

## Exercise 1a

**Variable: length**

Moments			
N	210	Sum Weights	210
Mean	5.62853333	Sum Observations	1181.992
Std Deviation	0.44306348	Variance	0.19630525
Skewness	0.52548156	Kurtosis	-0.7856445
Uncorrected SS	6693.90917	Corrected SS	41.0277963
Coeff Variation	7.87173943	Std Error Mean	0.03057428

Basic Statistical Measures			
Location		Variability	
Mean	5.628533	Std Deviation	0.44306
Median	5.523500	Variance	0.19631
Mode	5.236000	Range	1.77600
		Interquartile Range	0.71800

**Note: The mode displayed is the smallest of 2 modes with a count of 3.**

Seed lengths center around 5.6 (mean = 5.629; median = 5.524), with spread (SD = 0.443; CV ≈ 7.9%). The distribution shows a slight right skew (skewness = +0.525; mean > median) and kurtosis = -0.786. The middle 50% of lengths lie between 5.26 and 5.98 (IQR = 0.718), and overall values range from about 4.90 to 6.68 (range = 1.776).

## Exercise 1b

## Basic descriptives for LENGTH by VARIETY

**Variable: length  
variety = Canadian**

<b>Moments</b>			
<b>N</b>	70	<b>Sum Weights</b>	70
<b>Mean</b>	5.22951429	<b>Sum Observations</b>	366.066
<b>Std Deviation</b>	0.1380152	<b>Variance</b>	0.0190482
<b>Skewness</b>	0.05119272	<b>Kurtosis</b>	-0.4784569
<b>Uncorrected SS</b>	1915.6617	<b>Corrected SS</b>	1.31432549
<b>Coeff Variation</b>	2.63915906	<b>Std Error Mean</b>	0.01649597

<b>Basic Statistical Measures</b>			
<b>Location</b>		<b>Variability</b>	
<b>Mean</b>	5.229514	<b>Std Deviation</b>	0.13802
<b>Median</b>	5.224000	<b>Variance</b>	0.01905
<b>Mode</b>	5.236000	<b>Range</b>	0.64200
		<b>Interquartile Range</b>	0.18900

## Basic descriptives for LENGTH by VARIETY

**Variable: length**  
**variety = Kama**

<b>Moments</b>			
<b>N</b>	70	<b>Sum Weights</b>	70
<b>Mean</b>	5.50805714	<b>Sum Observations</b>	385.564
<b>Std Deviation</b>	0.23150803	<b>Variance</b>	0.05359597
<b>Skewness</b>	-0.3473746	<b>Kurtosis</b>	-0.0908666
<b>Uncorrected SS</b>	2127.40667	<b>Corrected SS</b>	3.69812177
<b>Coeff Variation</b>	4.20307966	<b>Std Error Mean</b>	0.0276705

<b>Basic Statistical Measures</b>			
<b>Location</b>		<b>Variability</b>	
<b>Mean</b>	5.508057	<b>Std Deviation</b>	0.23151
<b>Median</b>	5.534000	<b>Variance</b>	0.05360
<b>Mode</b>	5.395000	<b>Range</b>	1.15100
		<b>Interquartile Range</b>	0.29400

## Basic descriptives for LENGTH by VARIETY

**Variable: length  
variety = Rosa**

Moments			
N	70	Sum Weights	70
Mean	6.14802857	Sum Observations	430.362
Std Deviation	0.26819115	Variance	0.07192649
Skewness	-0.2537146	Kurtosis	0.26275797
Uncorrected SS	2650.8408	Corrected SS	4.96292794
Coeff Variation	4.36223002	Std Error Mean	0.03205497

Basic Statistical Measures			
Location		Variability	
Mean	6.148029	Std Deviation	0.26819
Median	6.148500	Variance	0.07193
Mode	5.979000	Range	1.31200
		Interquartile Range	0.33600

