

Topological Defect Cavity in  
Linearly Approximated Ring Resonator

Dimerized Lattice  
(Report)

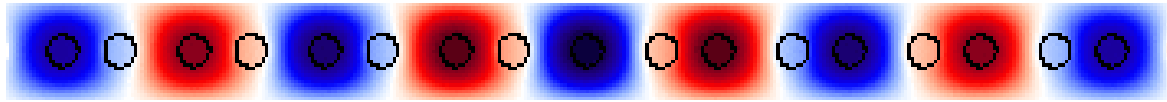
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# Coupled Cavity Modes

## First Cavity Mode



Fcen: 0.143880840001

Df: 0.01

Resolution: 20

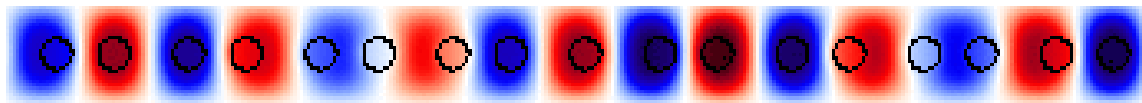
Detected Frequencies, Quality Factors, Amplitudes:

{0.143810939048/-3586..96/5.087}

{0.144030156815/60.50/0.2599}

Comments/Errors: None

## Second Cavity Mode



Fcen: 0.200000000000

Df: 0.005

Resolution: 20

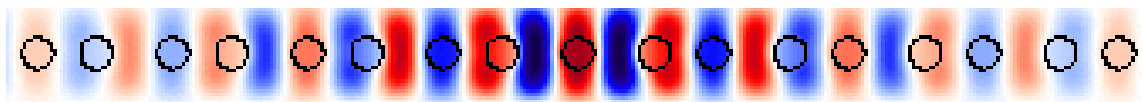
Detected Frequencies, Quality Factors, Amplitudes:

{0.199396105851/-160.99/0.1017}

{0.200991509668/-171.71/0.0737}

Comments/Errors: None

## Third Cavity Mode



Fcen: 0.311600000000

Df: 0.008

Resolution: 20

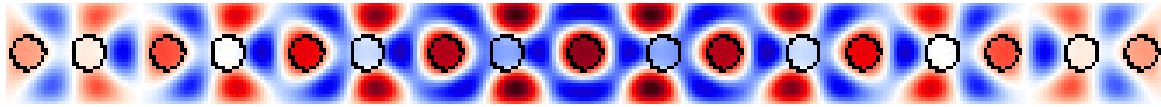
Detected Frequencies, Quality Factors, Amplitudes:

{0.310374417972/848.16/0.0089}

{0.311615003856/299.37/2.8453}

Comments/Errors: None

### Fourth Cavity Mode



Fcen: 0.380000000000

Df: 0.05

Resolution: 20

Detected Frequencies, Quality Factors, Amplitudes:

{0.380334670727/1115.57/0.0211}

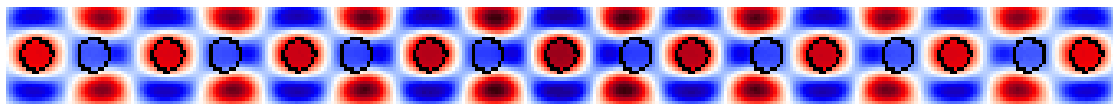
{0.383706672126/1163.52/0.7756}

{0.38602495445/950.70/1.0899}

Comments/Errors: None

## Isolated Cavity Modes

### Fourth Cavity Mode (1/2)



Fcen: 0.383713333583

Df: 0.002

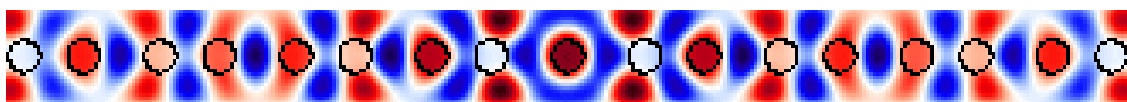
Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.383715719639/**129308.77**/17.0588}

Comments/Errors: Decent quality factor

### Fourth Cavity Mode (2/2)



Fcen: 0.38602495445

Df: 0.002

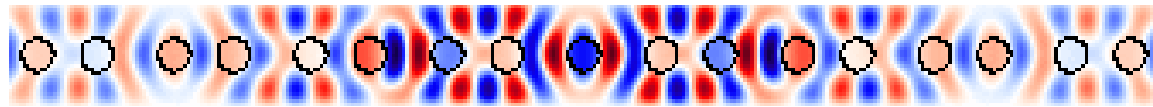
Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.386006873213/2676.87/9.2515}

