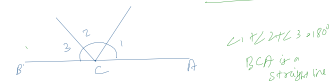
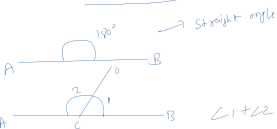


Lines and Angles



Theorem 6.1 : If two lines intersect each other, then the vertically opposite angles are equal.

Given: PO and BC are two lines intersecting each other at O.

To prove: $\angle AOB = \angle COD$

Proof: AOB is a straight line
 $\angle AOB + \angle BOD = 180^\circ$ (Linear pair)

BOC is a straight line
 $\angle BOD + \angle COD = 180^\circ$ (Linear pair)

From (i) and (ii)
 $\angle AOB + \angle BOD = \angle BOD + \angle COD$
 $\angle AOB = \angle COD$

Similarly we can prove $\angle BOD = \angle AOC$



Given: $\angle AOC = \angle AOE = 70^\circ$
 $\angle BOD = 40^\circ$

To find: $\angle BOE$ & reflex $\angle COE$

$\angle AOC = \angle BOD$ (Vertically opposite angles)
 $\angle AOC = 40^\circ$ — (1)

$\angle AOC + \angle BOE = 70^\circ$ (Given)

$40^\circ + \angle BOE = 70^\circ$ (From (1))
 $\angle BOE = 70^\circ - 40^\circ$
 $= 30^\circ$

AB is a straight line.

$\therefore \angle AOC + \angle COE + \angle BOE = 180^\circ$

$40^\circ + \angle COE + 30^\circ = 180^\circ$

$\angle COE = 180^\circ - 70^\circ$
 $= 110^\circ$

Reflex $\angle COE = 360^\circ - \angle COE$
 $= 360^\circ - 110^\circ$
 $= 250^\circ$



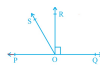
Given: $x + y = w + z$

To prove: AOB is a line

Proof: $x + y + w + z = 360^\circ$ (Complete angle)
 $(x + y) + (w + z) = 360^\circ$ (Given)
 $= 2(x + y) = 360^\circ$
 $\therefore x + y = 180^\circ$

but x & y are also linear pair.
 \therefore AOB is a line.

5. In Fig. 6.17, POQ is a line. Ray OR is perpendicular to line PQ. OS is another ray lying between rays OP and OR. Prove that $\angle ROS = \frac{1}{2}(\angle QOS - \angle POS)$.



To prove:

Given: POQ is a line,
 $\angle ROQ = 90^\circ$

$\angle ROS = \frac{1}{2}(\angle QOS - \angle POS)$

Proof:

$\angle QOS = \angle ROQ + \angle ROS$

$\angle QOS = 90^\circ + \angle ROS$

$\angle QOS - 90^\circ = \angle ROS$ — (i)

Add (i) & (ii)
 $2\angle ROS = \angle QOS - 90^\circ$
 $+ 90^\circ - \angle POS$

$\angle ROS = \frac{1}{2}(\angle QOS - \angle POS)$

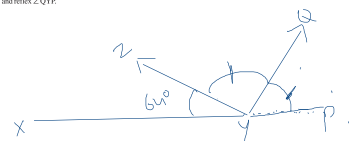
From the figure

$\angle POR = \angle ROS + \angle POS$

$90^\circ = \angle ROS + \angle POS$

$90^\circ - \angle POS = \angle ROS$ (ii)

6. It is given that $\angle XYZ = 64^\circ$ and XY is produced to point P. Draw a figure from the given information. Find $\angle YQP$ and $\angle YXQ$ and reflex $\angle YQP$.



XYZ is a str

$64^\circ + \angle ZYQ + \angle QYP = 180^\circ$
 $\angle ZYQ + \angle QYP = 116^\circ$

$\angle 1 = \angle 2$ (Corresponding angles)
 $\angle 3 = \angle 4$ (Corresponding angles)
 $\angle 5 = \angle 6$ (V.A.)
 $\angle 7 = \angle 8$ (V.A.)
 $\angle 3 = \angle 5$ (V.O.A.)
 $\angle 2 = \angle 7$ (V.O.A.)
 $\angle 4 = \angle 6$ (V.O.A.)
 $\angle 2 = \angle 7$ (Alternate interior angles)
 $\angle 3 = \angle 5$ (V.O.A.)
 $\angle 4 = \angle 6$ (V.O.A.)
 $\angle 2 = \angle 7$ (Alternate interior angles)

In Fig. 6.28, find the values of x and y and then show that $AB \parallel CD$.



$x + 50 = 180$ (Linear pair)
 $x = 130$
 $y + 110 = 180$ (Linear pair)
 $y = 70$
 $\therefore AB \parallel CD$

In Fig. 6.29, if $AB \parallel CD$, $CD \parallel EF$ and $\angle c = 37^\circ$, find $\angle a$.



$\angle a = 126$
 $\angle b = 126$

Given: $AB \parallel CD$, $CD \parallel EF$

To find: x
 let y and z be \angle at B & F

$\angle y + z = 180$ (Linear pair)
 $\angle z + \angle c = 180$ (Linear pair)
 $\angle c = 37$
 $\angle z = 143$
 $\angle y = 37$

In Fig. 6.30, if $AB \parallel CD$, $EF \perp CD$ and $\angle QRS = 120^\circ$, find $\angle AQR$, $\angle QRP$ and $\angle QSR$.



Given: $AB \parallel CD$, $EF \perp CD$
 $\angle QRS = 120^\circ$
 To find: $\angle AQR$, $\angle QRP$, $\angle QSR$

To find: $\angle AQR$
 Const: $RM \parallel ST$

$RM \parallel ST$ (By construction)
 $\angle QRS + \angle RST = 180$ (Sum of interior angles)
 $\angle QRS = 120$
 $\angle RST = 60$
 $\angle QSR = 180 - 120 = 60$
 $\angle AQR = 60$



$\angle APQ = x$ (Alternate interior angles)
 $\angle PRQ = y$ (Exterior angle property)
 $127 = x + y$
 $y = 127 - 50 = 77$

In Fig. 6.31, PQ and RS are two mirrors placed parallel to each other. An incident ray AB strikes the mirror PQ at B, the reflecting ray moves along the path BC, and strikes the mirror RS at C, and again reflects back along CD. Prove that $AB \parallel CD$.



Given: $PQ \parallel RS$
 To prove: $AB \parallel CD$
 Const: Construct normal BM on PQ and normal CN on RS.
 let $\angle BAM = x$
 $\angle 1 = \angle 2$ (Law of reflection, so BM is angle bisector)
 $\angle 3 = \angle 4$ (Law of reflection, so CN is angle bisector)
 $PQ \parallel RS$ (Given)
 $BM \perp PQ$, $CN \perp RS$
 $\therefore BM \parallel CN$
 $\angle BAC = \angle BCD$ (Alternate interior angles)
 $\therefore AB \parallel CD$