DATA ANALYSIS - SCIENTIFIC COMPUTING

Practical Tutorial 3 - Subspace Iteration Methods

Freshman Year, Computer Science Department

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Contents

Face Recognition

Question 01

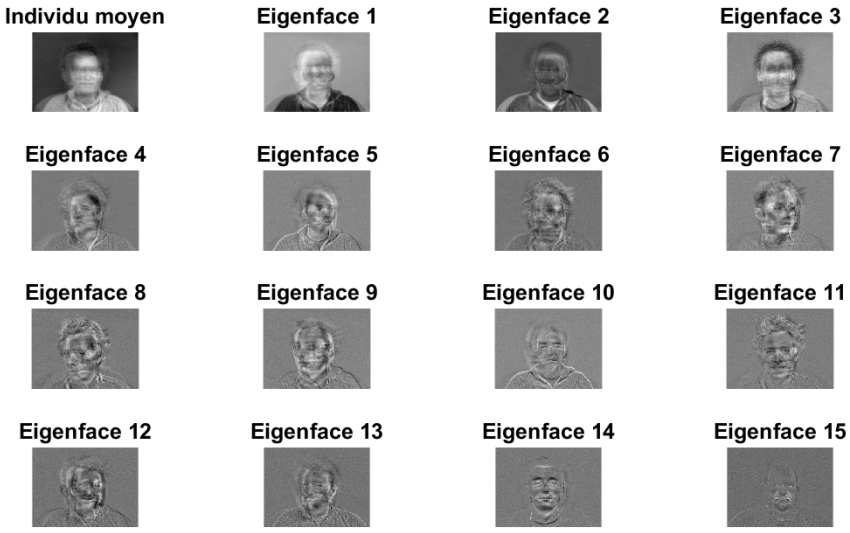


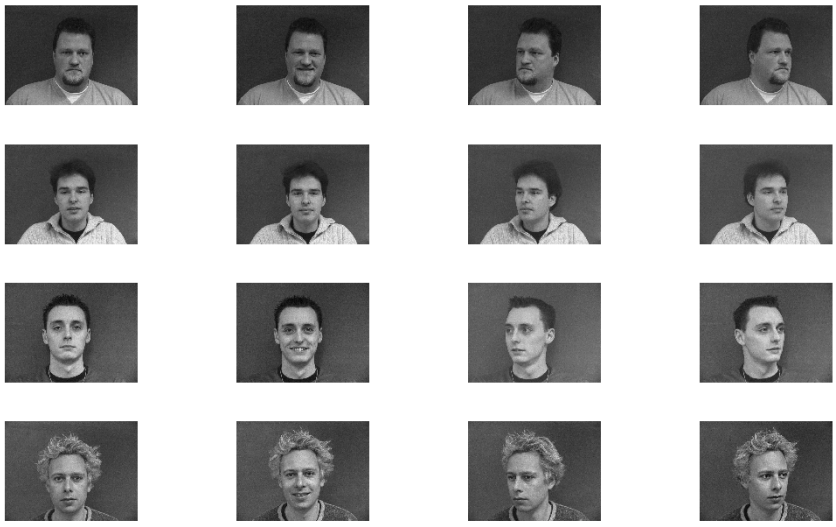
Figure 1.1: Generating Eigenfaces from the the learning images.

These are our principal components from which we will recover our data which is of course the human faces.
These Eigenfaces are the result of centering our vectored images then computing the eigenpairs of $\Sigma_2 = \frac{1}{n} \cdot X_c \cdot X_c^T$ instead of $\Sigma = \frac{1}{n} \cdot X_c^T \cdot X_c$ because of the latter's huge dimensions.
Thankfully, we can extract Σ eigenpairs from Σ_2 through the formula: $X_c^T \cdot Y, \forall\ Y$ eigenvector of Σ_2.

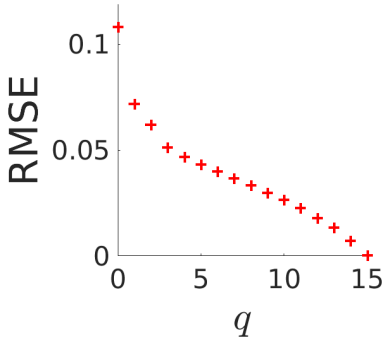
Question 02

(a) 3 Principal Components

(b) 10 Principal Components



(c) 15 Principal Components



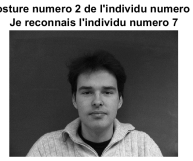
(d) Root Mean Square Error

Figure 1.2: Trying to recover the human faces using a variable number of Principal Components

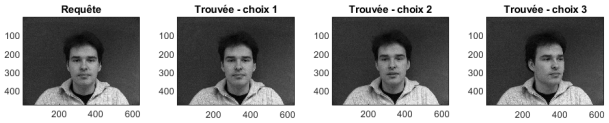
It is quite apparent on *Figure (d)* how the RMSE between the original images and the reconstructed ones

declines rapidly (eventually reaching 0) the more Principal Components we take into consideration, which can also be seen from the satisfying clarity of the images when using 15 Principal Components.

