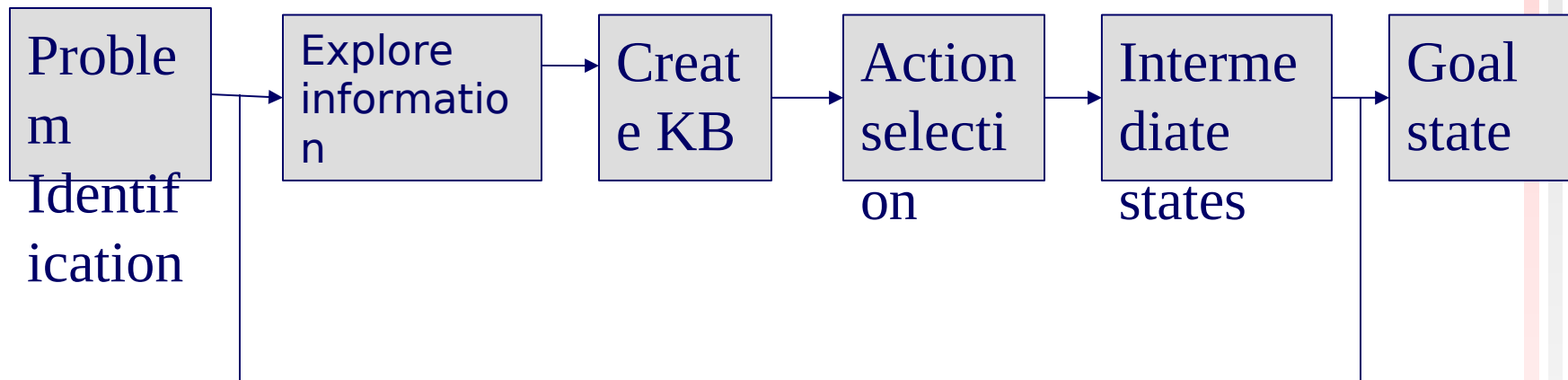
Problems, Problem Spaces, and Search?

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Problem solving Process

A systematic approach to defining the problem (question or situation that presents **uncertainty, perplexity or difficulty**) and creating a vast number of possible solutions without judging these solutions

Problem solving Process



Problem solving
process

Problem solving Process

Problem solving techniques involve the following:

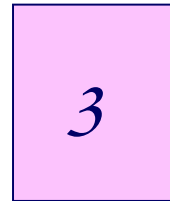
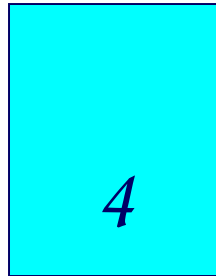
- Problem identification
- Problem analysis and representation
- Planning
- Execution
- Evaluating solution
- Consolidating gains

State Space

- Before an AI problem can be solved it **must be represented as a state space**. The state space is then searched to find a solution to the problem.
- A state space essentially consists of a **set of nodes** representing each state of the problem, arcs between nodes representing the legal moves from one state to another, an initial state and a goal state.
- Each state space takes the form of a tree or a graph.

Defining the problem

- *A water jug problem: 4-gallon and 3-gallon*



- *no marker on the bottle*
- *pump to fill the water into the jug*
- *How can you get exactly 2 gallons of water into the 4-gallons jug?*

A state space search

(x,y) : order pair

x : water in 4-gallons $\rightarrow x = 0,1,2,3,4$

y : water in 3-gallons $\rightarrow y = 0,1,2,3$

start state : $(0,0)$

goal state : $(2,n)$ where $n = \text{any value}$

- Rules :
1. Fill the 4 gallon-jug $(4,-)$
 2. Fill the 3 gallon-jug $(-,3)$
 3. Empty the 4 gallon-jug $(0,-)$
 4. Empty the 3 gallon-jug $(-,0)$

Water jug rules

- | | | | |
|---|---|--------------------------------|--|
| 1 | (x, y)
if $x < 4$ | $\rightarrow (4, y)$ | Fill the 4-gallon jug |
| 2 | (x, y)
if $y < 3$ | $\rightarrow (x, 3)$ | Fill the 3-gallon jug |
| 3 | (x, y)
if $x > 0$ | $\rightarrow (x - d, y)$ | Pour some water out of
the 4-gallon jug |
| 4 | (x, y)
if $y > 0$ | $\rightarrow (x, y - d)$ | Pour some water out of
the 3-gallon jug |
| 5 | (x, y)
if $x > 0$ | $\rightarrow (0, y)$ | Empty the 4-gallon jug
on the ground |
| 6 | (x, y)
if $y > 0$ | $\rightarrow (x, 0)$ | Empty the 3-gallon jug
on the ground |
| 7 | (x, y)
if $x + y \geq 4$ and $y > 0$ | $\rightarrow (4, y - (4 - x))$ | Pour water from the
3-gallon jug into the
4-gallon jug until the
4-gallon jug is full |

Water jug rules

- | | | | |
|----|---|--------------------------------|--|
| 8 | (x, y)
if $x + y \geq 3$ and $x > 0$ | $\rightarrow (x - (3 - y), 3)$ | Pour water from the
4-gallon jug into the
3-gallon jug until the
3-gallon jug is full |
| 9 | (x, y)
if $x + y \leq 4$ and $y > 0$ | $\rightarrow (x + y, 0)$ | Pour all the water
from the 3-gallon jug
into the 4-gallon jug |
| 10 | (x, y)
if $x + y \leq 3$ and $x > 0$ | $\rightarrow (0, x + y)$ | Pour all the water
from the 4-gallon jug
into the 3-gallon jug |
| 11 | $(0, 2)$ | $\rightarrow (2, 0)$ | Pour the 2 gallons
from the 3-gallon jug
into the 4-gallon jug |
| 12 | $(2, y)$ | $\rightarrow (0, y)$ | Empty the 2 gallons in
the 4-gallon jug on
the ground |