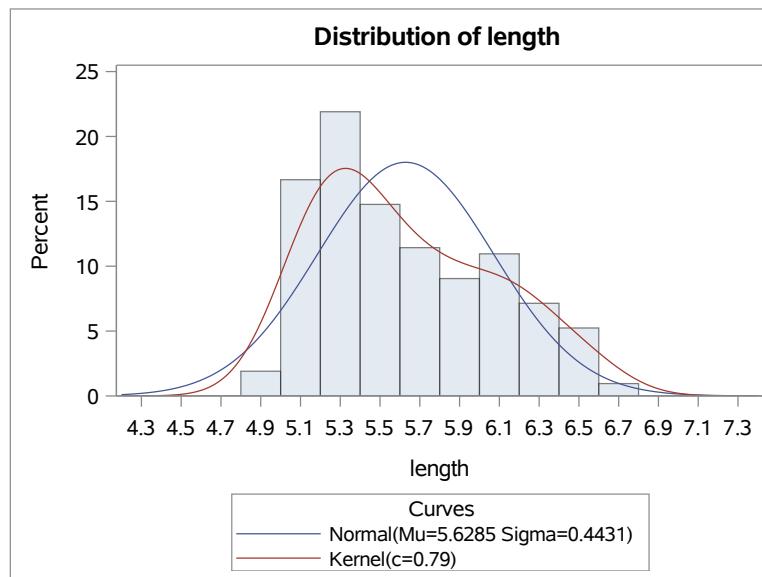
**Note: The mode displayed is the smallest of 3 modes with a count of 2.**

Canadian seeds are the shortest (mean  $\approx$  5.23, median  $\approx$  5.224), with the smallest spread (SD  $\approx$  0.138, IQR  $\approx$  0.189, range  $\approx$  0.64) and no skew (skew  $\approx$  +0.05). Kama seeds are mid-length (mean  $\approx$  5.51, median  $\approx$  5.534) with some variability (SD  $\approx$  0.232, IQR  $\approx$  0.294, range  $\approx$  1.15) and a slight left skew (skew  $\approx$  -0.35). Rosa seeds are the longest and most variable (mean  $\approx$  6.15, median  $\approx$  6.149; SD  $\approx$  0.268, IQR  $\approx$  0.336, range  $\approx$  1.31) with a mild left skew (skew  $\approx$  -0.25). Canadian seeds have the smallest variation and Rosa seeds have the widest spread.

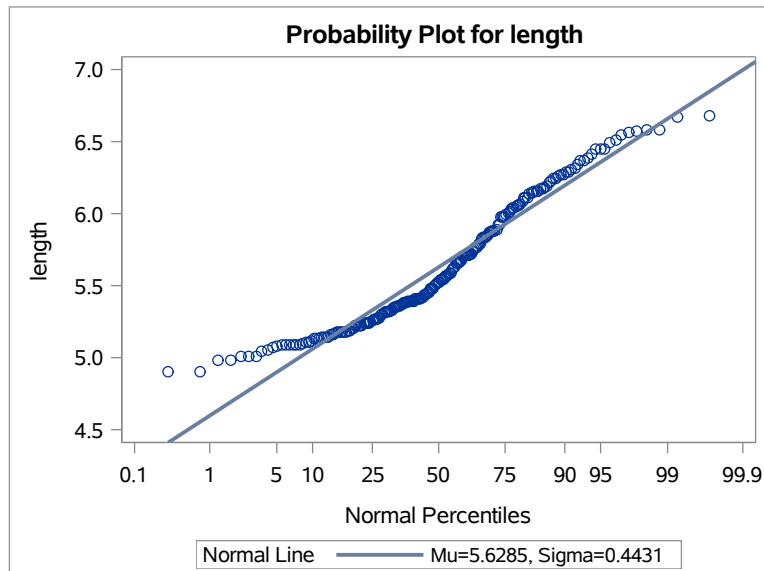
Exercise 2a

**Normality checks for LENGTH****Variable: length**

Tests for Normality				
Test	Statistic		p Value	
Shapiro-Wilk	W	0.943799	Pr < W	<0.0001
Kolmogorov-Smirnov	D	0.119154	Pr > D	<0.0100
Cramer-von Mises	W-Sq	0.655958	Pr > W-Sq	<0.0050
Anderson-Darling	A-Sq	3.891567	Pr > A-Sq	<0.0050

