

N.B.

- Answer **SIX** questions, taking any **THREE** from each section.
- All questions are equal values.
- Use **separate answer script** for each section

Section A

- (a) Define frequency distribution. For the following data, construct a frequency table using suitable class interval. 6.67

11	20	16	10	22	7	13	14	23	11
15	5	10	12	14	18	15	13	11	6
26	16	14	18	27	29	23	33	17	24
17	18	21	11	10	12	12	18	15	16
22	14	14	8	9	17	15	14	10	11

- (b) How do you distinguish variable from attributes? 2
- (c) Construct a Pie Chart with the following frequency table. 3

Size of the Shirt	S	M	L	XL
Frequency (Number of Shirts)	15	26	12	7

- (a) What is central tendency? Describe any three measures of central tendency with their advantages and disadvantages. 6
- (b) Prove that $AM \geq GM \geq HM$ where the notations have their usual meanings. When does equality hold? 5.67

- (a) What is dispersion? What are the measures of dispersion? Describe the relative measures of dispersion. Why do need measures of dispersion? Explain. 5
- (b) The following data are the monthly household incomes (in Tk.) of ten families 4

10648	17416	6517	13555	14821
9226	52923	11800	18527	12222

Calculate Variance of the household incomes and comment.

- (c) What do β_1 and β_2 measure? The notations have their usual meanings. Comment on the shape of the frequency distribution when it is characterized with the following measures. $\beta_1 = 0, \beta_1 < 0, \beta_1 > 0$ and $\beta_2 = 3$ 2.67
- (a) Define correlation. How do you interpret the values of correlation coefficient r ? What are the properties of correlation coefficient? 6
- (b) Show that the simple correlation coefficient r lies between -1 to $+1$. 5.67

Section B

- (a) What is regression analysis? How does it differ from correlation analysis? 3
- (b) How do you estimate the parameters of a simple linear regression model using OLS method? 6
- (c) Consider a two variable regression model 2.67

$$Y_i = \alpha + \beta X_i + u_i, \quad i = 1, 2, \dots, n.$$

For a particular data set you estimate the parameters and obtain the following results. $\hat{\alpha} = 20$ and $\hat{\beta} = 3$. Interpret the result.

- (a) Define random experiment, sample space and mutually exclusive events. 3
- (b) Define classical probability. Suppose two balanced dice are thrown. Find the probability that
 - The sum of the outcomes of two dice is 3. 5
 - The sum of the outcomes of two dice is greater than 4.
- (c) If two events A and B are independent then their complements are also independent. 3.67
- (a) Define Random variable with examples. When a function is said to be a probability mass function? 3
- (b) Suppose a fair coin is tossed times. Define a random variable X as the number of tails. Find the probability function of the random variable. Also find
 - $P(x \geq 2)$
 - $P(x < 1)$
 - $P(0 < x < 3)$
- (c) Let X be a continuous random variable with probability density function 3.67

$$f(x) = kx(1-x); 0 \leq x \leq 1.$$

Find the value of k

- (a) Define mathematical expectation and variance of random variable. 3
- (b) Let X be a random variable with the following probability function. 4

X: x	0	1	2
P(x)	1/4	1/2	1/4

Find (i) $E(X), E(3X + 2)$ (ii) $V(X), V(5X + 1)$

- (c) What is stochastic process? What are the various types of stochastic process? How will you relate 4.67

SECTION-A

1. (a) Define conductor, semiconductor and insulator with energy band diagram.
- (b) Determine V_o and I for the network of figure-1

2^{2/3}

4

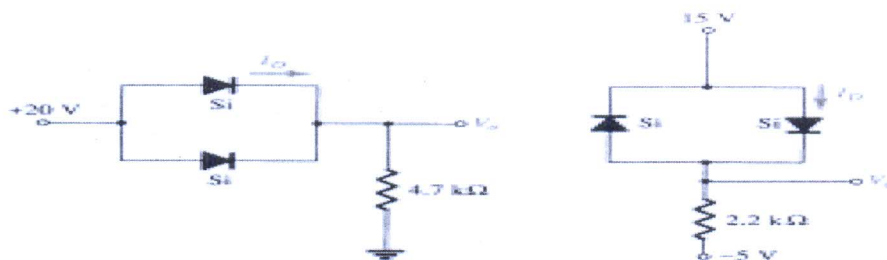


Figure-1

- (c) What is load line? Briefly explain how you can find point of operation of a diode using load line.
- (d) What is the basic difference between electrical circuit and electronic circuit?