A water jug solution

4-Gallon Jug

3-Gallon Jug

Rule Applied



0

3

2

3

0

9

3

3

2

4

2

7

0

2

5 or 12



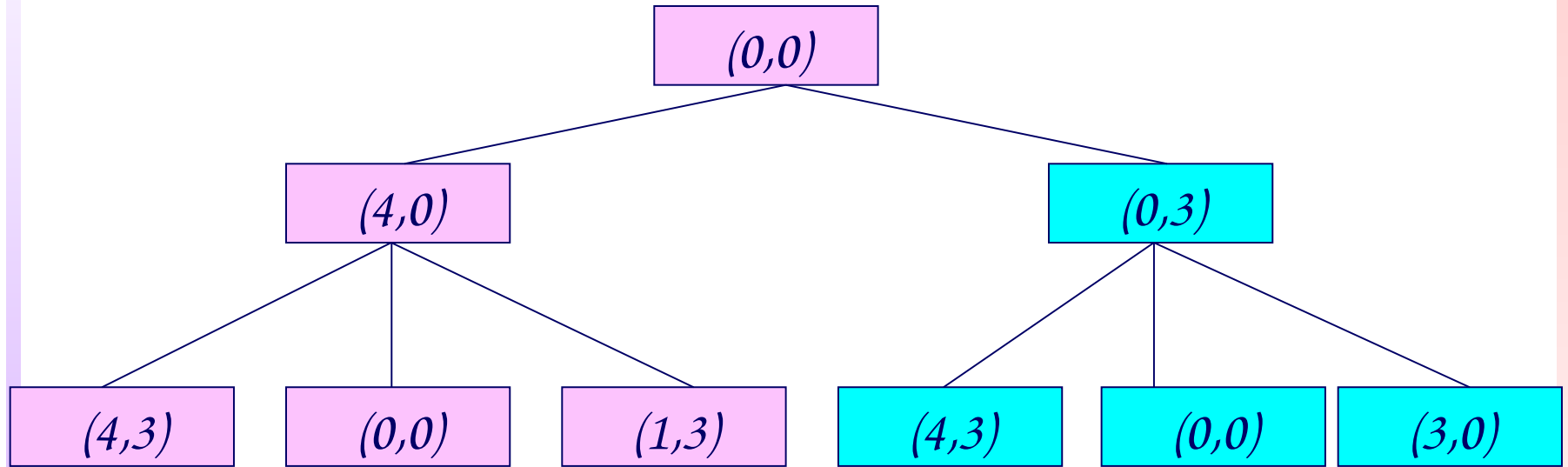
9 or 11

Solution : path / plan

Formal description of a problem

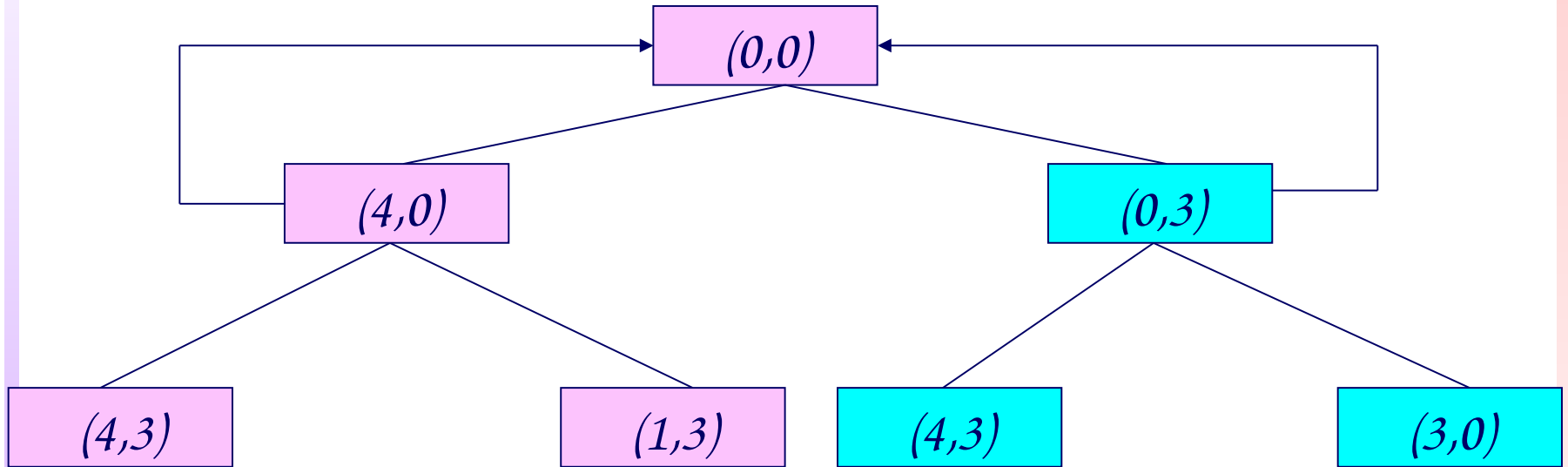
1. *Define a state space that contains all the possible configurations of the relevant objects.*
2. *Specify state/states that describes the situation of start state.*
3. *Specify state/states that describes the situation of goal state.*
4. *Specify the set of rules.*
 - assumption, generalization

Search Tree



Water jug problem.

Search Graph



- *Water jug problem.*
 - *Cycle: good control strategy that causes motion (BFS/DFS)*
 - *When will the search terminate?*

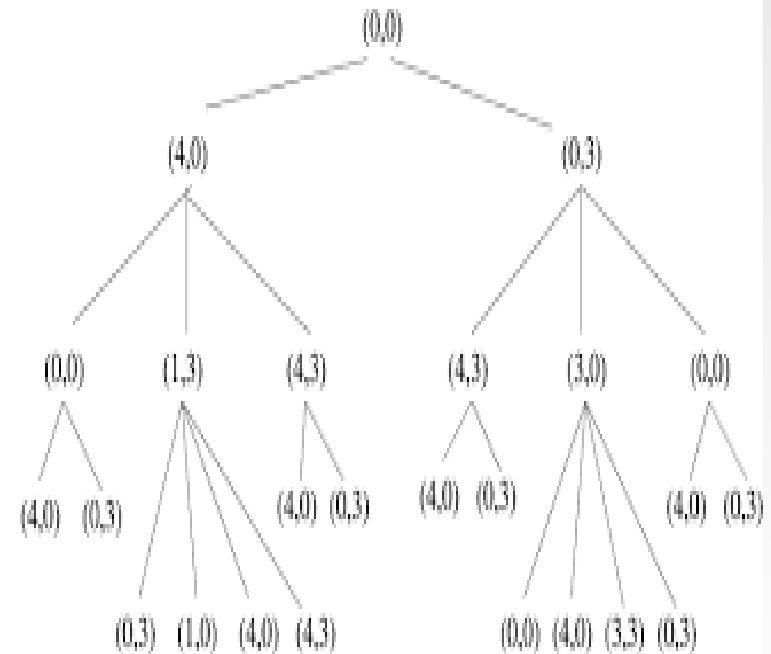
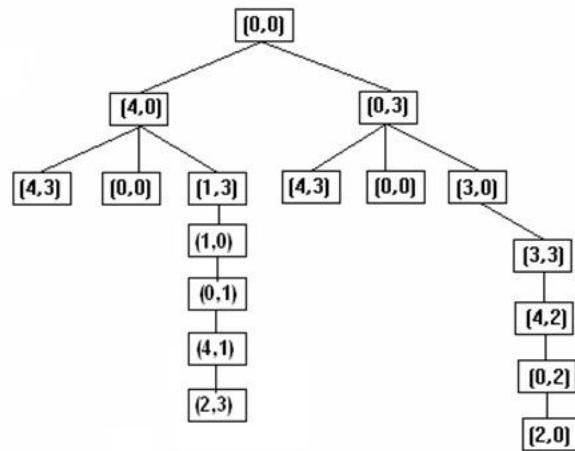
Water Jug Problem