**Normality checks for LENGTH**

## Normality checks for LENGTH



Visually, the histogram of length is roughly bell-shaped and shows a right tail, and the Q-Q plot has a curvature away from the straight line. Quantitatively, every formal normality test strongly rejects normality: Shapiro-Wilk  $W = 0.9438$ ,  $p < 0.0001$ ; Kolmogorov-Smirnov  $D = 0.1192$ ,  $p < 0.01$ ; Cramér-von Mises  $W^2 = 0.6560$ ,  $p < 0.005$ ; Anderson-Darling  $A^2 = 3.8916$ ,  $p < 0.005$ . Therefore, the normality assumption is not reasonable for length.

Exercise 2b

**Normality checks for LENGTH by VARIETY**

**Variable: length**  
**variety = Canadian**

Tests for Normality				
Test	Statistic		p Value	
Shapiro-Wilk	W	0.990179	Pr < W	0.8631
Kolmogorov-Smirnov	D	0.066585	Pr > D	>0.1500
Cramer-von Mises	W-Sq	0.040448	Pr > W-Sq	>0.2500
Anderson-Darling	A-Sq	0.253382	Pr > A-Sq	>0.2500

**Normality checks for LENGTH by VARIETY**

**Variable: length  
variety = Kama**

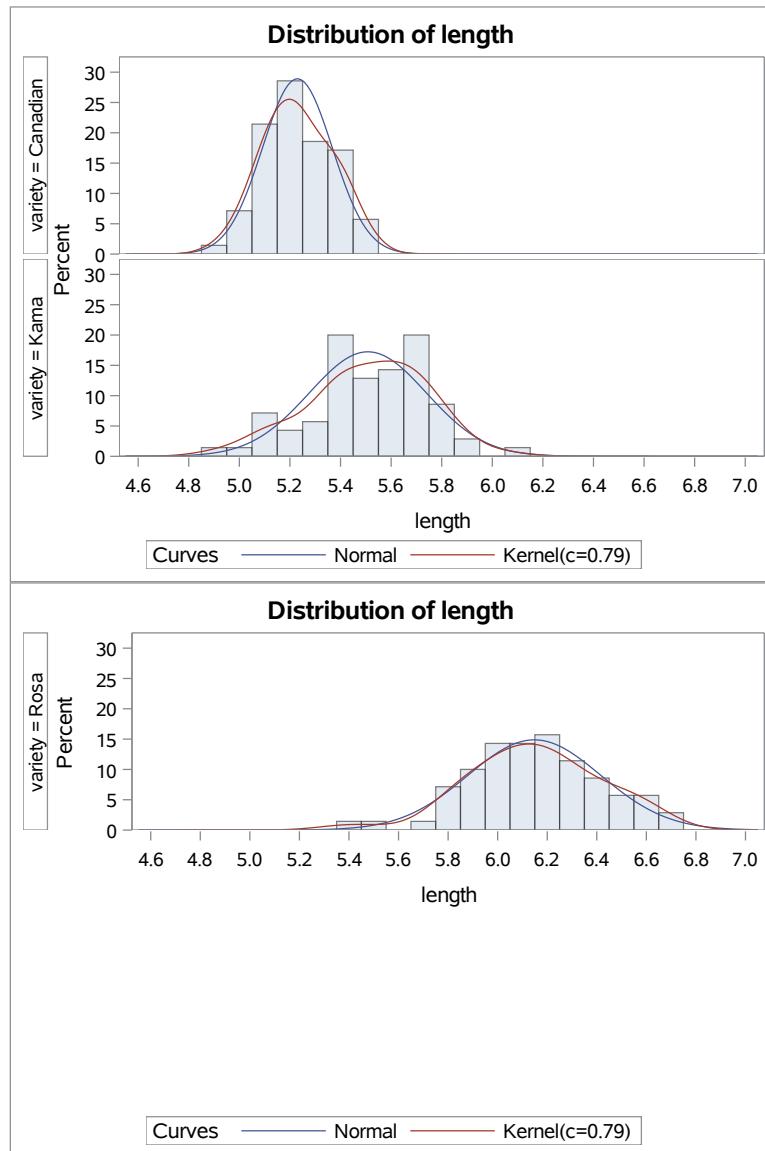
Tests for Normality				
Test	Statistic		p Value	
Shapiro-Wilk	W	0.984427	Pr < W	0.5367
Kolmogorov-Smirnov	D	0.067173	Pr > D	>0.1500
Cramer-von Mises	W-Sq	0.06146	Pr > W-Sq	>0.2500
Anderson-Darling	A-Sq	0.408654	Pr > A-Sq	>0.2500