Comments/Errors: None

### Fifth Cavity Mode



Fcen: 0.542059775082

Df: 0.0024

Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

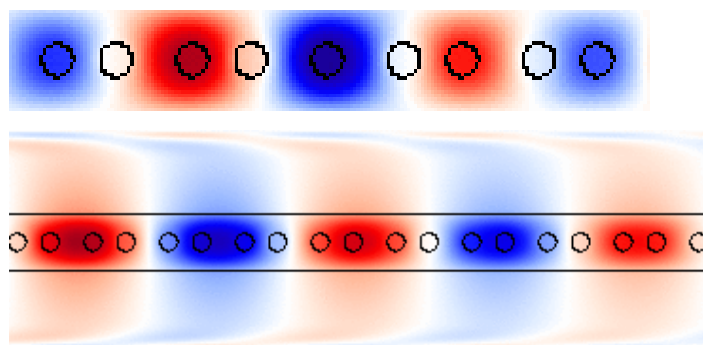
{0.542064236699/2950.24/11.6464}

Comments/Errors: Although from the results state it is the fifth mode, based on the larger than normal gap from the fourth cavity mode, it is suspected that the mode is the sixth cavity mode. Also notice how the higher order modes have no issues in being isolated, which will differ when dealing with lower modes in the next section.

## Anomalies in Isolated Cavity Modes

Hypothesis: Lower order modes require at least another frequency, no matter how little the amplitude, so that the standing wave can be localized at the center.

### First Cavity Mode



Fcen: 0.143810939048

Df: 0.0016

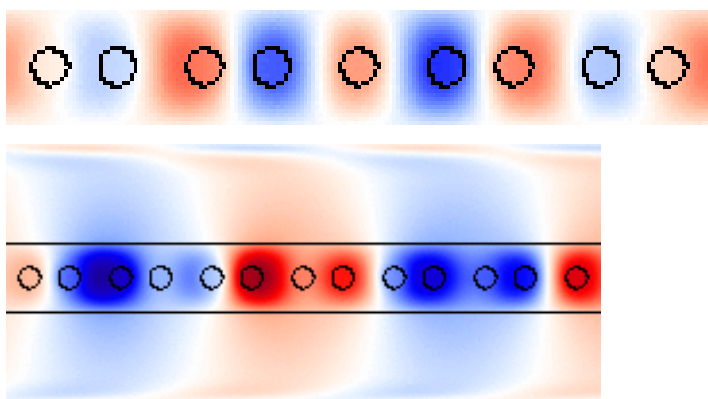
Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.14382268053/-3845.73/49.9267}

Comments/Errors: The first image is centered on the defect itself whereas the second image is centered at the left edge of the lattice. The right end is the same. Although removing other frequencies with negligible amplitudes in theory shouldn't affect the standing wave produced by the isolated mode, which can be seen in the previous section with higher order modes, the cavity mode was delocalized with a lot of the amplitude leaking through the lattice at the edges. The darkened packets at the edges slide outward without any regard for the lattice.

### Second Cavity Mode



Fcen: 0.20035362473

Df: 0.002

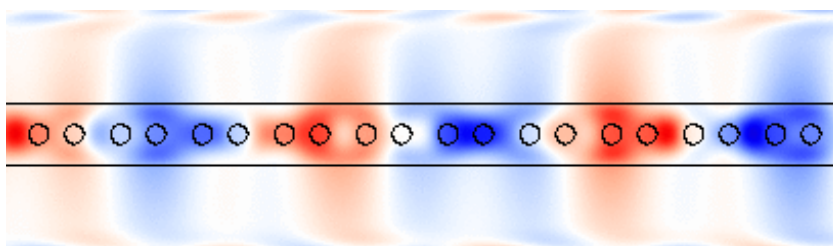
Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.200467161157/-3181.24/0.1989}

Comments/Errors: The anomaly is similar to the first isolated cavity mode, although at the center the standing wave is more faded than the original coupled mode, and the packets at the edges jump from group of holes instead of passing through them.

### Third Cavity Mode



Fcen: 0.31037441972

Df: 0.0022

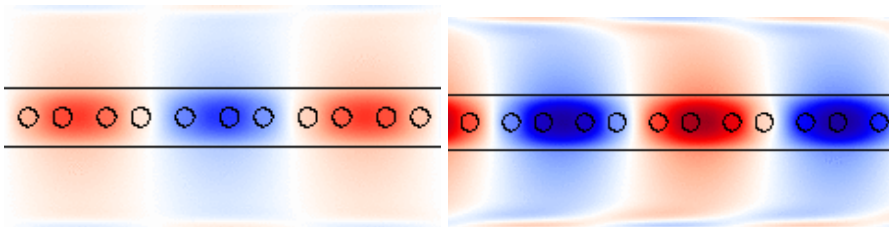
Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.310419018409/654.98/0.0086}

Comments/Errors: There is absolutely no light at the defect or the surrounding lattice structures. The removal of one of the frequencies that had a negligible amplitude in the coupled mode caused a significant drop in the quality factor and amplitude, and focused all the light to the edges where there is a high amount of leaking light.