Questions 03 and 04



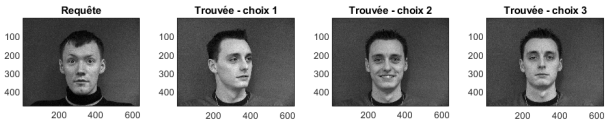
(a) Successful Face Recognition



(b) Detection of other Postures

Figure 1.3: A face from the learning set

(a) Failed Face Recognition



(b) Inability to detect other Postures (Confusion with other faces)

Figure 1.4: A face from the testing set

Figure 1.5: Trying to recognize a set of faces from a set of learning data

The Matlab script for this part tries to implement face recognition using the algorithm of the **k-nearest neighbors**.
This however is not always successful as it succeeds in recognizing faces from the learning set but not from the test set (This will be improved further down). It nonetheless detects the closest faces and postures efficiently as we can clearly see some resemblance even in Figure (d).

Question 05

Algorithm 1 k-Nearest Neighbors

Input: $Data_A$ and $Label_A$, the sets of data and learning labels as well as $Data_T$ the testing set.

1. Let there be $I_{test} \in Data_T$ an image whose k-nearest neighbors we will be searching for.
Compute distances $d(I - I_{test})\ \forall I \in Data_A$
2. Find $I_k \in Data_A$ the k-nearest neighbors to I_{test}
3. Determine the class C most represented amid the k-nearest neighbors of I_{test}
3. Assign class C to I_{test}

Computing the confusion matrix for 100 test leaves much to be desired as all of the faces outside the testing set fail to be recognized. This can be due to the limited number of Principal Components taken into consideration, which is 8 instead of 15, as well as the limited learning set.
The program efficiently detects all faces from the learning set but not those outside it. The small number of face in this set comes in the way of the learning ability of the program.
As such, the error rate extracted from confusion matrix is high: a staggering `87%`. **It is thus apparent that some changes need to be made.**

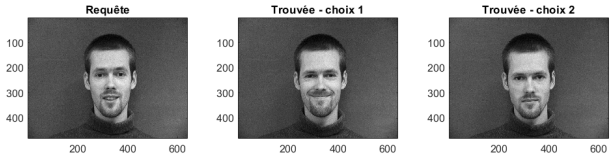
Questions 03 to 05: Changing the learning Data

To associate a test Image to its correct class using k-NN Algorithm, its class should actually be present in the Training Data. That is to say, we can only recognize individual X's face in a posture Y, if there is a posture Z of this individual X in our Training Data already.
As such, what we did is take not only the 4 first postures of individuals 2, 4, 6 and 37 as our Training Data, but the first 2 postures of every single individual: 74 Training Images out of 222 Images in total, which means 33% of Training Data and 67% of Testing Data; a fairly acceptable rate when it comes to k-NN Classification.
Doing this makes sure that our classifier recognizes all present classes from 1 to 37, all that is left is see if it recognize the Testing Data classify them correctly.

See Matlab Script `k_NearestNeighbors.m`

The results are quite satisfying:

(a) Successful Face Recognition



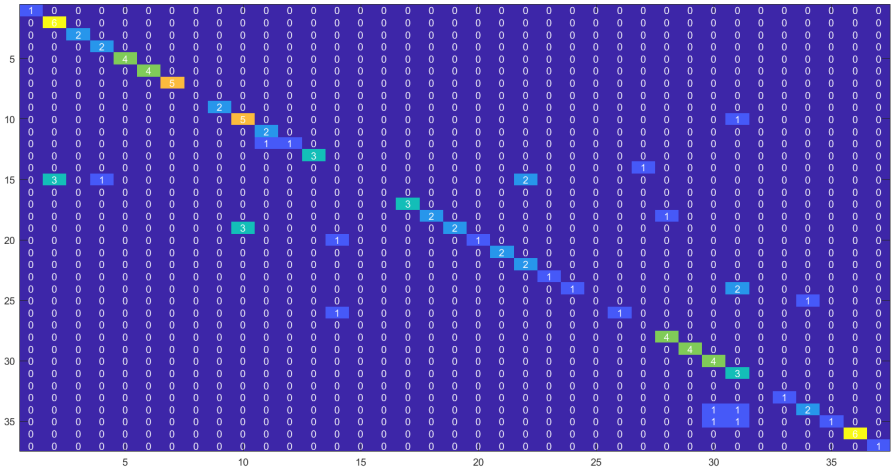
(b) Detection of other Postures of the same face

Figure 1.6: A random face with a random posture selected from the 222 Images

Figure 1.7: Trying to recognize and classify a random face and identify its other postures

See Matlab Script `faceRecognitionWithQuery.m`

As we can see, the randomly selected face is **not present in the Learning Data** because we only took the first *two* postures of each individual.
Nonetheless, the 2-NN classifier associates it to its correct class (34) and we are able to find the 2 closest/nearest postures efficiently.
Like all classifiers, however, there are bound to be some errors; faces which the 2-NN Algorithm could not classify correctly. As such, we ought to test exactly what is the success rate of our program.
It is thus the time now for the confusion matrix: we will be randomly selecting 100 images, classifying them and we'll see how many of them were not classified correctly during the 100 classifications.



(a) Confusion Matrix

Figure 1.8: Confusion Matrix generated from 100 tests

See Matlab Script `faceRecognitionWithConfusionMatrix.m`

As we can see in the figure of the Confusion Matrix above (which is a 37×37 Matrix), our 2-NN classifier *does* make errors but most of the values are on the diagonal of the matrix, that is to say that most of the classifications were correct. To be precise: `78` **classifications out of** `100` were classified properly.
That is an **error rate of** `22%` compared to the earlier `87%`.
This is an all-around satisfying result.