**Normality checks for LENGTH by VARIETY**

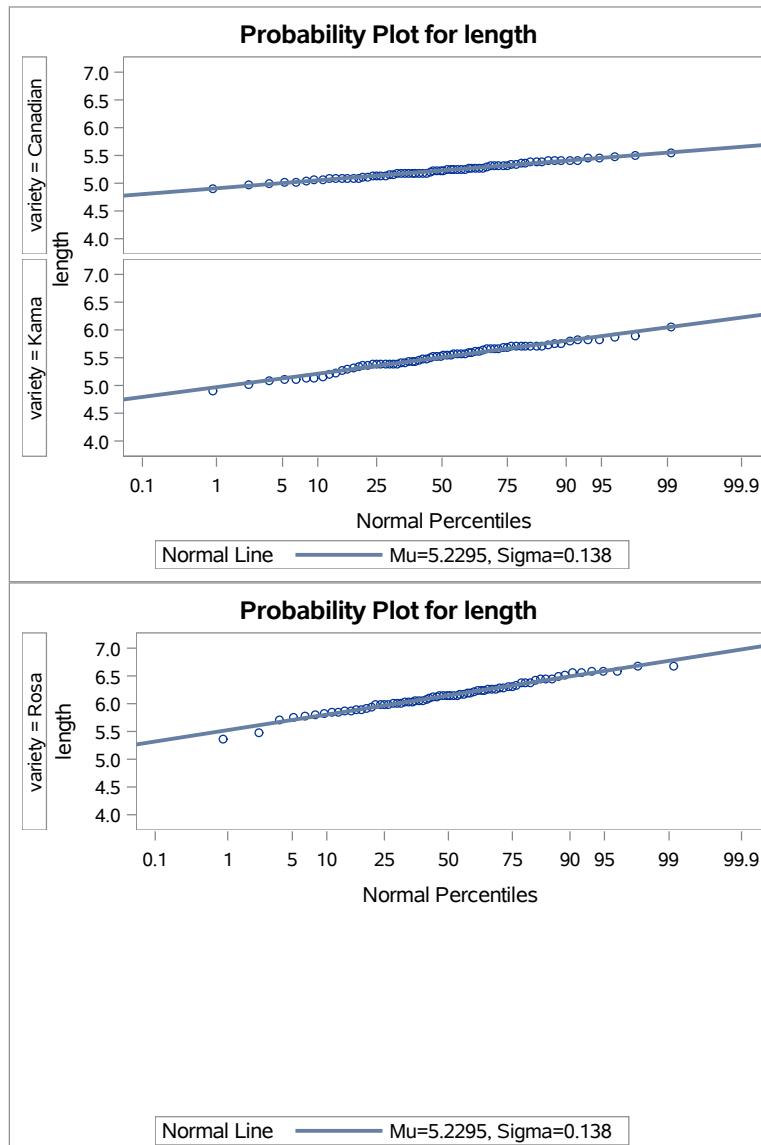
**Variable: length**  
**variety = Rosa**

