Announcements Nested declarations Higher-order functions Scope of names

L3: Higher-order Functions; Scope of Names

Structure and Interpretation of Computer Programs

Martin Henz

July 7, 2023



- 1 Announcements
- 2 Nested declarations
- 3 Higher-order functions
- Scope of names

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- Contest "Beautiful Runes" opens today! Closes on Monday, 10/7. Contests are not graded.
- Exam: On Thursday, 20/7, 10am to 12noon.

Announcements
Nested declarations
Higher-order functions
Scope of names

Schedule

Schedule

- Lectures, 10am–12noon: Saturday (8/7), Monday–Saturday (10/7-15/7)
- Labs, 2pm-6pm: Monday-Saturday (10/7-15/7)
- Project work: 17/7-12/7
- Project presentations: Tuesday 25/7

Announcements
Nested declarations
Higher-order functions
Scope of names

Read the textbook



- Read the textbook
- Use the substitution model (and stepper tool, if needed)

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- Think, then program

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- Use the substitution model (and stepper tool, if needed)
- Think, then program
- Less is more

- 1 Announcements
- 2 Nested declarations
 - Nested function declarations
 - Nested constant declarations
- 3 Higher-order functions
- 4 Scope of names

Names can refer to intermediate values

Example from SICP JS 1.3.2

$$f(x,y) = x(1+xy)^2 + y(1-y) + (1+xy)(1-y)$$

Compute f(2,3)

```
function f(x, y) {
    const a = 1 + x * y;
    const b = 1 - y;
    return x * square(a) + y * b + a * b;
}
f(2, 3);
```

Can we do this with functions, too?

```
function sum_of_squares(a, b) {
    return square(a) + square(b);
}
function hypotenuse(a, b) {
    return math_sqrt(sum_of_squares(a, b));
}
```

"Hiding"

Can we hide the function sum_of_squares so that only the body of hypotenuse can "see" it?

Yes, we can! (see also SICP JS 1.1.8)

```
function hypotenuse(a, b) {
    function sum_of_squares(a, b) {
        return square(a) + square(b);
    }
    return math_sqrt(sum_of_squares(a, b));
}
```

Yes, we can! (see also SICP JS 1.1.8)

```
function hypotenuse(a, b) {
    function sum_of_squares(a, b) {
        return square(a) + square(b);
    }
    return math_sqrt(sum_of_squares(a, b));
}
```

Function nesting

Function declarations can be *nested inside of* other function declarations, and only visible there.

sum_of_squares could use parameters of hypotenuse

```
function hypotenuse(a, b) {
    function sum_of_squares() {
        return square(a) + square(b);
    }
    return math_sqrt(sum_of_squares());
}
```

Even simpler version: Using nested const

```
function hypotenuse(a, b) {
    const sum_of_squares = square(a) + square(b);
    return math_sqrt(sum_of_squares);
}
```

Can we avoid tree recursion?

Can we avoid tree recursion?

Question

Can we implement this function with linear recursion?

Is this a good idea?

Is this a good idea?

Can we declare a const...

Is this a good idea?

Can we declare a const...

...just for the alternative of the conditional?

```
function fractal_3(rune, n) {
   if (n === 1) {
      return rune;
   } else {
      const f = fractal_3(rune, n - 1);
      return beside(rune, stack(f, f));
   }
}
```

```
function fractal_3(rune, n) {
   if (n === 1) {
      return rune;
   } else {
      const f = fractal_3(rune, n - 1);
      return beside(rune, stack(f, f));
   }
}
```

Each branch of the conditional is a block.

```
function fractal_3(rune, n) {
   if (n === 1) {
      return rune;
   } else {
      const f = fractal_3(rune, n - 1);
      return beside(rune, stack(f, f));
   }
}
```

- Each branch of the conditional is a block.
- A block can have local names, only visible inside the block.

```
function fractal_3(rune, n) {
   if (n === 1) {
      return rune;
   } else {
      const f = fractal_3(rune, n - 1);
      return beside(rune, stack(f, f));
   }
}
```

- Each branch of the conditional is a block.
- A block can have local names, only visible inside the block.
- Remember to return a result in each branch.
 (Otherwise undefined is returned.)



