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Week 7

Israel Nolazco

D)  $\sigma \rightarrow 40$  hrs  $\mu = 780$  hrs  
sample 30 bulbs

Find  $\Rightarrow$  96% confidence interval for the population mean  
of all light bulbs produced by this firm

$$96\% \Rightarrow P\left(-\frac{z_{\alpha}}{2} < Z < \frac{z_{\alpha}}{2}\right) = 1 - \alpha$$

$$96\% = 100(1 - \alpha)\%$$

$$.96 = 1 - \alpha$$

$$\boxed{\alpha = 0.04} \Rightarrow -z_{0.04/2} < Z < z_{0.04/2}$$

$$\Rightarrow -z_{0.02} < Z < z_{0.02}$$

Note since we are looking for 96% confidence interval  
then we are looking for the right hand side of the curve.

Thus  $z_{0.02} = 2.05$  \* from z-table website

statisticshowto.com

$$780 - 2.05 \left( \frac{40}{\sqrt{30}} \right) < \mu < 780 + 2.05 \left( \frac{40}{\sqrt{30}} \right)$$

i) continue

$$780 - 2.05 \left( \frac{40}{\sqrt{30}} \right) < M < 780 + 2.05 \left( \frac{610}{\sqrt{30}} \right)$$

$$\Rightarrow 765.02 < M < 794.97$$

which if we round them  $\Rightarrow [765 < M < 795]$  for  
an interval confidence of 96%

2) How big or a sample if we wish.

96% confidence interval with 10 hrs of true mean

$$770 < \mu < 790$$

$$770 = 780 - 2.05 \left( \frac{40}{\sqrt{n}} \right)$$

$$2.05 \left( \frac{40}{\sqrt{n}} \right) = 780 - 770$$

$$2.05 = (780 - 770) \left( \frac{\sqrt{n}}{40} \right)$$

$$\left( 40 \left( \frac{2.05}{780 - 770} \right) \right)^2 = (\sqrt{n})^2$$

$$67.24 = n \quad \text{The sample size would need to be about 67 light bulbs}$$

$$3) 3.4, 2.5, 4.8, 2.0$$

$$3.6, 2.8, 3.3, 5.6$$

$$3.7, 2.8, 4.4, 4.0$$

$$3.2, 3.0, 4.8$$

$n = 15$  samples

\* Note: lets go back to ch. 8.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\bar{x} = \frac{3.4 + 2.5 + 4.8 + \dots + 3.0 + 4.8}{15} = \frac{56.8}{15}$$

$$\bar{x} = 3.8$$

standard deviation

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$s^2 = \frac{1}{14} \left[ (3.4 - 3.8)^2 + (2.5 - 3.8)^2 + (4.8 - 3.8)^2 + \dots + (3.0 - 3.8)^2 + (4.8 - 3.8)^2 \right]$$

$$s^2 = \frac{1}{14} [ 13.2 ]$$

$$s = \sqrt{\frac{13.2}{14}} = 0.97$$

Now that we have  $\bar{x}$ ,  $n$  &  $s$  we need to find our 95% prediction interval for the drying for the next trial of paint

$$95\% = 100(1-\alpha)^{\frac{3}{2}}$$

$$0.95 = (1-\alpha) \Rightarrow \alpha = 0.05$$

$$z_{\frac{\alpha}{2}} \Rightarrow z_{0.025}$$

$$-z_{0.025} < \mu < z_{0.025} \Rightarrow \text{covers the } 95\%$$

Note: Since we are looking at random sampling

& doing a prediction. This looks more of a  $t$ -distribution

Therefore  $V=14$  degrees of freedom

$$z_{0.025} = 2.145 \quad \text{from table A.4}$$

$$3.8 - 2.145(0.97)(\sqrt{1+\frac{1}{14}}) < \mu < 3.8 + 2.145(0.97)(\sqrt{1+\frac{1}{14}})$$

$$3.8 - 2.148 < \mu < 3.8 + 2.148$$

$$\boxed{1.65 < \mu < 5.95}$$

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9)

Using method 1

$$n = 100$$

98% confidence

$$X = 8$$

$$\hat{q} = 1 - \hat{p}$$

$$\hat{p} = \frac{X}{n} = 0.08$$

$$\hat{p} - z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}\hat{q}}{n}} < p < \hat{p} + z_{\frac{\alpha}{2}} \sqrt{\frac{\hat{p}\hat{q}}{n}}$$

$$98\% = 100(1-\alpha)\%$$

$$0.98 = 1 - \alpha \Rightarrow 0.02 = \alpha \quad \frac{\alpha}{2} = 0.01$$

$$0.08 - 2.325 \sqrt{\frac{(0.08)(0.92)}{100}} < p$$

$$z_{0.01} = 2.325$$

$$0.08 + 2.325 \sqrt{\frac{(0.08)(0.92)}{100}} > p$$

$$0.08 - 0.063 < p < 0.08 + 0.063$$

$$0.017 < p < 0.143$$