EXTRA: Adding a new set of faces to the database

As a bonus, we tried playing around with the algorithm and see if it could recognize one of our group members' face. He took 6 pictures of himself and added them to the database.
This of course means that the Training Set should include at least one picture of him as well. Just like you can't ask a child to identify some Superman toys if he's never seen Superman, the k-NN Classifier can't identify our teammate if it doesn't have at least some kind of preview of what he looks like, i.e., one of the new 6 images should without question be in the Training Set.
We thus added the first 2 postures to the training set and tested if the classifier would recognize the $\mathbf{6}^{th}$ posture and fulfil the query:

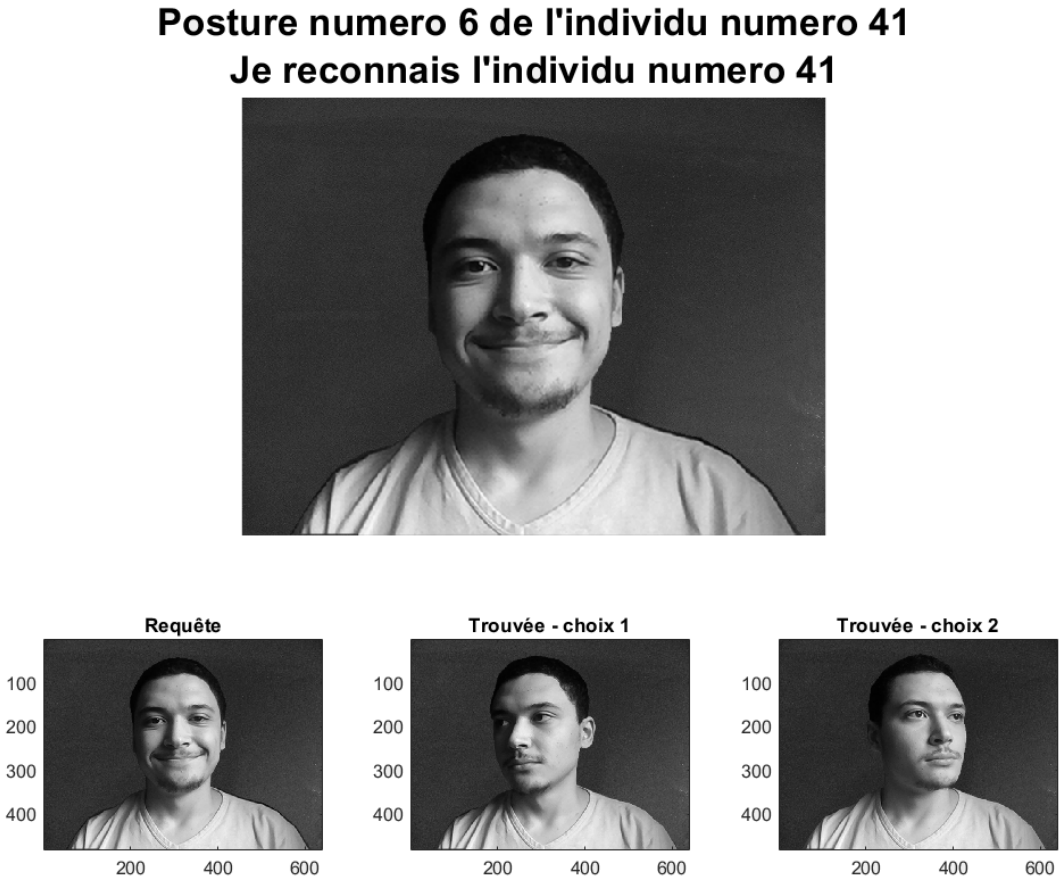


Figure 1.9: Successful Face Recognition of our Team member

As we can see, the 2-NN Classifier successfully recognizes the face in the 6^{th} posture even if it doesn't belong to the Training Set and efficiently finds the other postures. This computation generated

`min(NearestNeighborsDistances) = 15` which isn't too shabby, considering that the class boundaries of our Classifier is `s = 50`.

Question 06 and 07

We have so far used the pre-defined matlab method (eig) to calculate the eigenpairs. We recall that this method reduces the matrix to a symmetric tridiagonal matrix T by an orthogonal similarity transformation and then uses the QR algorithm that effectively factorizes T and computes eigenvalues by bisection and eigenvectors by inverse iteration.

This method is acceptable only when it comes to small dimension matrix , otherwise , it is proved to be very wasteful in storage and computing time when the main matrix is large and sparse . Therefore , we always look for an alternative algorithm which is the subspace iteration , which is provided to find a small subset of eigenvalues and their corresponding eigenvectors.

In our concrete case, we recall that instead of focusing on the matrix $\Sigma = \frac{1}{n} \cdot X_c^T \cdot X_c$ we prefer to focus on $\Sigma_2 = \frac{1}{n} \cdot X_c \cdot X_c^T$ and conclude the eigenparis from it becasue Σ_2 takes as a dimension (n, n) where n is the number of the individuals in our data set. So we can say that the matlab eig method has a reasonable running and storage time because $n = 37$ in our case which is a very small number and using the subspace iteration method wouldn't optimize it that much.