- States: *Amount of water in jugs*
- Goal: *To get the specified amount of water in big jug .*
- Path cost: *Number of actions applied.(minimum the no of actions better is the solution)*
- Actions:
 1. *Empty the big jug*
 2. *Empty the small jug*
 3. *Pour water from small jug to big jug*
 4. *Pour water from big jug to small jug*

State Space : Water jug

Example: Water jug problem

State space representation



Homework

- *Is there any other solution for a water jug problem?*
- *If there is some other solution, describe in an order pair of how to solve it.*

State Space: Tic- tac- toe problem

Initial state Goal State

	x	

o		x
o	x	x
x	o	

Initial State: *State in figure*

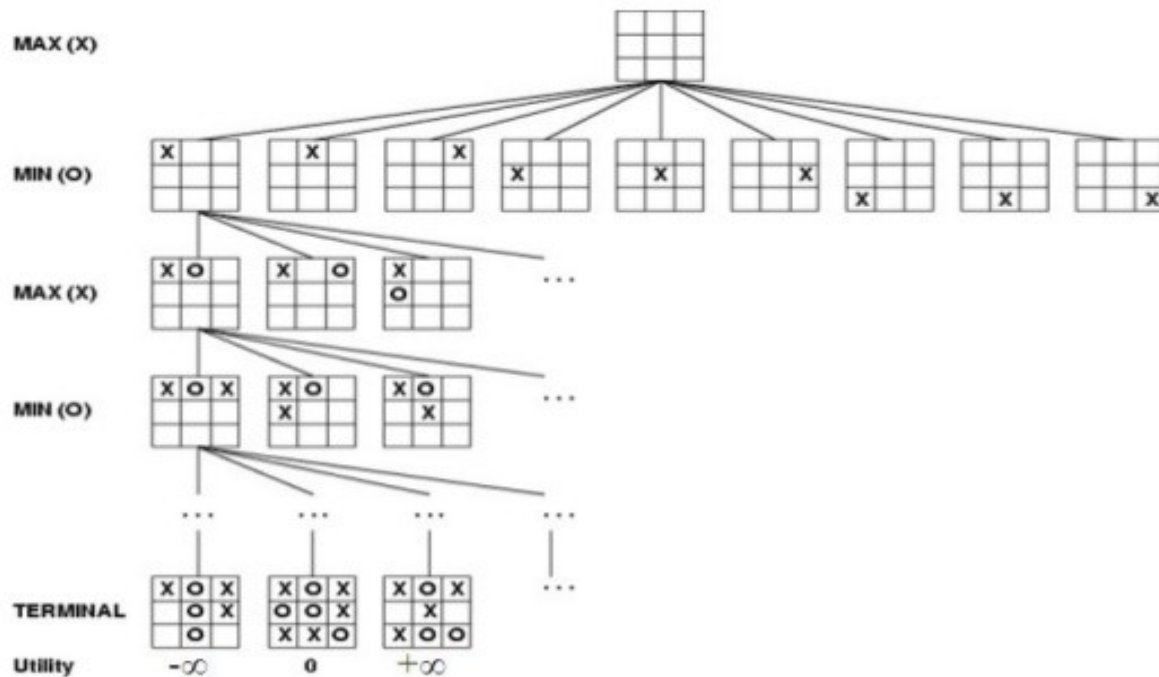
Goal State: *To reach the final winning position*

Operator: *adding 'x' or 'o' in cells one by one*

Path cost: *Each step costs 1 so that the path cost is the length of the path*

State Space: Tic-tac-toe problem

Game tree for Tic-Tac-Toe



Question answering question

1. *Marcus was a man.*
2. *Marcus was a Pompeian.*
3. *Marcus was born in 40 A.D.*
4. *All men are mortal.*
5. *All Pompeians died when the volcano erupted in 79 A.D.*
6. *No mortal lives longer than 150 years.*
7. *It is now 1991 A.D.*

Is Marcus alive?

Solution 1

- | | |
|---|----------------|
| 1. <i>Marcus was man.</i> | <i>axiom 1</i> |
| 4. <i>All men are mortal.</i> | <i>axiom 4</i> |
| 8. <i>Marcus is mortal.</i> | <i>1,4</i> |
| 3. <i>Marcus was born in 40 A.D.</i> | <i>axiom 3</i> |
| 7. <i>It is now 1991 A.D.</i> | <i>axiom 7</i> |
| 9. <i>Marcus' age is 1951 years.</i> | <i>3,7</i> |
| 6. <i>No mortal lives longer than 150 years</i> | <i>axiom 6</i> |
| 10. <i>Marcus is dead.</i> | <i>8,6,9</i> |

Solution 2

<i>7. It is now 1991 A.D.</i>	<i>axiom 7</i>
<i>5. All Pompeians died in 79 A.D.</i>	<i>axiom 5</i>
<i>11. All Pompeians are dead now.</i>	<i>7,5</i>
<i>2. Marcus was a Pompeian.</i>	<i>axiom 2</i>
<i>12. Marcus is dead.....</i>	<i>11,2</i>

Understanding a sentence

- *The bank president ate a dish of pasta salad with the fork.*

- *bank* = financial institution / a side of a river
- *dish* = eat dish / eat pasta
- *pasta salad* : dog food → food with dog meat?
- *with a fork* : withher friend. / with vegetable.
- *solution : state of the world*