3

2

2. (a) Determine V_o for the network of figure-2

3

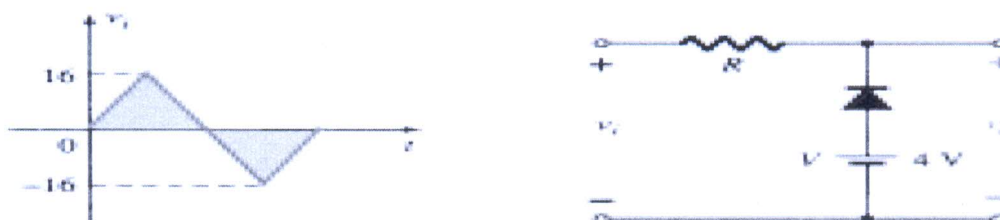


Figure-2

- (b) What is Zener diode? How a Zener diode can be used as a voltage regulator?
- (c) (a) For the Zener diode network of figure-3, determine V_L , V_R , I_Z and P_Z .
- (b) Repeat part (a) with $R_L = 3K\Omega$

3^{2/3}

4

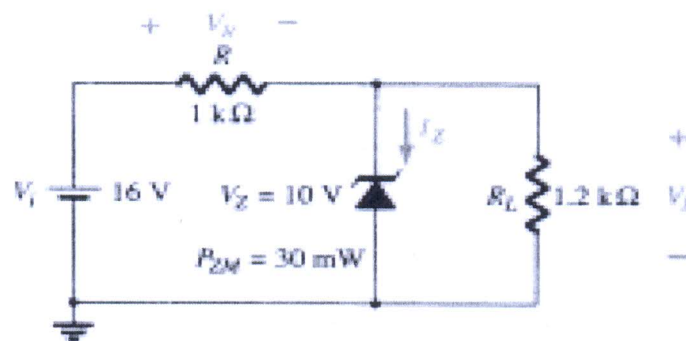


Figure-3

- (d) What is PIV?

1

3. (a) Draw and explain input and output characteristics of common base configuration of Bipolar Junction Transistor.
- (b) Discuss BJT amplifying action. Why it is called transistor?
- (c) From the emitter bias network, determine

4^{2/3}

3

4

- (i) I_B
- (ii) V_{CE}
- (iii) V_B
- (iv) V_{BC}

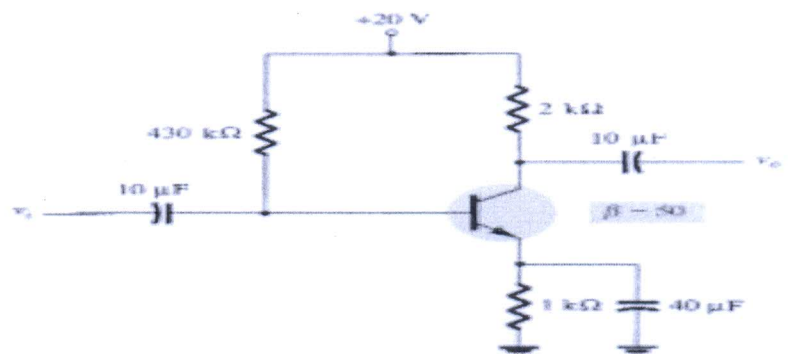


Figure-4

4. (a) Briefly explain transistor operation with neat sketch 3^{2/3}
 (b) Determine Input impedance Z_{IN} , Output impedance Z_O , Voltage gain A_V , and Current gain A_I for the common-emitter fixed biased configuration of figure-5 5

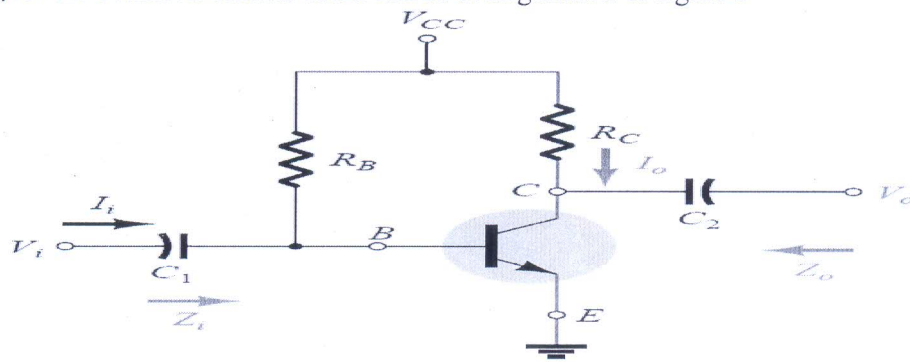


Figure-5

- (c) Is transistor a bipolar device? Why so? 1.5
 (d) Write short notes on reverse recovery time and transition capacitance 1.5