- 1 Announcements
- Nested declarations
- 3 Higher-order functions
 - Functions as arguments (1.3.1)
 - Lambda expressions (1.3.2)
 - Functions as returned values (1.3.4)
 - Summary of constructs discussed today
- 4 Scope of names

Passing functions to functions

```
function f(g, x) {
    return g(x);
}

function g(y) {
    return y + 1;
}

f(g, 7);
```

Passing more functions to functions

```
function f(g, x) {
    return g(g(x));
}

function g(y) {
    return y + 1;
}

f(g, 7);
```

Abstraction: Recall repeat_pattern

```
Repeating the pattern n times
```

```
repeat_pattern(4, make_cross, rcross);
```

Passing a rune function

Look at this function (1.3.1)

...and this one

Abstraction (1.3.1)

Abstraction (1.3.1)

```
function sum(a, b) {
     return a > b ? 0
                     : (compute value with a)
                       +
                       sum(\langle next value from a \rangle, b);
in Source:
function sum(term, a, next, b) {
     return a > b ? 0
                     : term(a)
                       +
                       sum(term, next(a), next, b);
}
```

sum_integers using sum

```
function identity(x) {
    return x;
}
function plus_one(x) {
    return x + 1;
}
function sum_integers(a, b) {
    return sum(identity, a, plus_one, b);
}
```

sum_skip_cubes using sum

```
function cube(x) {
    return x * x * x;
}
function plus_two(x) {
    return x + 2;
}
function sum_skip_cubes(a, b) {
    return sum(cube, a, plus_two, b);
}
```

sum_skip_cubes using sum

```
function cube(x) {
    return x * x * x;
}
function plus_two(x) {
    return x + 2;
}
function sum_cubes(a, b) {
    return sum(cube, a, plus_two, b);
}
```

Visibility



sum_skip_cubes using sum

```
function cube(x) {
    return x * x * x;
}
function plus_two(x) {
    return x + 2;
}
function sum_cubes(a, b) {
    return sum(cube, a, plus_two, b);
}
```

Visibility

Can we "hide" cube and plus_two inside of sum_skip_cubes?



Yes, we can! (see also SICP JS 1.1.8)

```
function sum_skip_cubes(a, b) {
    function cube(x) {
        return x * x * x;
    }
    function plus_two(x) {
        return x + 2;
    }
    return sum(cube, a, plus_two, b);
}
```

```
function sum_skip_cubes(a, b) {
    function cube(x) {
        return x * x * x;
    }
    function plus_two(x) {
        return x + 2;
    }
    return sum(cube, a, plus_two, b);
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function sum_skip_cubes(a, b) {
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        return x * x * x;
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    function plus_two(x) {
        return x + 2;
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    return sum(cube, a, plus_two, b);
}
```

This is still quite verbose

```
function sum_skip_cubes(a, b) {
    function cube(x) {
        return x * x * x;
    }
    function plus_two(x) {
        return x + 2;
    }
    return sum(cube, a, plus_two, b);
}
```

This is still quite verbose

Do we need all these words such as function, return?

```
function sum_skip_cubes(a, b) {
    function cube(x) {
        return x * x * x;
    }
    function plus_two(x) {
        return x + 2;
    }
    return sum(cube, a, plus_two, b);
}
```

This is still quite verbose

Do we need all these words such as function, return?

Do we need to even give names to these functions?



No, we don't! Lambda expressions

```
function sum_skip_cubes(a, b) {
    function cube(x) {
        return x * x * x;
    function plus_two(x) {
        return x + 2;
    return sum(cube, a, plus_two, b);
// instead just write:
function sum_skip_cubes(a, b) {
   return sum(x => x * x * x, a, x => x + 2, b);
}
```

Lambda expressions (1.3.2)

```
New kinds of expressions
```

(parameters) => expression

Lambda expressions (1.3.2)

New kinds of expressions

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If there is only one parameter, you can write

parameter => expression

Lambda expressions (1.3.2)

New kinds of expressions

(parameters) => expression

If there is only one parameter, you can write

parameter => expression

Meaning

The expression evaluates to a function value.

Function has given parameters and return expression; as body.