Seven problem characteristics

1. *Decomposable Problem*

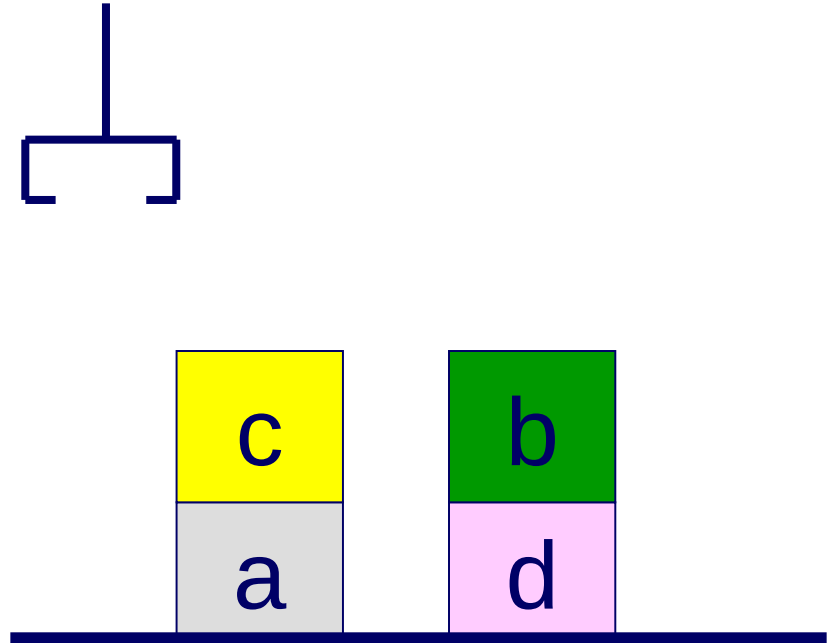
- *Block world problem*

2. *Can solution steps be ignored or undone?*

- *Ignorable* : theorem proving
 - solution steps can be ignored
- *Recoverable* : 8 puzzle
 - solution steps can be undone (backtracking)
- *Irrecoverable* : chess
 - solution steps can not be undone

A blocks world

- *on(c,a).*
- *on(b,d).*
- *ontable(a).*
- *ontable(d).*
- *clear(b).*
- *clear(c).*
- *hand_empty.*



Seven problem characteristics

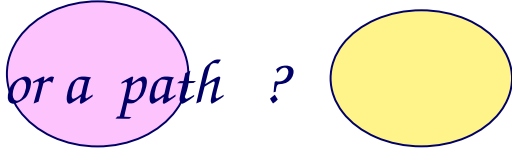
- 3. *Is the universe predictable?*

- 8-puzzle (yes)
- bridge (no) → but we can use probabilities of each possible outcomes
 - controlling robot arm → gear of the arm might stuck
 - helping the lawyer to decide how to defend his client against a murder charge.

- 4. *Is a good solution absolute or relative?*

- - formal inference methods
- - More than one solution?
- - traveling salesman problem

Seven problem characteristics

5. Is the *solution* a state or a path ? 
- water jug problem → *path / plan*

6. What is the role of knowledge?

knowledge for perfect program of chess

(need knowledge to constrain the search)

newspaper story understanding

(need knowledge to recognize a solution)

7. Does the task require *interaction with a person?* *solitary/ conversational*

Production system

1. *A set of rules.*
2. *Knowledge contains information for a particular task.*
3. *A control strategy.*
 - resolve conflict rule.
 - Breadth-first search
 - Depth-first search

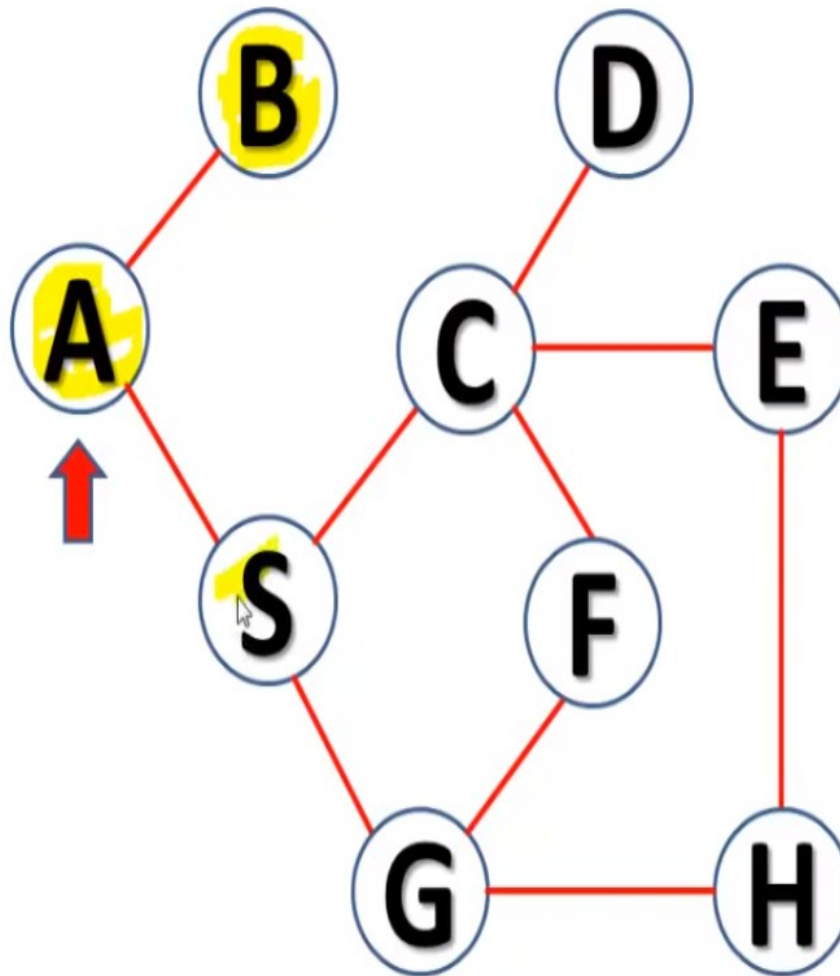
*Expert system shells : provide
environment for construct
knowledge based expert system.*

Breadth-first search

- *Algorithm BFS:*
 1. Create a variable called *NODE-LIST* and set it to the initial state.
 2. Until a goal state is found or *NODE-LIST* is empty do:
 - Remove the first element from *NODE-LIST* and call it *E*. If *NODE-LIST* was empty, quit.
 - For each way that each rule can match the state described in *E* do:
 - Apply the rule to generate a new state.
 - If the new state is a goal state, quit and return this state.
 - Otherwise, add the new state to the end of *NODE-LIST*.

```
BFS-B(G,s)
  for all v in V[G] do
    visited[v] := false
  end for
  Q := EmptyQueue
  visited[s] := true
  Enqueue(Q,s)
  while not Empty(Q) do
    u := Dequeue(Q)
    for all w in Adj[u] do
      if not visited[w] then
        visited[w] := true
        Enqueue(Q,w)
      end if
    end for
  end while
```