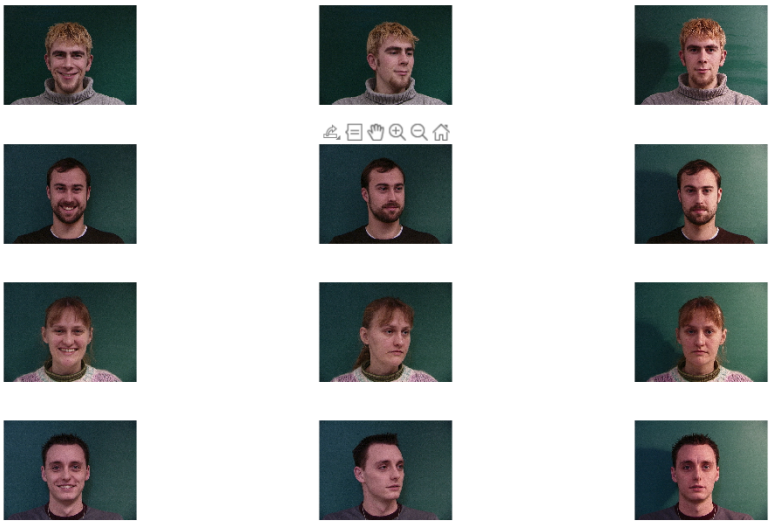
However, if we were to study a data set where we have an enormous amount of individuals (dozens of millions for example) , the eig method wouldn't be working at all , we will have the same problem that we had first when $p = 307200$ was a very large dimension of the matrix Σ except that this time , even our alternative solution which is focusing on Σ_2 wouldn't work because the dimension n goes past millions! Therefore , it would be necessary and mandatory to use the subspace iteration method.

Question 08

Colored Images Reconstruction with Eigenfaces and PCA:

It would be much nicer for us if we could recognize the faces using colored images due to the clarity that they can offer to our process. However, many questions should be asked about its cost and accuracy. Our new set of data will use from now on colored images: Adding the color factor to the matrix is basically making it three-dimensionnal $(480 \times 640 \times RGB)$, therefore it takes more resources to handle as the matrix contains more data associated to every picture . If we were to ask whether or not the we can extract the eigenfaces even from colored pictures to reconstruct the images, the following figures answer that question:

(a) Reconstruction of colored images with the first 5 Principal Components



(a) Full reconstruction of the colored images using 11 Principal Components

Figure 1.11: Reconstruction of Colored Images from the Principal Components of the Learning Set and Eigenfaces

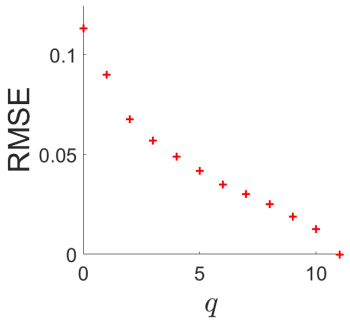


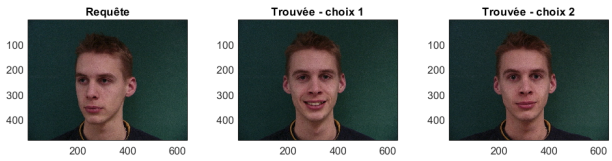
Figure 1.12: Root Mean Square Error with Colored Images

As we can see, the images get fully reconstructed using the Eigenfaces and principal components by the time we use **only 11 Principal Components** while we needed 15 of them to fully reconstruct images without colors.

Face Recognition of Colored Images:

Now we should start asking further questions about the efficiency of adding colors to our images set. The first one to come to mind is : does this make us recognize the inviduals better or in a more accurate way ?

(a) Successful Face Recognition with Color

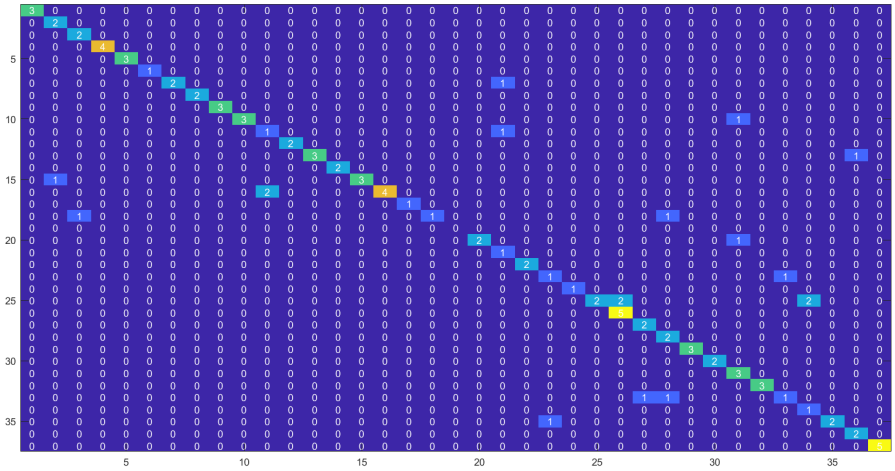


(b) Detection of other Colored Postures of the same face

Figure 1.13: Trying to recognize and classify a random Colored face and identify its other postures

See Matlab Script `ColorFaceRecognitionWithQuery.m`

As we can see, the face recognition is done successfully even with colors. Actually, you may have noticed that in the *old* confusion matrix, this individual is number 14 (17 - 3) in the matrix and was always mistaken for someone else and the recognition of this particular individual failed as a result.
This means that the recognition of this individual was successful thanks to adding colors. Which begs the question: what is the error rate of face recognition with colors and the corresponding confusion matrix?