SECTION-B

5. (a) What is buffer amplifier? Why we use buffer amplifier in spite of unity gain noninverting amplifier? 4^{2/3}
 (b) Design an amplifier circuit using OP-AMP whose input is +1V and required output is +20 volt 3
 (c) Derive an expression of output voltage of an noninverting operational amplifier 3
 (d) What is open loop gain? 1
6. (a) Derive the expression of integrator by using 741 op-amp. 4^{2/3}
 (b) Suppose that you have three battery say 1V, 2V, and 3V. How do you add these three voltage using operational amplifier? 4
 (c) What is feedback circuit? Write down the advantages of feedback circuit. 3
7. (a) Draw the circuit diagram of four basic feedback tropology. 4
 (b) What is oscillator? Write short notes on feedback oscillator and relaxation oscillator. 4^{2/3}
 (c) Briefly discuss Wien-Bridge oscillator circuit with neat sketch. 3
8. (a) What is LED? Today why we use LED bulb as an alternative of incandescent bulb? Write down the application of LED. 3^{2/3}
 (b) What is photo conductive cell? Draw and explain illumination characteristics of photoconductive cell. 3
 (c) What is optocoupler? How it works? 2
 (d) Suppose that your teacher give you a red LED and told you to check it. Design a circuit to check that LED. Assume any value as you want. 3

N.B.

- i) Answer **SIX** questions, taking any **THREE** from each section.
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Section-A

1. (a) Define domain and range of a real function 2
 (b) Drawing the graph find the domain and range of the following function. 3

$$f(x) = \begin{cases} x^2 + 1 & \text{when } x < 0 \\ x & \text{when } 0 \leq x \leq 1 \\ \frac{1}{x} & \text{when } 1 < x \end{cases}$$

 (c) Define limit of a function. Using the (ϵ, δ) definition of limit show that 3.67

$$\lim_{x \rightarrow a} \left(\frac{x^2 - a^2}{x - a} \right) = 2a$$

 (d) Define continuous function. A function $f(x)$ is defined as follows: 3

$$f(x) = -x \text{ When } x \leq 0$$

$$= x \text{ when } 0 < x < 1$$

$$= 2-x \text{ when } x \geq 1$$

 Test the continuity at $x=1$
 2. (a) Show that the function $f(x) = |x-1| + |x-2|$ is not differentiable at $x=2$. 4
 (b) If $y = \left(\frac{n}{x}\right)^{nx} \left(1 + \ln \frac{x}{n}\right)$ find $\frac{dy}{dx}$ 3
 (c) If $f(x) = \left(\frac{a+x}{b+x}\right)^{a+b+2x}$, then show that $f(0) = \left(\frac{a}{b}\right)^{a+b} \left[\frac{b^2-a^2}{ab} + 2 \ln \frac{a}{b}\right]$ 4.67
 3. (a) Find the n th derivatives of the function $y = \frac{1}{x^2 + a^2}$. 4
 (b) Verify mean value theorem for the following function and find C if possible $f(x) = (x-1)(x-2)(x-3)$ in $[0, 4]$ 4
 (c) State and prove Leibnitz theorem. 3.67
 4. (a) State and prove mean value theorem. 4
 (b) If $V = \sin^{-1} \frac{x^2 + y^2}{x+y}$, then prove that $xV_x + yV_y = \tan V$ 4
 (c) State and prove Euler's theorem. 3.67

Section-B

5. (a) Evaluate the following integrals (i) $\int \frac{dx}{\sqrt{x+a} + \sqrt{x+b}}$ (ii) $\int \sec^{2n+2} x dx$ 11.67
 (iii) $\int \frac{1}{(1+x^2)\sqrt{1-x^2}} dx$ (iv) $\int \frac{dx}{\sqrt{(x-a)(b-x)}}$
 6. (a) State and prove fundamental theorem of integral calculus. 5
 (b) Integrate (i) $\int \frac{dx}{x^3+1}$ (ii) $\int \frac{dx}{1+\tan x}$ 6.67
 7. (a) Evaluate $\int_a^\beta \sqrt{(x-\alpha)(x-\beta)} dx$ 3.67
 (b) Find the reduction formula for $\int \sin^m x \cos^n x dx$ and hence find the value of $\int_0^{\frac{\pi}{6}} \sin^4 3x dx$ 4
 (c) If $U_{(m,n)} = \int_0^{\frac{\pi}{2}} \sin^m x \cos^n x dx$ then prove that $U_{(m,n)} = \frac{n-1}{m+n} U_{(m,n-2)}$ 4
 8. (a) Find the area of the region bounded by the curve $a^2 y^2 = a^2 x^2 - x^4$ 3.67
 (b) Find the area enclosed by the parabolas $y^2 = 4ax$ and $x^2 = 4ay$ 4
 (c) Find the volume of the solid formed by the revolution of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ 4