BREADTH FIRST SEARCH

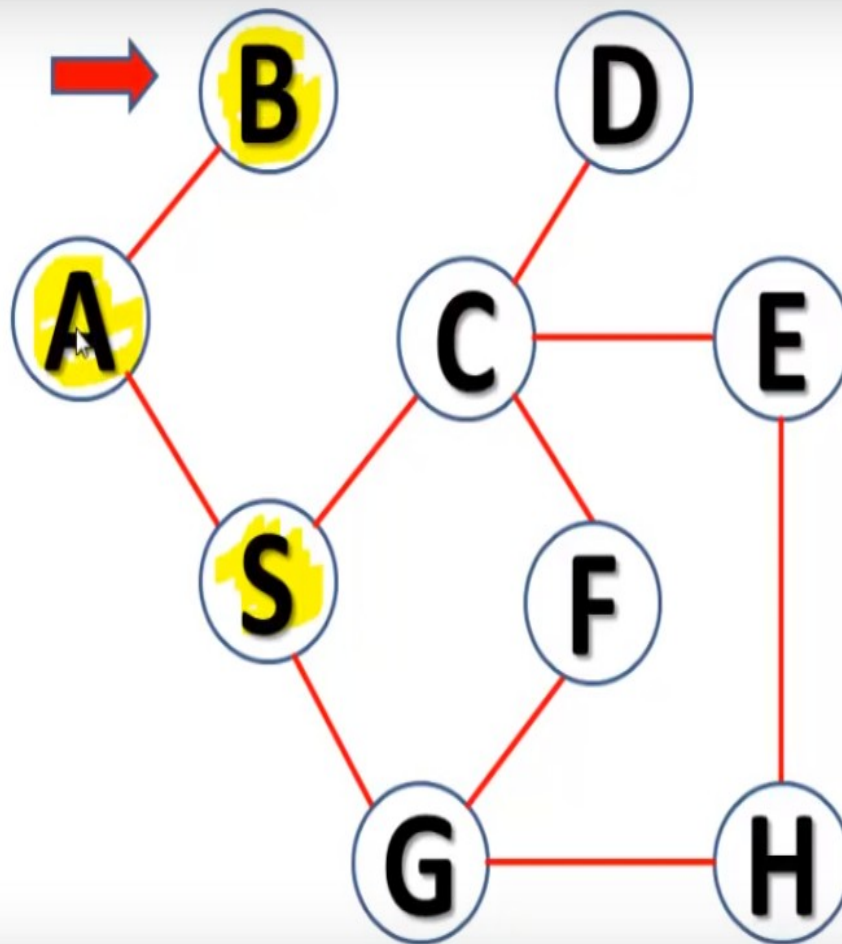


Queue Status

B
S

OUTPUT: **A B**

BREADTH FIRST SEARCH



Queue Status

S

Pause (k)

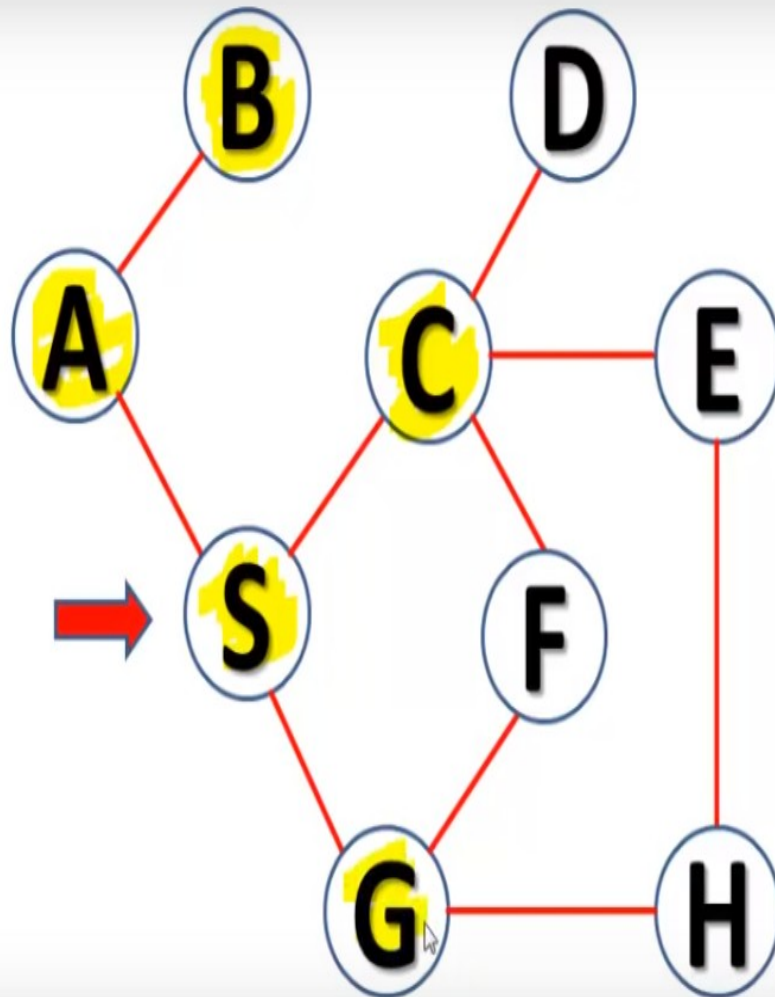


1:55 / 4:33

OUTPUT: A B S



BREADTH FIRST SEARCH



Queue Status

C
G

Pause (k)