Tests for Normality				
Test	Statistic		p Value	
Shapiro-Wilk	W	0.984142	Pr < W	0.5210
Kolmogorov-Smirnov	D	0.04876	Pr > D	>0.1500
Cramer-von Mises	W-Sq	0.01902	Pr > W-Sq	>0.2500
Anderson-Darling	A-Sq	0.20045	Pr > A-Sq	>0.2500

## Normality checks for LENGTH by VARIETY



### Normality checks for LENGTH by VARIETY



None of the three groups show a statistically significant deviation from normality. For Canadian seeds, all tests are nonsignificant—Shapiro-Wilk  $p=0.863$ , K-S  $p>0.15$ , CvM/AD  $p>0.25$  and a straight Q-Q line. Kama seeds have nonsignificant tests—Shapiro-Wilk  $p=0.537$ , K-S  $p>0.15$ , CvM/AD  $p>0.25$  and the histogram/Q-Q look bell-shaped. Rosa seeds also have nonsignificant tests—Shapiro-Wilk  $p=0.521$ , K-S  $p>0.15$ , CvM/AD  $p>0.25$  and a linear Q-Q plot. Each variety's seed lengths are consistent with normality.

Exercise 3a

## One-sample location test for LENGTH

**Variable: length**

Tests for Location: Mu0=5.5				
Test	Statistic		p Value	
Student's t	t	4.203969	Pr >  t	<.0001
Sign	M	3	Pr >=  M	0.7302
Signed Rank	S	2691.5	Pr >=  S	0.0021

Since the distribution is a bit symmetric, we will use Wilcoxon signed-rank. The p-value = 0.0021 which is << 0.05. Therefore, the tests are highly significant and the median value differs from the hypothesized value. Since the test statistic is positive, the median is slightly greater than 5.5.

Exercise 3b

### Test to check if Rosa is shorter than Kama

**Variable: length**

variety	Method	Mean	95% CL Mean		Std Dev	95% CL Std Dev	
Kama		5.5081	5.4529	5.5633	0.2315	0.1985	0.2778
Rosa		6.1480	6.0841	6.2120	0.2682	0.2300	0.3218
Diff (1-2)	Pooled	-0.6400	-0.7101	Infty	0.2505	0.2241	0.2840
Diff (1-2)	Satterthwaite	-0.6400	-0.7101	Infty			

Method	Variances	DF	t Value	Pr > t
Pooled	Equal	138	-15.11	1.0000
Satterthwaite	Unequal	135.12	-15.11	1.0000

Equality of Variances				
Method	Num DF	Den DF	F Value	Pr > F
Folded F	69	69	1.34	0.2243

The lengths are roughly normal within each variety. The two-sample t-test shows Rosa seeds are longer on average: Rosa=6.15 and Kama=5.51. The test gives  $t = -15.11$  with a one-sided p-value of 1.000. Therefore, we reject the claim and conclude Rosa seeds are longer than Kama seeds.

Exercise 4a

## Correlation analysis for the area, compactness, and length variables for all of the data

3 Variables:	area	compactness	length
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Simple Statistics						
Variable	N	Mean	Std Dev	Median	Minimum	Maximum
area	210	14.84752	2.90970	14.35500	10.59000	21.18000
compactness	210	0.87100	0.02363	0.87345	0.80810	0.91830
length	210	5.62853	0.44306	5.52350	4.89900	6.67500

Pearson Correlation Coefficients, N = 210 Prob >  r  under H0: Rho=0			
	area	compactness	length
area	1.00000	0.60829 <.0001	0.94999 <.0001
compactness	0.60829 <.0001	1.00000	0.36792 <.0001
length	0.94999 <.0001	0.36792 <.0001	1.00000

Spearman Correlation Coefficients, N = 210 Prob >  r  under H0: Rho=0			
	area	compactness	length
area	1.00000	0.63850 <.0001	0.93092 <.0001
compactness	0.63850 <.0001	1.00000	0.37808 <.0001
length	0.93092 <.0001	0.37808 <.0001	1.00000

