

Question 1

Correct

Marked out of 16

(Secant Method). All numerical answers should be rounded to 7-digit floating-point numbers. Given a real number z , the symbol \tilde{z} denotes the result of rounding of z to a 7-digit floating-point number.

(i) Apply the Secant method to find an approximation p_N of the solution of the equation

$$\frac{x - \sin(x)}{1 - \cos x} = 0.69$$

in $[\pi/2, \pi]$ satisfying

$$\text{RE}(\tilde{p}_N \approx \tilde{p}_{N-1}) < 10^{-6}$$

by taking $p_0 = 2.6$ and $p_1 = 2.8$ as the initial approximations.

(ii) Show your work by filling the following standard output table for the Secant method (if a particular row is not necessary, please type an asterisk * in each input field of that row):

n	p_{n-2}	p_{n-1}	p_n	$\text{RE}(\tilde{p}_n \approx \tilde{p}_{n-1})$
2	2.6	2.8	2.009835	0.3931492
	✓	✓	✓	✓
3	2.8	2.009835	1.8736	0.07271296
	✓	✓	✓	✓
4	2.009835	1.8736	1.837149	0.01984107
	✓	✓	✓	✓
5	1.8736	1.837149	1.835829	0.0007190212
	✓	✓	✓	✓
6	1.837149	1.835829	1.835819	5.44716e-06
	✓	✓	✓	✓
7	1.835829	1.835819	1.835819	0
	✓	✓	✓	✓
8	*	*	*	*
	✓	✓	✓	✓
9	*	*	*	*
	✓	✓	✓	✓
10	*	*	*	*
	✓	✓	✓	✓

(ii) According to your results in (i) and (ii),

$$p_N \doteq 1.835819 \quad \checkmark \quad .$$

Check