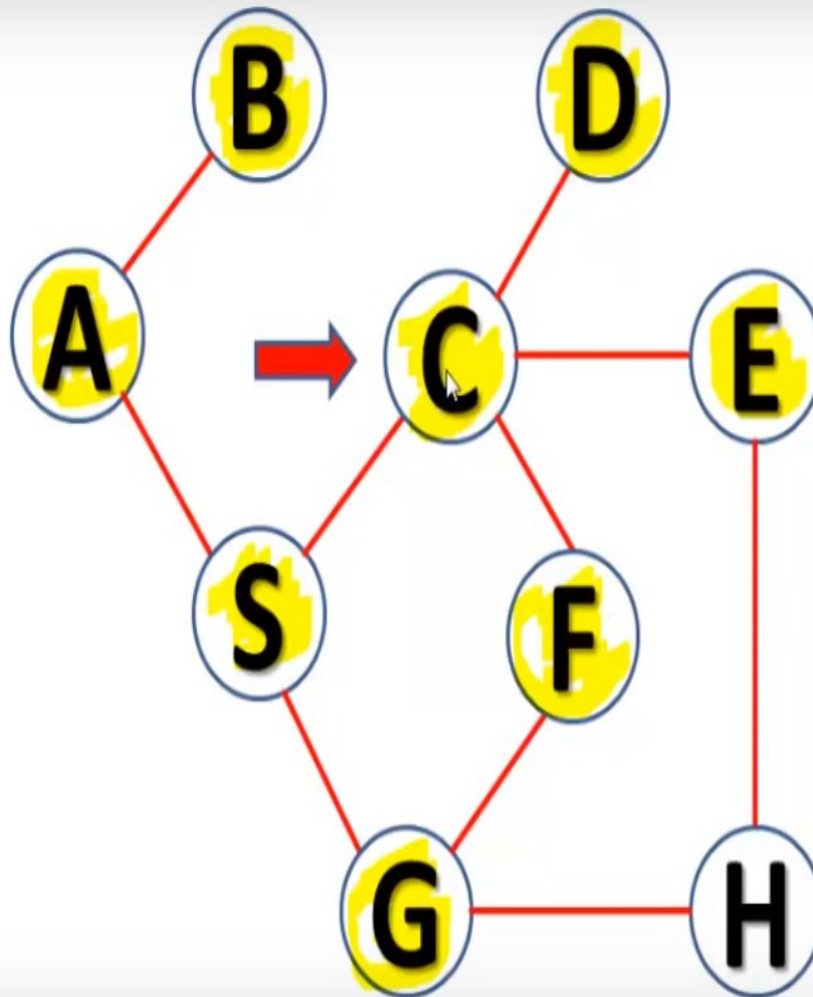


2:27 / 4:33

OUTPUT: A B S C G



BREADTH FIRST SEARCH



Queue Status

G
D
E
F

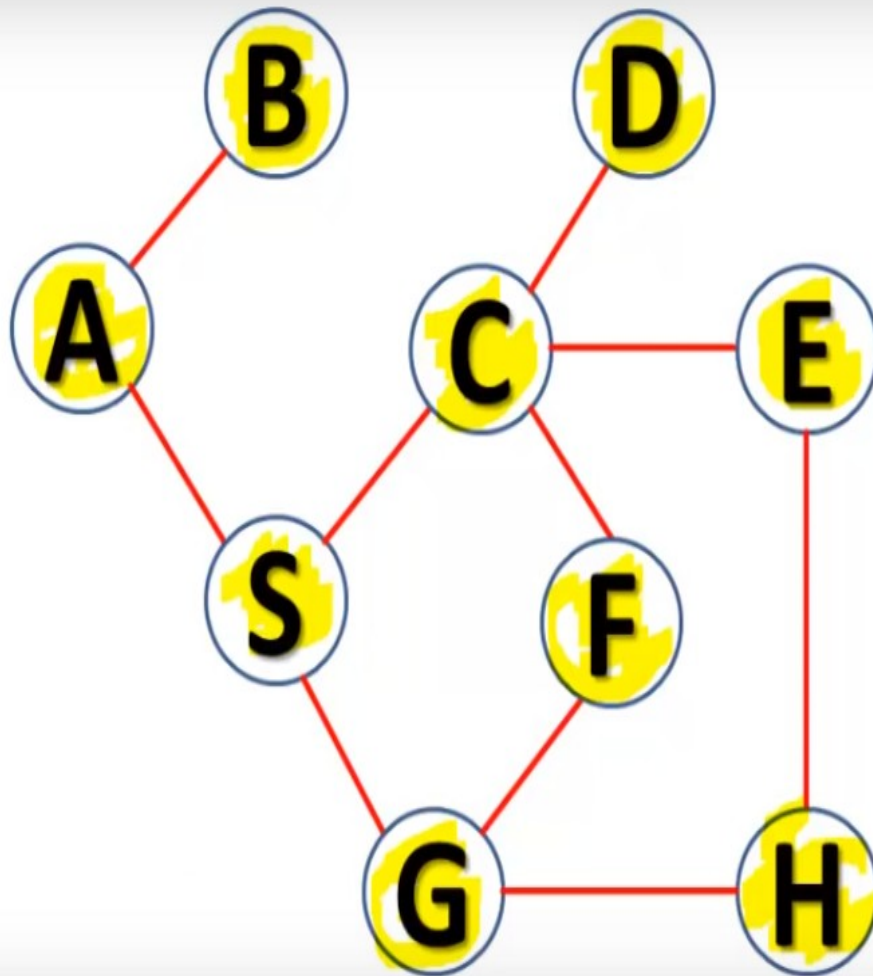
Play (k)

OUTPUT: A B S C G D E F

3:17 / 4:33



BREADTH FIRST SEARCH

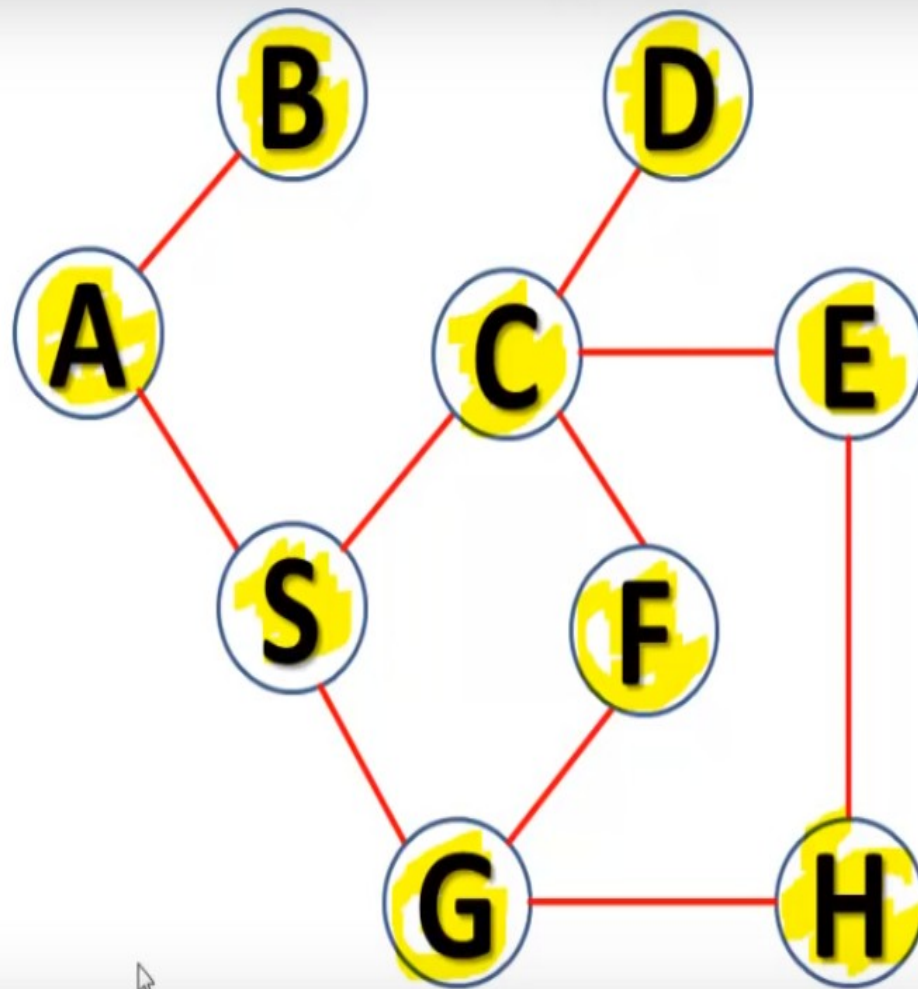


Queue Status

D
E
F
H

OUTPUT: A B S C G D E F H

BREADTH FIRST SEARCH



Queue Status



Queue Empty

Play (k)