Area and length are perfectly correlated (Pearson  $r=0.95$ , Spearman  $r\approx 0.93$ ;  $p<.0001$ ), longer seeds have larger area. Area and compactness show a moderate positive link ( $r\approx 0.61$ ), and length and compactness have a weak positive link ( $r\approx 0.37$ ). As seed length goes up, area goes up a lot, and compactness tends to increase a bit

Exercise 4b

## Correlation analysis by variety

variety=Canadian

<b>3 Variables:</b>	area	compactness	length
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Simple Statistics						
Variable	N	Mean	Std Dev	Median	Minimum	Maximum
<b>area</b>	70	11.87386	0.72300	11.83500	10.59000	13.37000
<b>compactness</b>	70	0.84941	0.02176	0.84935	0.80810	0.89770
<b>length</b>	70	5.22951	0.13802	5.22400	4.89900	5.54100

Pearson Correlation Coefficients, N = 70 Prob >  r  under H0: Rho=0			
	area	compactness	length
<b>area</b>	1.00000	0.54676 <.0001	0.51660 <.0001
<b>compactness</b>	0.54676 <.0001	1.00000	-0.37000 0.0016
<b>length</b>	0.51660 <.0001	-0.37000 0.0016	1.00000

Spearman Correlation Coefficients, N = 70 Prob >  r  under H0: Rho=0			
	area	compactness	length
<b>area</b>	1.00000	0.53005 <.0001	0.47883 <.0001
<b>compactness</b>	0.53005 <.0001	1.00000	-0.36143 0.0021
<b>length</b>	0.47883 <.0001	-0.36143 0.0021	1.00000

## Correlation analysis by variety

**variety=Kama**

<b>3 Variables:</b>	area	compactness	length
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<b>Simple Statistics</b>						
Variable	N	Mean	Std Dev	Median	Minimum	Maximum
<b>area</b>	70	14.33443	1.21570	14.35500	11.23000	17.08000
<b>compactness</b>	70	0.88007	0.01619	0.88050	0.83920	0.91830
<b>length</b>	70	5.50806	0.23151	5.53400	4.90200	6.05300

<b>Pearson Correlation Coefficients, N = 70</b>			
	area	compactness	length
<b>area</b>	1.00000	0.37104 0.0016	0.83478 <.0001
<b>compactness</b>	0.37104 0.0016	1.00000	-0.14630 0.2268
<b>length</b>	0.83478 <.0001	-0.14630 0.2268	1.00000

<b>Spearman Correlation Coefficients, N = 70</b>			
	area	compactness	length
<b>area</b>	1.00000	0.34061 0.0039	0.79428 <.0001
<b>compactness</b>	0.34061 0.0039	1.00000	-0.18310 0.1292
<b>length</b>	0.79428 <.0001	-0.18310 0.1292	1.00000

## Correlation analysis by variety

**variety=Rosa**

<b>3 Variables:</b>	area	compactness	length
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Simple Statistics						
Variable	N	Mean	Std Dev	Median	Minimum	Maximum
area	70	18.33429	1.43950	18.72000	15.38000	21.18000
compactness	70	0.88352	0.01550	0.88260	0.84520	0.91080
length	70	6.14803	0.26819	6.14850	5.36300	6.67500

Pearson Correlation Coefficients, N = 70 Prob >  r  under H0: Rho=0			
	area	compactness	length
area	1.00000	0.27263 0.0224	0.82643 <.0001
compactness	0.27263 0.0224	1.00000	-0.21695 0.0712
length	0.82643 <.0001	-0.21695 0.0712	1.00000

Spearman Correlation Coefficients, N = 70 Prob >  r  under H0: Rho=0			
	area	compactness	length
area	1.00000	0.19515 0.1055	0.85062 <.0001
compactness	0.19515 0.1055	1.00000	-0.17674 0.1433
length	0.85062 <.0001	-0.17674 0.1433	1.00000

Within each variety, area and length move together strongly (bigger seeds -> larger area), just like in the full data. Area vs. compactness is a weak-moderate positive (strongest in Canadian, weakest in Rosa). Length vs. compactness is not positive inside varieties-it's near zero for Kama/Rosa and negative for Canadian.