### Stationary Mode



Fcen: 0.588468828044

Df: 0.002

Resolution: 20

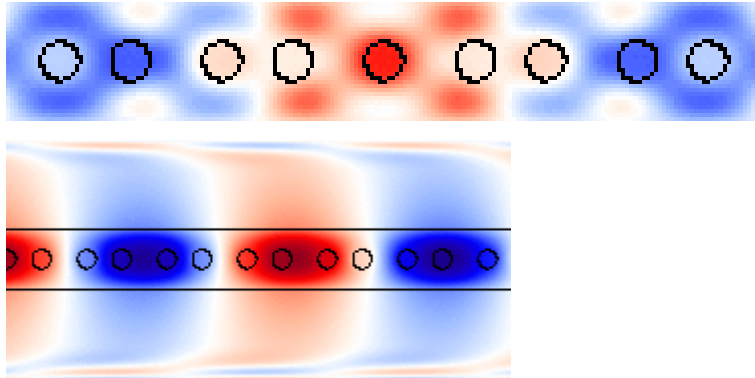
Detected Frequency, Quality Factors, Amplitudes:

{0.589375716351/461.16/0.0004}

Comments/Errors: Although having a very small amplitude, the light is still pronounced at the center and edges. The light does not move, or flash like it would in a standing wave, instead it darkens and then fades slightly as the gif resets the set of images.

# Chaotic Topological Modes

## High Quality Factor Leaky Mode



Fcen: 0.383713333583

Df: 0.0015

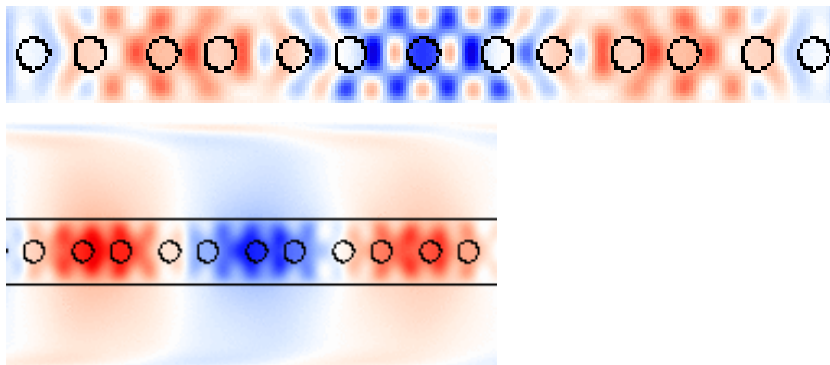
Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.383715504677/**2376954.80**/22.6175}

Comments/Errors: The after sources runtime was changed from the default value of 400 to 600.

## Flickering Cavity Mode



Fcen: 0.588468828044

Df: 0.0025

Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

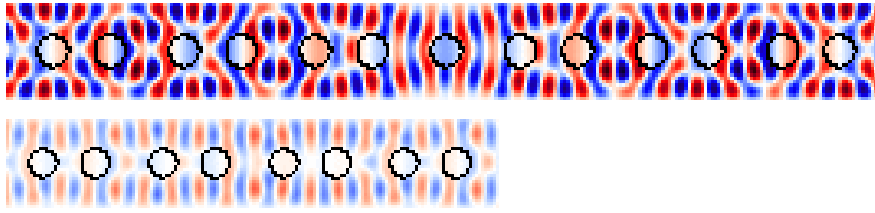
{0.588025851833/307.35/0.0006}

{0.589259756963/655.80/0.0002}

Comments/Errors: Instead of flashing between colours like in a regular standing wave, the mode flickers briefly and keeps the same colour.



### Higher Order Topological Mode



Fcen: 0.800000000000

Df: 0.05

Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.785601489422/229.37/0.0011}

{0.785601489422/-152.49/2.0830}

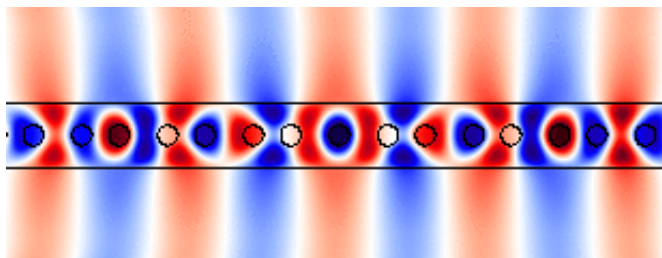
{0.809409808586/208.57/0.0109}

{0.8146372449482/-**20750.46**/0.0136}

{0.815342086385/1155.66/0.0108}

Comments/Errors: The first image is at the defect in the dimerized lattice although the intensity is not dispersed through the defect. The second image is some propagation at the sides. What is most noticeable is the highly negative quality factor of the fourth detected frequency.

### Leaky Cavity Mode



Fcen: 0.287761680000

Df: 0.01

Resolution: 20

Detected Frequency, Quality Factors, Amplitudes:

{0.285510053245/-89.98/0.0017}

{0.286526246084/-72.13/0.0030}

{0.288965424199/-56.67/0.0011}

Comments/Errors: Although it is a leaky mode, instead of having the outside intensity of light propagate along the lattice, the leaking seems to be an

extension to the flashing standing wave, in that it doesn't move in any direction which would suggest leakage, it only flashes.