4:25 / 4:33

OUTPUT: A B S C G D E F H

HD

Advantage BFS

1. *will not trapped exploring a blind alley*
2. *if there is a solution, BFS is guaranteed to find it.*
3. *if there are multiple solutions, a minimum solution will be found.*

Depth-first search

Algorithm DFS:

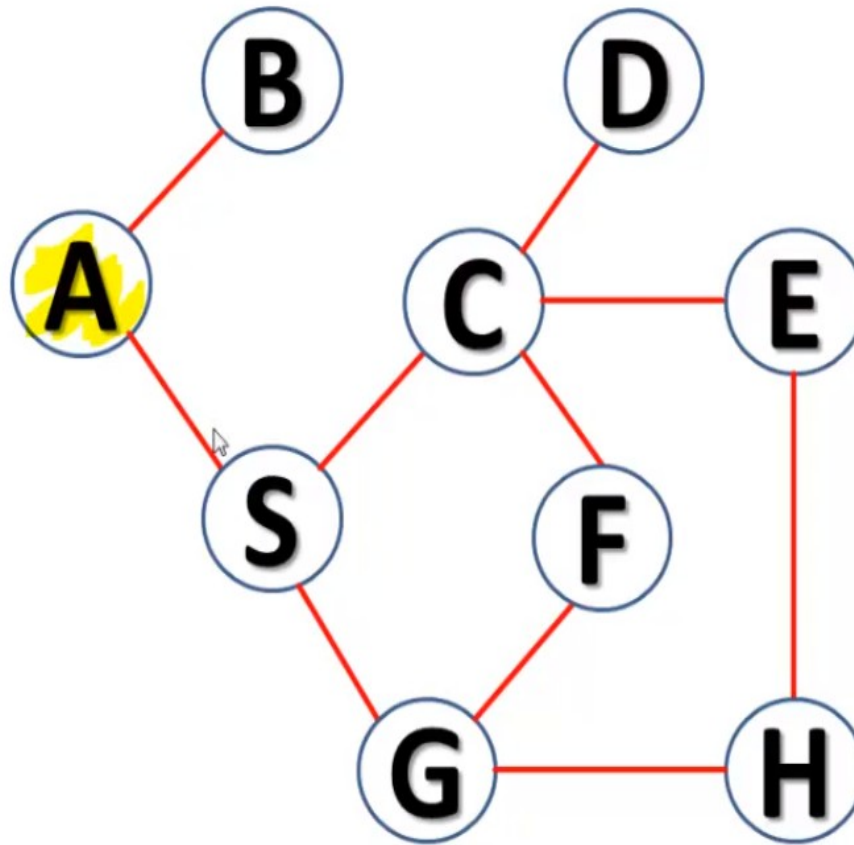
- 1. If the initial state is a goal state, quit and return success.*
- 2. Otherwise, do the following until success or failure is signaled:*
 - Generate a successor, E, of the initial state. If there are no more successors, signal failure.
 - Call Depth-First Search with E as the initial state.
 - If success is returned, signal success. Otherwise continue in this loop.

```

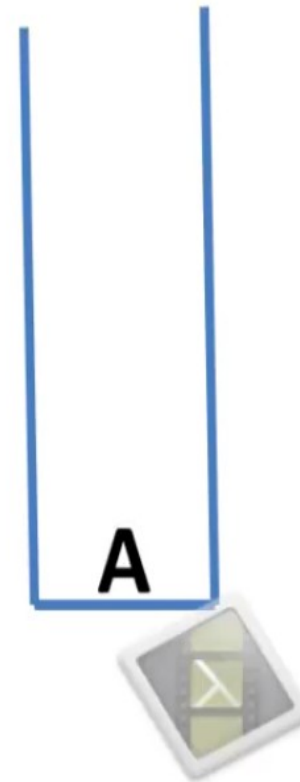
DFS-A(G,s)
  for all v in V[G] do
    visited[v] := false
  end for
  S := EmptyStack
  Push(S,s)
  while not Empty(S) do
    u := Pop(S)
    if not visited[u] then
      visited[u] := true
      for all w in Adj[u] do
        if not visited[w] then
          Push(S,w)
        end if
      end for
    end if
  end while

