

3-4-5 Natural Partitioning

Importing necessary libraries

```
In [42]: import numpy as np
import pandas as pd
```

Taking Input

```
In [43]: X = [32, 38, 48, 91, 46, 37, 22, 69, 78, 82, 33, 49, 55, 66, 84, 86, 67, 80, 79, 44]
```

```
In [44]: # min = int(input("Enter minimum value: "))
# max = int(input("Enter maximum value: "))

min = 0
max = 100
```

Defining the partitioning algorithm

```
In [45]: def partitioning(nums,minimum,maximum):

    # Finding the most significant digit
    nums = sorted(nums)
    print()
    print("Numbers = {}".format(nums))
    print("Number of distinct values = {}".format(maximum - minimum))

    most_sig_digit = int(str(maximum - minimum)[0])
    print("Most Significant Digit = {}".format(most_sig_digit))

    # Finding the number of partitions
    num_of_partitions = 0
    if most_sig_digit in [3, 6, 7, 9]:
        num_of_partitions = 3
    elif most_sig_digit in [2, 4, 8]:
        num_of_partitions = 4
    else:
        num_of_partitions = 5
    print("Number of partitions decided : ", num_of_partitions)

    # Initializing the partitions dictionary and intervals list
    temp = (maximum-minimum) / num_of_partitions
    partitions = {}
    intervals = []

    # Adding partitions and intervals
    for i in range(0,num_of_partitions):
        interval_min = round(minimum + (i*temp))
        interval_max = round(minimum + (i+1)*temp)
        intervals.append((i+1,interval_min,interval_max))

    partitions[i+1] = []

    print("Partitions = {}".format(partitions))
    print("Intervals = {}".format(intervals))

    for num in nums:
        for interval in intervals:
            if num > interval[1] and num < interval[2]:
                partitions[interval[0]].append(num)

    print("Partitions = {}".format(partitions))
    print()
    return partitions,intervals
```

Partitioning for 2 Levels

```
In [46]: print("----- LEVEL 1 -----")
partitions,intervals = partitioning(X,min,max)

print("----- LEVEL 2 -----")
final_partitions = {}
i = 1
for interval in intervals:
    partitions,intervals = partitioning(newData[interval[0]],interval[1],interval[2])
    for key in partitions.keys():
        final_partitions[i] = partitions[key]
    i += 1

----- LEVEL 1 -----

Numbers = [22, 32, 33, 37, 38, 44, 46, 48, 49, 55, 66, 67, 69, 78, 79, 80, 82, 84, 86, 91]
Number of distinct values = 100
Most Significant Digit = 1
Number of partitions decided : 5
Partitions = {1: [], 2: [], 3: [], 4: [], 5: []}
Intervals = [(1, 0, 20), (2, 20, 40), (3, 40, 60), (4, 60, 80), (5, 80, 100)]
Partitions = {1: [], 2: [22, 32, 33, 37, 38], 3: [44, 46, 48, 49, 55], 4: [66, 67, 69, 78, 79], 5: [82, 84, 86, 91]}

----- LEVEL 2 -----

Numbers = []
Number of distinct values = 20
Most Significant Digit = 2
Number of partitions decided : 4
Partitions = {1: [], 2: [], 3: [], 4: []}
Intervals = [(1, 0, 5), (2, 5, 10), (3, 10, 15), (4, 15, 20)]
Partitions = {1: [], 2: [], 3: [], 4: []}

Numbers = [22, 32, 33, 37, 38]
Number of distinct values = 20
Most Significant Digit = 2
Number of partitions decided : 4
Partitions = {1: [], 2: [], 3: [], 4: []}
Intervals = [(1, 20, 25), (2, 25, 30), (3, 30, 35), (4, 35, 40)]
Partitions = {1: [22], 2: [], 3: [32, 33], 4: [37, 38]}

Numbers = [44, 46, 48, 49, 55]
Number of distinct values = 20
Most Significant Digit = 2
Number of partitions decided : 4
Partitions = {1: [], 2: [], 3: [], 4: []}
Intervals = [(1, 40, 45), (2, 45, 50), (3, 50, 55), (4, 55, 60)]
Partitions = {1: [44], 2: [46, 48, 49], 3: [], 4: []}

Numbers = [66, 67, 69, 78, 79]
Number of distinct values = 20
Most Significant Digit = 2
Number of partitions decided : 4
Partitions = {1: [], 2: [], 3: [], 4: []}
Intervals = [(1, 60, 65), (2, 65, 70), (3, 70, 75), (4, 75, 80)]
Partitions = {1: [], 2: [66, 67, 69], 3: [], 4: [78, 79]}

Numbers = [82, 84, 86, 91]
Number of distinct values = 20
Most Significant Digit = 2
Number of partitions decided : 4
Partitions = {1: [], 2: [], 3: [], 4: []}
Intervals = [(1, 80, 85), (2, 85, 90), (3, 90, 95), (4, 95, 100)]
Partitions = {1: [82, 84], 2: [86], 3: [91], 4: []}
```

Final Answer

```
In [47]: print("----- FINAL PARTITIONS -----")
final_partitions
```

```
Out[47]: {1: [],
2: [],
3: [],
4: [],
5: [22],
6: [],
7: [32, 33],
8: [37, 38],
9: [44],
10: [46, 48, 49],
11: [],
12: [],
13: [],
14: [66, 67, 69],
15: [],
16: [78, 79],
17: [82, 84],
18: [86],
19: [91],
20: []}
```

Replacing original values with intervals

```
In [52]: X = sorted(X)
new_X = []
for key in final_partitions.keys():
    for i in range(len(final_partitions[key])):
        new_X.append(key)
```

```
In [53]: new_X
```

```
Out[53]: [5, 7, 7, 8, 8, 9, 10, 10, 10, 14, 14, 14, 16, 16, 17, 17, 18, 19]
```