(a) Confusion Matrix

Figure 1.14: Confusion Matrix generated from 100 tests WITH COLORS

See Matlab Script `ColorFaceRecognitionWithConfusionMatrix.m`

We can see that the confusion matrix extracted from the script using colored training data set has more elements in its diagonal than the confusion matrix without colors. We can deduce from this that adding colors, while computionally expensive, adds more criteria that the classifier uses to tell the difference between different people. The error rate we got from 100 tests is an **error rate of `18%`**, which is lower than the one we obtained with colorless images. That is to say, the recognition failed only 18 times out of 100.

Annex

2.1 Question 01 Script

```
clear;
close all;

taille_ecran = get(0,'ScreenSize');
L = taille_ecran(3);
H = taille_ecran(4);
load donnees;
figure('Name','Individu moyen et eigenfaces','Position',[0,0,0.67*L,0.67*H]);

% Calcul de l'individu moyen :
individu_moyen = mean(X,1);

% Centrage des donnees :
X_c = X - individu_moyen;

% Calcul de la matrice Sigma_2 (de taille n x n) [voir Annexe 1 pour la nature de Sigma_2] :
Sigma_2 = X_c * X_c' * 1/size(X_c,1);

% Calcul des vecteurs/valeurs propres de la matrice Sigma_2 :
[W_2, D_2] = eig(Sigma_2);

% Tri par ordre decroissant des valeurs propres de Sigma_2 :
[D_2_sorted, indexes] = sort(diag(D_2), 'descend');

% Tri des vecteurs propres de Sigma_2 dans le meme ordre :
W_2_sorted = W_2(:, indexes);

% Elimination du dernier vecteur propre de Sigma_2 :
W_2_sorted = W_2_sorted( : , 1 : end - 1);

% Vecteurs propres de Sigma (deduits de ceux de Sigma_2) :
W = transpose(X_c) * W_2_sorted;

% Normalisation des vecteurs propres de Sigma
% [les vecteurs propres de Sigma_2 sont normalises
% mais le calcul qui donne W, les vecteurs propres de Sigma,
% leur fait perdre cette propriete] :
for k =1: n-1
    W(:,k) = W(:,k)/norm(W(:,k));
end

%Affichage de l'individu moyen et des eigenfaces sous forme d'images :
colormap gray;
img = reshape(individu_moyen,nb_lignes,nb_colonnes);
subplot(nb_individus,nb_postures,1);
imagesc(img);
axis image;
```

```
axis off;
title('Individu moyen','FontSize',15);
for k = 1:n-1
  img = reshape(W(:,k),nb_lignes,nb_colonnes);
  subplot(nb_individus,nb_postures,k+1);
  imagesc(img);
  axis image;
  axis off;
  title(['Eigenface ',num2str(k)],'FontSize',15);
end

save exercice_1;
```

2.2 Question 02 Script

```
clear;
close all;
load exercice_1;
h = figure('Position',[0,0,0.67*L,0.67*H]);
figure('Name','RMSE en fonction du nombre de composantes principales','Position',[0.67*L
    ,0,0.33*L,0.3*L]);

% Calcul de la RMSE entre images originales et images reconstruites :
RMSE_max = 0;

% Composantes principales des donnees d'apprentissage
C = X_c * W;

for q = 0:n-1
    qPC = C( : , 1:q ); % q premieres composantes principales
    qEF = W( : , 1:q );   % q premieres eigenfaces
    X_reconstruit = qPC * qEF' + individu_moyen;
    figure(1);
    set(h,'Name',['Utilisation des ' num2str(q) ' premieres composantes principales']);
    colormap gray;
    hold off;
    for k = 1:n
        subplot(nb_individus,nb_postures,k);
        img = reshape(X_reconstruit(k, : ), nb_lignes, nb_colonnes);
        imagesc(img);
        hold on;
        axis image;
        axis off;
    end

    figure(2);
    hold on;
    RMSE = sqrt(mean(mean((X_reconstruit - X).^2)));
    RMSE_max = max(RMSE,RMSE_max);
    plot(q,RMSE,'r+','MarkerSize',8,'LineWidth',2);
    axis([0 n-1 0 1.1*RMSE_max]);
    set(gca,'FontSize',20);
    hx = xlabel('$q$','FontSize',30);
    set(hx,'Interpreter','Latex');
    ylabel('RMSE','FontSize',30);

    pause(0.01);
end
```

2.3 k-NN Algorithm

```
%--------------------------------------------------------------------------
% ENSEEIHT - 1SN - Analyse de donnees
% PROJET Analyse de Données - Calcul Scientifique
% Auteurs : Younes SAOUDI, Issam HABIBI et Hamza MOUDDENE
% fonction kppv.m
%--------------------------------------------------------------------------
function [Partition, voisins, distances] = kppv(DataA,DataT,labelA,labelT,K,ListeClass,
    Nt_test)

    [Na,~] = size(DataA);
    [Nt,~] = size(DataT);
    Partition = zeros(Nt_test,1);

    for i = 1:Nt_test

        distances = vecnorm( ((ones(Na, 1) * DataT(i, :)) - DataA)' )';
        [~, indices] = sort(distances);
        voisins = indices(1:K);
        labels = labelA(voisins);
        compte = histc(labels, ListeClass);
        [valeurMax, indiceClasse] = max(compte);
        if length(find(compte == valeurMax)) > 1
            classe = labelA(voisins(1));
        else
            classe = ListeClass(indiceClasse);
        end
        Partition(i) = classe;

    end
end
```