```

DEPTH FIRST SEARCH



Stack Status

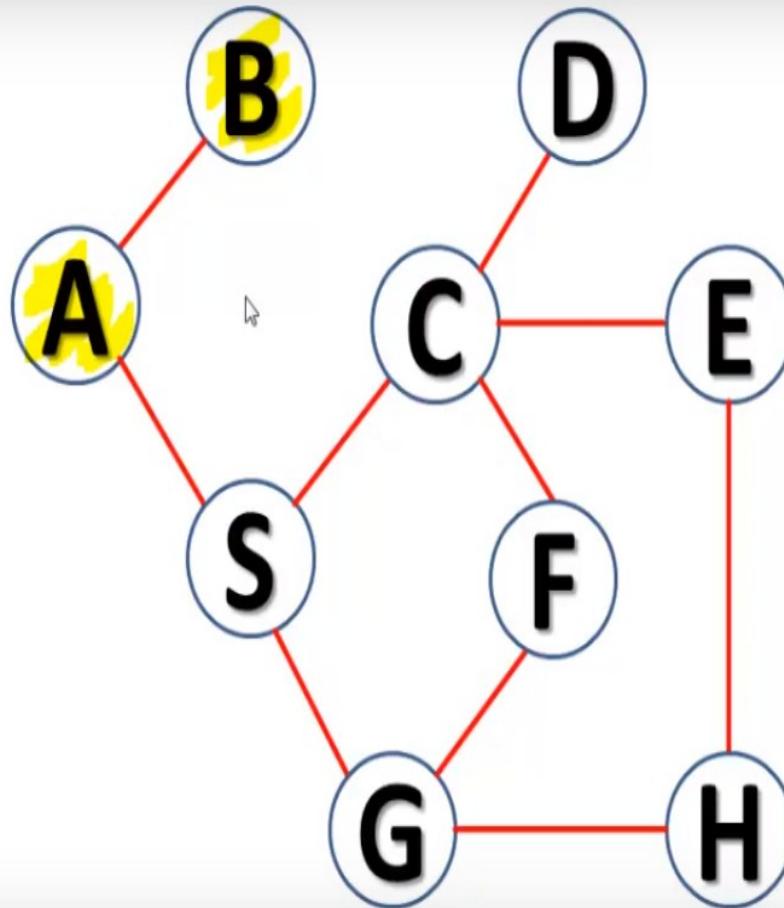


OUTPUT: **A**

DEPTH FIRST SEARCH



Stack Status



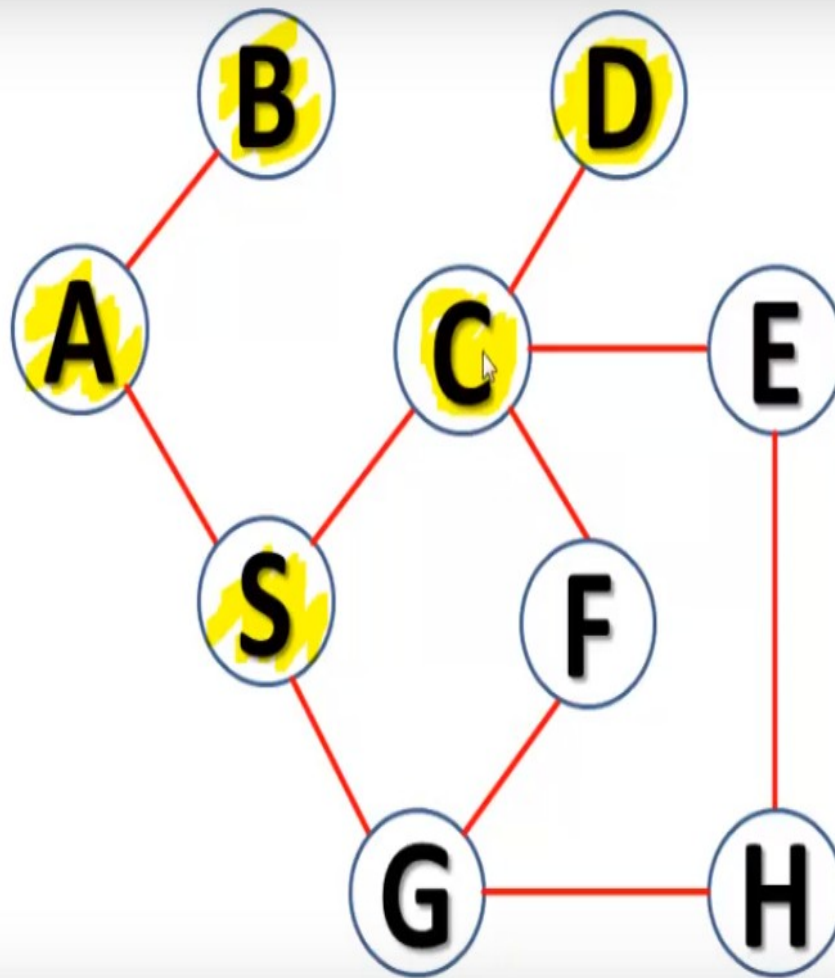
Play (k)

OUTPUT: **A B**

1:14 / 3:46



DEPTH FIRST SEARCH



Stack Status

D
C
S
A



OUTPUT: **A B S C**



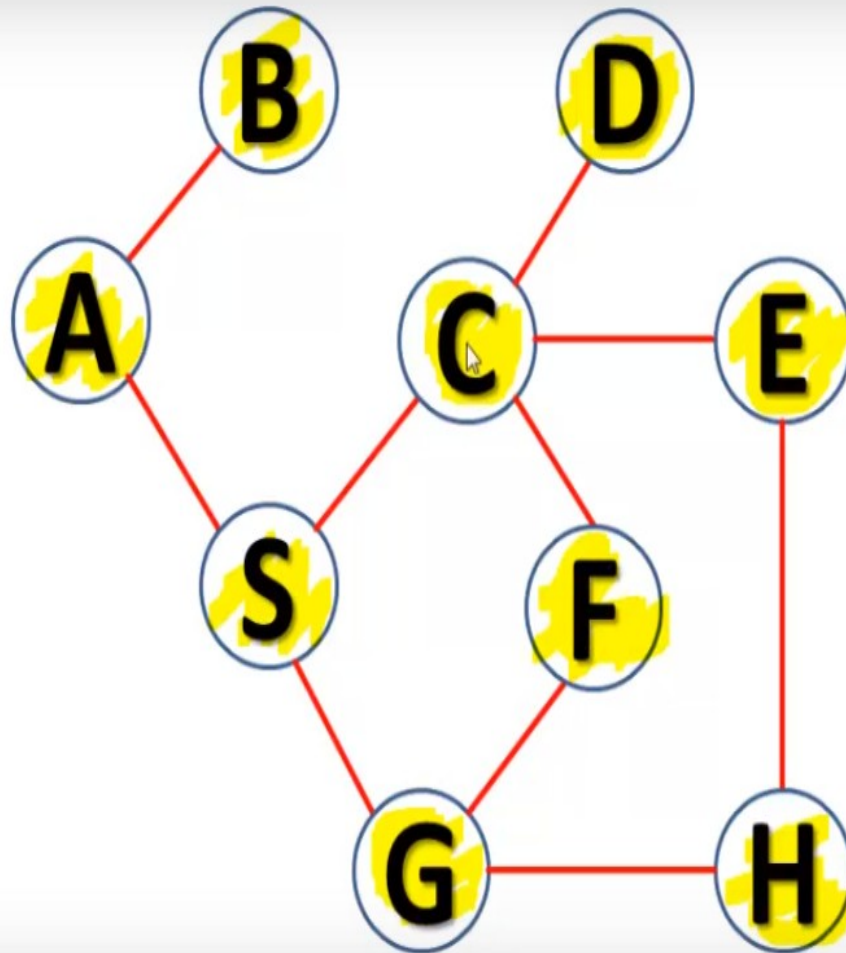
2:06 / 3:46



DEPTH FIRST SEARCH



Stack Status



F
G
H
E
C
S
A

Play (k)



2:59 / 3:46

OUTPUT: **A B S C D E H G F**



Advantage DFS

1. *require less memory*
2. *may find a solution without examining much of the search space.*

Heuristic Search

- *Heuriskein* → to discover (Greek word)
- *Heuristic* is a technique that improves the efficiency of the search process.(tour guide)
 - - It is often useful to introduce heuristics based on relatively unstructured knowledge.
 - - can not use Mathematical analysis.
- *Heuristic function* : is the function that maps from problem state descriptions to measures of desirability, usually represent as number. → guide the most profitable direction

To solve a problem

1. Define the problem precisely. Specify the problem space, and the starting and goal state (s).
2. Analyze the problem to determine where it falls with respect to **seven important issues**.
3. Identify and represent the knowledge required by the task.
4. Choose one or more techniques for problem solving , and apply those techniques to the problem.

References

Introduction to Artificial Intelligence
by Rusell Norving