Full Marks: 70

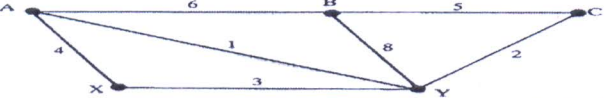
Times: 4 Hours

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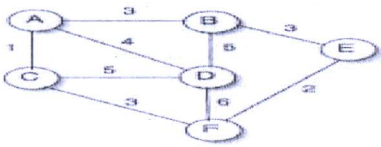
SECTION-A

1. a) What do you mean by data structure? Explain the basic operations those are normally performed on a particular data structure. 4
b) Describe how arrays stored in memory. How you dynamically allocate memory and used it as an array using pointer. 4
c) Describe a situation where storing items in array is clearly better than storing items on a linked list. 3.67
2. a) How you check for balanced parentheses in an expression? 4
b) What is Recursion? Write a program to generate Fibonacci series using recursion. 3.67
c) Describe the implementation of queue using link list. 4
3. a) What do you mean by binary search tree? 2
b) Build a heap from the following list of numbers: 40, 30, 70, 23, 54, 50, 21, 44, 55, 77. 6
c) Explain "For breath first search; it traverse a graph from lowest level to highest level with respect to start node". 3.67
4. a) What do you mean by topological sort and Minimum spanning tree? 3
b) Write down the algorithm of searching a linked list when the list is unsorted. 4
c) **The pre-order and in-order traversal sequences of nodes in a binary tree are given below:** 4.67
Pre-order — M A D H U S M I T A
In-order — M A D H U S M I T A
Construct the binary tree and state the logic to construct the tree.

SECTION-B

5. a) What is hashing? What is main advantage that open addressing hashing technique has over chaining? 3
b) Write down some hash functions with their limitation and advantages. 3
c) What are the advantages of linked list over array? Consider the following list of 11 numbers: 33 11 77 45 23 17 60 25 71 31 85. Use the Quick sort algorithm to find the final position of 33. 3.67
6. a) What is graph? Give practical use of graph, DFS and BFS. 4
b) How do you determine all vertices of a graph are connected or not and write pseudo code for implementation. 4
c) How file are stored logically in computer disc. 4
7. a) Find a minimal spanning tree of the following weighted graph using Prim's algorithm. 4

- b) Write the Huffman's Algorithm. Suppose A, B, C, D, E, F, G and H are 8 items and suppose they are assigned Weights as follows: 4

Data Item :	A	B	C	D	E	F	G	H
Weight :	22	5	11	19	2	11	25	5

Construct a tree using Huffman's algorithm.
- c) How you convert infix expression to postfix expression? 3.67
8. a) How you represent this graph in computer. 3

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Construct a tree using Huffman's algorithm.
- c) How you find maximum path between to vertices in graph. 5.67

- Q.6. a) Distinguish between interference and diffraction process. 2
- b) Obtain the maxima and minima of interference from Fraunhofer diffraction at double slit. 5
- c) Explain polarization of light on the basis of electromagnetic theory. 2.67
- d) What do you understand by optical activity of a material? 2
- Q.7 a) Deduce the Coulombs law from Gauss's law. 2.67
- b) For a parallel capacitor, prove that, $\epsilon_0 \oint \vec{K} \cdot d\vec{S} = Q$ where the symbols have their usual meaning. 5
- c) Mention some application of Biot - savart law. 2
- d) An electric dipole consists of two opposites charges of magnitude $q = 2.0 \times 10^{-6}$ Coul separated by 2.0cm. The dipole is placed in an external field of 2.0×10^5 Newton/Coul. Calculate the maximum torque on the dipole. 2
- Q.8 a) What is meant by Faraday effect? Give the physical interpretation of Faraday effect. 3
- b) Discuss the magnetic effect of current with the help of Biot –Savart law. 3
- c) Calculate the energy density of the electromagnetic field in empty space. 4
- d) Mention the Maxwell equations with their origin. 1.67

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Section B

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7. (a) Define Random variable with examples. When a function is said to be a probability mass function? 3
- (b) Suppose a fair coin is tossed times. Define a random variable X as the number of tails. Find the probability function of the random variable. Also find 5

(i) $P(x \geq 2)$ (ii) $P(x < 1)$ (iii) $P(0 < x < 3)$

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- $$f(x) = kx(1-x); 0 \leq x \leq 1.$$

Find the value of k

8. (a) Define mathematical expectation and variance of random variable. 3
- (b) Let X be a random variable with the following probability function. 4

X: x	0	1	2
	$\frac{1}{4}$	$\frac{1}{2}$	$\frac{1}{4}$