2.4 Face Recognition Script

```
%-------------------------------------------------------------------------
% ENSEEIHT - 1SN - Analyse de donnees
% PROJET Analyse de Données - Calcul Scientifique
% Auteurs : Younes SAOUDI, Issam HABIBI et Hamza MOUDDENE
%-------------------------------------------------------------------------
clear;
close all;
load donnees;
load exercice_1;

s = 50;

%Tirage d'une image aléatoire
individu = randi(37);
posture = randi(6);
chemin = './Images_Projet_2020';
fichier = [chemin '/' num2str(individu+3) '-' num2str(posture) '.jpg'];
Im=importdata(fichier);
I=rgb2gray(Im);
I=im2double(I);
image_test=I(:)';

% Affichage de l'image de test :
colormap gray;
imagesc(I);
axis image;
axis off;

% Nombre N de composantes principales a prendre en compte
% [dans un second temps, N peut etre calcule pour atteindre le pourcentage
% d'information avec N valeurs propres] :
N = 8;

% Composantes principales des donnees d'apprentissage
C = X_c * W;

% N premieres composantes principales des images d'apprentissage :
N_CP_Appr = C( : , 1:N );

% N premieres composantes principales des images de test :
image_test_c = image_test - individu_moyen;
C_test = image_test_c * W;
N_CP_test = C_test( : , 1:N );

% Determination des images d'apprentissage les plus proches (plus proches voisins) :
ListeClasse = 1:37;         %Les classes présentes dans la base d'Images

train_labels = repmat(numeros_individus, nb_postures, 1);
train_labels = train_labels(:); %Les classes d'apprentissage

k = 2; %Nombre de voisins plus proches que l'on cherche.

[Partition, kppv, Distances] = kppv(N_CP_Appr, N_CP_test, train_labels, individu, k,
    ListeClasse, 1);

if(min(Distances) < s)
    individu_reconnu = Partition; % le n° de l'indiv reconnu est celui dont la classe est la
     plus présente
    title({['Posture numero ' num2str(posture) ' de l''individu numero ' num2str(individu+3)
    ];...
        ['Je reconnais l''individu numero ' num2str(individu_reconnu+3)]},'FontSize',20);
else
```

```
     title({['Posture numero ' num2str(posture) ' de l''individu numero ' num2str(individu+3)];...
         'Je ne reconnais pas cet individu !'},'FontSize',20);
end

%Trouver les résultats de la requête
postures = mod(kppv, nb_postures).';
postures(postures == 0) = nb_postures;
test_labels = train_labels(kppv);
recognitionMatrix = [test_labels postures'];

%Affichage de l'image requête
figure('Name',"FIGURE - Résultat d'une requête sur une base de visages",'Position',[0.2*L,0.2*H,0.6*L,0.5*H]);
subplot(1, k + 1, 1);
colormap gray;
imagesc(I);
axis image;
title("Requête");

%Affichage du résultat de la requête
for i = 1:k
    subplot(1, k+1, i+1);
    fichier = [chemin '/' num2str(recognitionMatrix(i, 1) + 3) '-' num2str(recognitionMatrix(i, 2) ) '.jpg'];
    Im = importdata(fichier);
    I = rgb2gray(Im);
    I = im2double(I);
    imagesc(I);
    axis image;
    title("Trouvée - choix " + i);
end
```

2.5 Confusion Matrix of Face Recognition Script

```
%-------------------------------------------------------------------------
% ENSEEIHT - 1SN - Analyse de donnees
% PROJET Analyse de Données - Calcul Scientifique
% Auteurs : Younes SAOUDI, Issam HABIBI et Hamza MOUDDENE
%-------------------------------------------------------------------------
clear;
close all;
load donnees;
load exercice_1;

% Tirage aleatoire de nbrTests images de test :
nbrTests = 100;
individus_aleatoires = zeros(nbrTests,1);
images_test = zeros(nbrTests, size(X,2));

for i=1:nbrTests
    individu = randi(37);
    posture = randi(6);
    individus_aleatoires(i) = individu;
    chemin = './Images_Projet_2020';
    fichier = [chemin '/' num2str(individu+3) '-' num2str(posture) '.jpg'];
    Im=importdata(fichier);
    I=rgb2gray(Im);
    I=im2double(I);
    image_test=I(:)';
    images_test(i,:) = image_test;
end

% Nombre N de composantes principales a prendre en compte
% [dans un second temps, N peut etre calcule pour atteindre le pourcentage
% d'information avec N valeurs propres] :
N = 8;

% Composantes principales des donnees d'apprentissage
C = X_c * W;

% N premieres composantes principales des images d'apprentissage :
N_CP_Appr = C( : , 1:N );

% N premieres composantes principales des images de test :
images_test_c = images_test - individu_moyen;
C_test = images_test_c * W;
N_CP_test = C_test( : , 1:N );

% Determination des images d'apprentissage les plus proches (plus proches voisins) :
ListeClasse = 1:37;         %Les classes présentes dans la base d'Images

train_labels = repmat(numeros_individus, nb_postures, 1);
train_labels = train_labels(:); %Les classes d'apprentissage

%Nombre de voisins plus proches
k = 2;
[Partition, kppv, ~] = kppv(N_CP_Appr, N_CP_test, train_labels, individus_aleatoires, k,
    ListeClasse, nbrTests);

individu_reconnu = Partition; % le n° des indiv reconnus sont ceux dont la classe est la
    plus présente

confusion_matrix = zeros(37);
for i = 1:nbrTests
    confusion_matrix(individus_aleatoires(i), individu_reconnu(i)) = confusion_matrix(
    individus_aleatoires(i), individu_reconnu(i))+1;
```

```
60 end
61
62 errorRate = (nbrTests - sum(diag(confusion_matrix))) / nbrTests * 100
```