An alternative syntax for function declaration

```
function plus4(x) {
    return x + 4;
}
can be written as
const plus4 = x => x + 4;
```

Returning Functions from Functions (1.3.4)

```
function make_adder(x) {
    function adder(y) {
        return x + y;
    }
    return adder;
}

const adder_four = make_adder(4);
adder_four(6);
```

...or with the new lambda expressions

```
function make_adder(x) {
    return y => x + y;
}

const adder_four = make_adder(4);
adder_four(6);
```

Returning Functions from Functions

```
function make_adder(x) {
    return y => x + y;
}

( make_adder(4) )(6);

// you can also write:
//
// make_adder(4)(6);
```

Returning Functions from Functions

```
function make_adder(x) {
    return y => x + y;
}

const adder_1 = make_adder(1);
const adder_2 = make_adder(2);

adder_1(10); // returns 11

adder_2(20); // returns 22
```

Summary of constructs discussed today

- Nested constant and function declaration statements
- Conditional statements and blocks
- Lambda expressions

- 1 Announcements
- Nested declarations
- 3 Higher-order functions
- Scope of names
 - Examples
 - Overview of scoping rules
 - The details

Scope of names: an example

```
const z = 2;
function f(g) {
    const z = 4;
    return g(z);
}
f( y => y + z );
```

Scope of names: an example

```
const z = 2;
function f(g) {
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```

Questions about scope

What names are declared by this program?

Scope of names: an example

```
const z = 2;
function f(g) {
    const z = 4;
    return g(z);
}
f( y => y + z );
```

Questions about scope

What names are declared by this program? Which declaration does each name occurrence refer to?

Scope of names: another example

```
const x = 10;
function square(x) {
    return x * x;
}
function addx(y) {
    return y + x;
}
square(x + 5) * addx(x + 20);
```

Questions about scope

Which declaration does each occurrence of x refer to?



Scope of names: yet another example

```
const pi = 3.141592653589793;
function circle_area_from_radius(r) {
   const pi = 22 / 7;
   return pi * square(r);
}
```

Questions about scope

Which declaration does the occurrence of pi refer to?

Scope of names: hypotenuse example

```
function square(x) {
    return x * x;
}
function hypotenuse(a, b) {
    function sum_of_squares() {
        return square(a) + square(b);
    }
    return math_sqrt(sum_of_squares());
}
```

Scope of names: hypotenuse example

```
function square(x) {
    return x * x;
}
function hypotenuse(a, b) {
    function sum_of_squares() {
        return square(a) + square(b);
    }
    return math_sqrt(sum_of_squares());
}
```

Names can refer to declarations outside of the immediately surrounding function declaration.

Overview of scoping rules

Declarations mandatory

All names in Source must be declared.

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All names in Source must be declared.

Forms of declaration

- Pre-declared names
- 2 Constant declarations
- Parameters of function declarations and lambda expressions
- Function name of function declarations

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Declarations mandatory

All names in Source must be declared.

Forms of declaration

- Pre-declared names
- 2 Constant declarations
- Parameters of function declarations and lambda expressions
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Scoping rule

A name occurrence refers to the closest surrounding declaration.



Forms of Declaration

(1) Pre-declared names

The Source §1 pages tell us what names are pre-declared, e.g. math_floor.

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(1) Pre-declared names

The Source §1 pages tell us what names are pre-declared, e.g. math_floor.

We can also import further pre-declared names from modules. For example, from the rune module:

```
import { heart, quarter_turn_right } from "rune";
```

Forms of Declaration

(2) Constant declarations

The scope of a constant declaration is the closest surrounding pair of $\{\ldots\}$, or the whole program, if there is none.

Example

```
function f(x, y) {
    if (x > 0) {
        const z = x * y;
        return math_sqrt(z);
    } else {
        ...
    }
}
```

Forms of Declaration

(3) Parameters

The scope of the parameters of a lambda expression or function declaration is the body of the function.

```
function f(x, y, z) {
    ... x ... y ... z ...
}
(v. w. u) => ... v ... w ... u ...
```

Forms of Declaration

(4) Function name

The scope of the function name of a function declaration is as if the function was declared with const.

Lexical scoping

Scoping rule

A name occurrence refers to the *closest surrounding* name declaration.

Announcements Nested declarations Higher-order functions Scope of names

• Hiding can be a useful abstraction technique

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- Recursion is an elegant pattern of problem solving

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- Recursion is an elegant pattern of problem solving
- Functions can be passed to functions
- Functions can be returned from functions
- Higher-order functions are useful for building abstractions
- With nested functions and conditional statements, we need to understand the scope of names



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Concluding Chapter 1

Mental model: substitution model

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- Big ideas: iterative/recursive processes, higher-order, scope

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- Problem solving technique: recursion ("wishful thinking")

- Mental model: substitution model
- Big ideas: iterative/recursive processes, higher-order, scope
- Problem solving technique: recursion ("wishful thinking")
- Look out for Chapter 2: Building Abstractions with Data, starting with L5 tomorrow