```
import tensorflow as tf # Import TensorFlow library
from tensorflow.keras.datasets import mnist # Import MNIST dataset
from tensorflow.keras.models import Sequential # Import Sequential model class
from tensorflow.keras.layers import Dense, Flatten # Import layers: Dense and Flatten
from tensorflow.keras.utils import to_categorical # Import utility for one-hot encoding
import matplotlib.pyplot as plt # Import matplotlib for plotting
import numpy as np # Import NumPy for numerical operations
# 1. Load and preprocess the data
(x_train, y_train), (x_test, y_test) = mnist.load_data() # Load MNIST dataset (60k train, 10k test)
# Normalize pixel values to range [0,1]
x_train = x_train.astype("float32") / 255.0
x_{test} = x_{test.astype("float32")} / 255.0
# One-hot encode labels (e.g., '3' -> [0,0,0,1,0,0,0,0,0,0])
y_train_cat = to_categorical(y_train, 10)
y_test_cat = to_categorical(y_test, 10)
# 2. Build the model
model = Sequential([
                                       # Flatten 28x28 image into 784 vector
   Flatten(input_shape=(28,28)),
   Dense(128, activation='relu'),
                                      # Fully connected hidden layer with ReLU
   Dense(10, activation='softmax')
                                      # Output layer with 10 neurons for digits 0-9
])
# 3. Compile the model
model.compile(optimizer='adam', # Adam optimizer
             loss='categorical_crossentropy', # Loss for multi-class classification
             metrics=['accuracy']) # Track accuracy during training
# 4. Train the model
model.fit(x_train, y_train_cat, epochs=5, batch_size=32, validation_split=0.1)
# Train for 5 epochs with batch size 32, using 10% of training data for validation
# 5. Evaluate the model
test_loss, test_acc = model.evaluate(x_test, y_test_cat, verbose=0) # Evaluate on test set
print(f"Test Accuracy: {test_acc:.4f}") # Print test accuracy
# 6. Predict a single test sample
sample_index = 0 # Choose the first test image
sample_image = x_test[sample_index] # Extract image
sample_label = y_test[sample_index] # Extract true label
sample_input = np.expand_dims(sample_image, axis=0) # Add batch dimension (1,28,28)
pred_probs = model.predict(sample_input) # Predict softmax probabilities
pred_class = np.argmax(pred_probs) # Get class with highest probability
print("True label:", sample_label) # Print true label
print("Predicted label:", pred_class) # Print predicted label
print("Softmax probabilities:", pred_probs[0]) # Print probability distribution
# 7. Optional: plot the image and probabilities
plt.figure(figsize=(8,4))
# Show the test image
plt.subplot(1,2,1)
plt.imshow(sample_image, cmap='gray')
plt.title(f"True: {sample_label}, Pred: {pred_class}")
plt.axis('off')
# Show softmax probabilities as a bar chart
```

```
plt.subplot(1,2,2)
plt.bar(range(10), pred_probs[0])
plt.xticks(range(10))
plt.xlabel("Digit")
plt.ylabel("Probability")
plt.title("Softmax Probabilities")
plt.tight_layout()
plt.show()
```