2.6 Exercise 1 with Colors

```
clear;
close all;

taille_ecran = get(0,'ScreenSize');
L = taille_ecran(3);
H = taille_ecran(4);
load donneesCouleur;
figure('Name','Individu moyen et eigenfaces','Position',[0,0,0.67*L,0.67*H]);

% Calcul de l'individu moyen :
individu_moyen = mean(X,1);

% Centrage des donnees :
X_c = X - individu_moyen;

% Calcul de la matrice Sigma_2 (de taille n x n) [voir Annexe 1 pour la nature de Sigma_2] :
Sigma_2 = X_c * X_c' * 1/size(X_c,1);

% Calcul des vecteurs/valeurs propres de la matrice Sigma_2 :
[W_2, D_2] = eig(Sigma_2);

% Tri par ordre decroissant des valeurs propres de Sigma_2 :
[D_2_sorted, indexes] = sort(diag(D_2), 'descend');

% Tri des vecteurs propres de Sigma_2 dans le meme ordre :
W_2_sorted = W_2(:, indexes);

% Elimination du dernier vecteur propre de Sigma_2 :
W_2_sorted = W_2_sorted( : , 1 : end - 1);

% Vecteurs propres de Sigma (deduits de ceux de Sigma_2) :
W = transpose(X_c) * W_2_sorted;

% Normalisation des vecteurs propres de Sigma
% [les vecteurs propres de Sigma_2 sont normalisés
% mais le calcul qui donne W, les vecteurs propres de Sigma,
% leur fait perdre cette propriété] :
for k =1: n-1
    W(:,k) = W(:,k)/norm(W(:,k));
end

%Affichage de l'individu moyen et des eigenfaces sous forme d'images :
colormap gray;
img = reshape(individu_moyen,nb_lignes,nb_colonnes,3);
subplot(min(8, nb_individus), nb_postures,1);
imagesc(img);
axis image;
axis off;
title('Individu moyen','FontSize',15);
for k = 1:min(15, n-1)
  img = reshape(W( : , k ), nb_lignes, nb_colonnes, 3);
  subplot(min(8,nb_individus), nb_postures, k+1);
  imagesc(img);
  axis image;
  axis off;
  title(['Eigenface ',num2str(k)],'FontSize',15);
end

save ColorExercise1;
```

2.7 Exercise 2 with Colors

```
clear;
close all;
load ColorExercise1;
h = figure('Position',[0,0,0.67*L,0.67*H]);
figure('Name','RMSE en fonction du nombre de composantes principales','Position',[0.67*L
    ,0,0.33*L,0.3*L]);

% Calcul de la RMSE entre images originales et images reconstruites :
RMSE_max = 0;

% Composantes principales des donnees d'apprentissage
C = X_c * W;

for q = 0:n-1
    qPC = C( : , 1:q ); % q premieres composantes principales
    qEF = W( : , 1:q );   % q premieres eigenfaces
    X_reconstruit = qPC * qEF' + individu_moyen;
    figure(1);
    set(h,'Name',['Utilisation des ' num2str(q) ' premieres composantes principales']);
    colormap gray;
    hold off;
    for k = 1:n
        subplot(nb_individus,nb_postures,k);
        img = reshape(X_reconstruit(k, : ), nb_lignes, nb_colonnes,3);
        imagesc(img);
        hold on;
        axis image;
        axis off;
    end

    figure(2);
    hold on;
    RMSE = sqrt(mean(mean((X_reconstruit - X).^2)));
    RMSE_max = max(RMSE,RMSE_max);
    plot(q,RMSE,'r+','MarkerSize',8,'LineWidth',2);
    axis([0 n-1 0 1.1*RMSE_max]);
    set(gca,'FontSize',20);
    hx = xlabel('$q$','FontSize',30);
    set(hx,'Interpreter','Latex');
    ylabel('RMSE','FontSize',30);

    pause(0.01);
end
```

