

Assignment-3

Part-A

Pseudocode

SmartPriorityQueue(Generic[K]):

 constructor(capacity: int, comparison_function: Callable[[K, K], bool]):

 heap_array: List[K] = []

 size = 0

 is_min_heap = True

 comparator = comparison_function

insert(element: K):

 heapq.heappush(heap_array, element)

 size += 1

top() -> K:

 if is_empty():

 raise ValueError

 return heap_array[0]

toggle():

 is_min_heap = not is_min_heap

 if is_min_heap:

 comparator = lambda a, b: a < b

 else:

 comparator = lambda a, b: a > b

 heapq.heapify(heap_array)

remove_top() -> K:

 if is_empty():

 raise ValueError

 return heapq.heappop(heap_array)

remove(element: K) -> K:

 if is_empty():

```
        raise ValueError
    heap_array.remove(element)
    heapq.heapify(heap_array)
    return element
```

```
replace_key( old_key: K, new_key: K) -> K:
    if is_empty():
        raise ValueError
    remove(old_key)
    insert(new_key)
    return old_key
```

```
replace_value( old_value: K, new_value: K) -> K:
    if is_empty():
        raise ValueError
    index = heap_array.index(old_value)
    heap_array[index] = new_value
    heapq.heapify(heap_array)
    return old_value
```

```
status() -> str:
    return "Min" if is_min_heap else "Max"
```

```
is_empty() -> bool:
    return size == 0
```

```
size() -> int:
    return size
```

```
to_array() -> List[K]:
    return heap_array
```

Part - B

Tight Big-O time complexities

- insert: $O(\log n)$
- top: $O(1)$
- toggle: $O(n)$
- remove_top: $O(\log n)$
- remove: $O(n)$
- replace_key: $O(n)$
- replace_value: $O(n)$
- status, is_empty, size: $O(1)$