2.8 Face Recognition and Query with Colors

```
%-------------------------------------------------------------------------
% ENSEEIHT - 1SN - Analyse de donnees
% PROJET Analyse de Données - Calcul Scientifique
% Auteurs : Younes SAOUDI, Issam HABIBI et Hamza MOUDDENE
%-------------------------------------------------------------------------
clear;
close all;
load donneesCouleur;
load ColorExercise1;

s = 100;

%Tirage d'une image aléatoire
individu = 14;
posture = randi(6);
chemin = './Images_Projet_2020';
fichier = [chemin '/' num2str(individu+3) '-' num2str(posture) '.jpg'];
Im=importdata(fichier);
I=im2double(Im);
r=I(:,:,1);
v=I(:,:,2);
b=I(:,:,3);
image_test=[r(:)',v(:)',b(:)'];

% Affichage de l'image de test :
imagesc(I);
axis image;
axis off;

% Nombre N de composantes principales a prendre en compte
% [dans un second temps, N peut etre calcule pour atteindre le pourcentage
% d'information avec N valeurs propres] :
N = 8;

% Composantes principales des donnees d'apprentissage
C = X_c * W;

% N premieres composantes principales des images d'apprentissage :
N_CP_Appr = C( : , 1:N );

% N premieres composantes principales des images de test :
image_test_c = image_test - individu_moyen;
C_test = image_test_c * W;
N_CP_test = C_test( : , 1:N );

% Determination des images d'apprentissage les plus proches (plus proches voisins) :
ListeClasse = 1:37;         %Les classes présentes dans la base d'Images

train_labels = repmat(numeros_individus, nb_postures, 1);
train_labels = train_labels(:); %Les classes d'apprentissage

k = 2; %Nombre de voisins plus proches que l'on cherche.

[Partition, kppv, Distances] = kppv(N_CP_Appr, N_CP_test, train_labels, individu, k,
    ListeClasse, 1);

if(min(Distances) < s)
    individu_reconnu = Partition; % le n° de l'indiv reconnu est celui dont la classe est la
     plus présente
    title({['Posture numero ' num2str(posture) ' de l''individu numero ' num2str(individu+3)
    ];...
        ['Je reconnais l''individu numero ' num2str(individu_reconnu+3)]},'FontSize',20);
```

```
else
    title({['Posture numero ' num2str(posture) ' de l''individu numero ' num2str(individu+3)
    ];...
        'Je ne reconnais pas cet individu !'},'FontSize',20);
end

%Trouver les résultats de la requête
postures = mod(kppv, nb_postures).';
postures(postures == 0) = nb_postures;
test_labels = train_labels(kppv);
recognitionMatrix = [test_labels postures'];

%Affichage de l'image requête
figure('Name',"FIGURE - Résultat d'une requête sur une base de visages",'Position',[0.2*L
    ,0.2*H,0.6*L,0.5*H]);
subplot(1, k + 1, 1);
colormap gray;
imagesc(I);
axis image;
title("Requête");

%Affichage du résultat de la requête
for i = 1:k
    subplot(1, k+1, i+1);
    fichier = [chemin '/' num2str(recognitionMatrix(i, 1) + 3) '-' num2str(
    recognitionMatrix(i, 2) ) '.jpg'];
    Im = importdata(fichier);
    I=im2double(Im);
    r=I(:,:,1);
    v=I(:,:,2);
    b=I(:,:,3);
    result=[r(:)',v(:)',b(:)'];
    result = reshape(result, nb_lignes, nb_colonnes, 3);
    imagesc(result);
    axis image;
    title("Trouvée - choix " + i);
    result= [];
end
```

2.9 Confusion Matrix with Colors

```
%-------------------------------------------------------------------------
% ENSEEIHT - 1SN - Analyse de donnees
% PROJET Analyse de Données - Calcul Scientifique
% Auteurs : Younes SAOUDI, Issam HABIBI et Hamza MOUDDENE
%-------------------------------------------------------------------------
clear;
close all;
load donneesCouleur;
load ColorExercise1;

% Tirage aleatoire de nbrTests images de test :
nbrTests = 100;
individus_aleatoires = zeros(nbrTests,1);
images_test = zeros(nbrTests, size(X,2));

for i=1:nbrTests
    individu = randi(37);
    posture = randi(6);
    individus_aleatoires(i) = individu;
    chemin = './Images_Projet_2020';
    fichier = [chemin '/' num2str(individu+3) '-' num2str(posture) '.jpg'];
    Im=importdata(fichier);
    I=im2double(Im);
    r=I(:,:,1);
    v=I(:,:,2);
    b=I(:,:,3);
    image_test=[r(:)',v(:)',b(:)'];
    images_test(i,:) = image_test;
end

% Nombre N de composantes principales a prendre en compte
% [dans un second temps, N peut etre calcule pour atteindre le pourcentage
% d'information avec N valeurs propres] :
N = 8;

% Composantes principales des donnees d'apprentissage
C = X_c * W;

% N premieres composantes principales des images d'apprentissage :
N_CP_Appr = C( : , 1:N );

% N premieres composantes principales des images de test :
images_test_c = images_test - individu_moyen;
C_test = images_test_c * W;
N_CP_test = C_test( : , 1:N );

% Determination des images d'apprentissage les plus proches (plus proches voisins) :
ListeClasse = 1:37;         %Les classes présentes dans la base d'Images

train_labels = repmat(numeros_individus, nb_postures, 1);
train_labels = train_labels(:); %Les classes d'apprentissage

%Nombre de voisins plus proches
k = 2;
[Partition, kppv, ~] = kppv(N_CP_Appr, N_CP_test, train_labels, individus_aleatoires, k,
    ListeClasse, nbrTests);

individu_reconnu = Partition; % le n° des indiv reconnus sont ceux dont la classe est la
    plus présente

confusion_matrix = zeros(37);
for i = 1:nbrTests
```

```
61      confusion_matrix(individus_aleatoires(i), individu_reconnu(i)) = confusion_matrix(
        individus_aleatoires(i), individu_reconnu(i))+1;
62  end
63
64  errorRate = (nbrTests - sum(diag(confusion_matrix))) / nbrTests * 100
```