

# Artistic Style Transfer

**Saifuddin Syed**

**MLRG Fall 2016**

# Outline

## 1 Introduction

## 2 Review of CNN

- VGG Network

## 3 The Gatys et al Construction

- Content Representation
- Style Representation
- Image Construction
- Examples

## 4 Alternative Methods

- MRF Construction
- Examples

## 5 AST For video

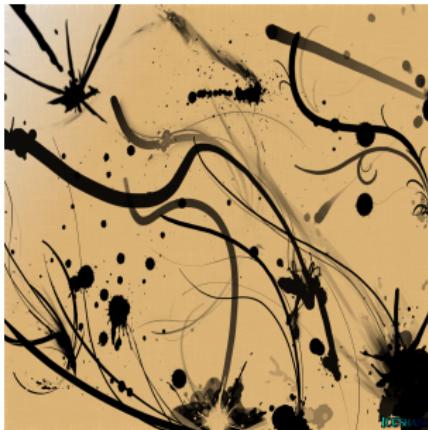
- Example

# Introduction

Suppose I give you a piece of art and a photo. I ask you to recreate the photo in the style of the art. How would one go about doing it?

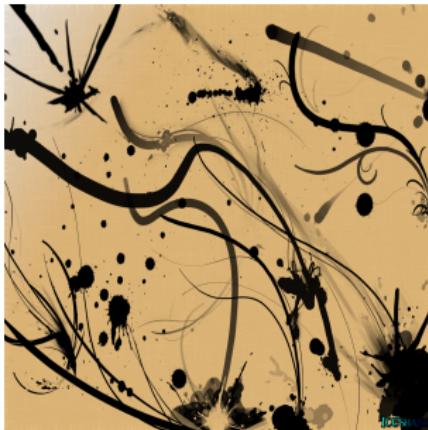
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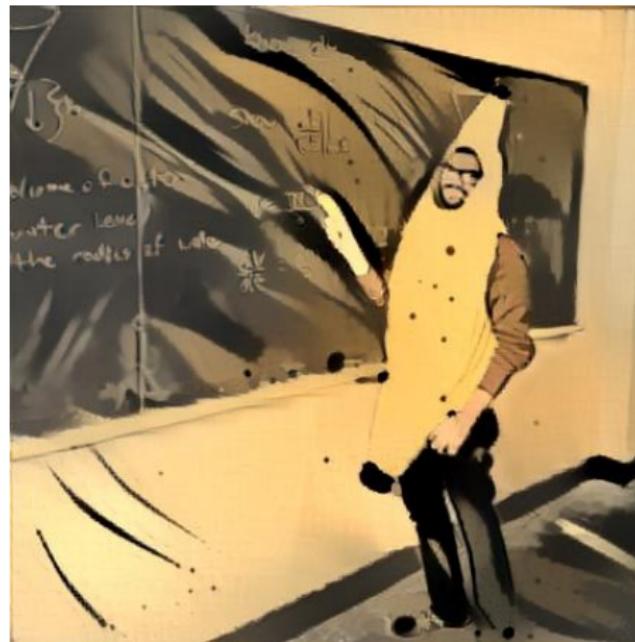
# Introduction

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This is a very difficult task for humans, even talented ones.

Our goal is to teach a computer to do exactly this.



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We input an image and each layer applies a set of filters that identify local features in the network.

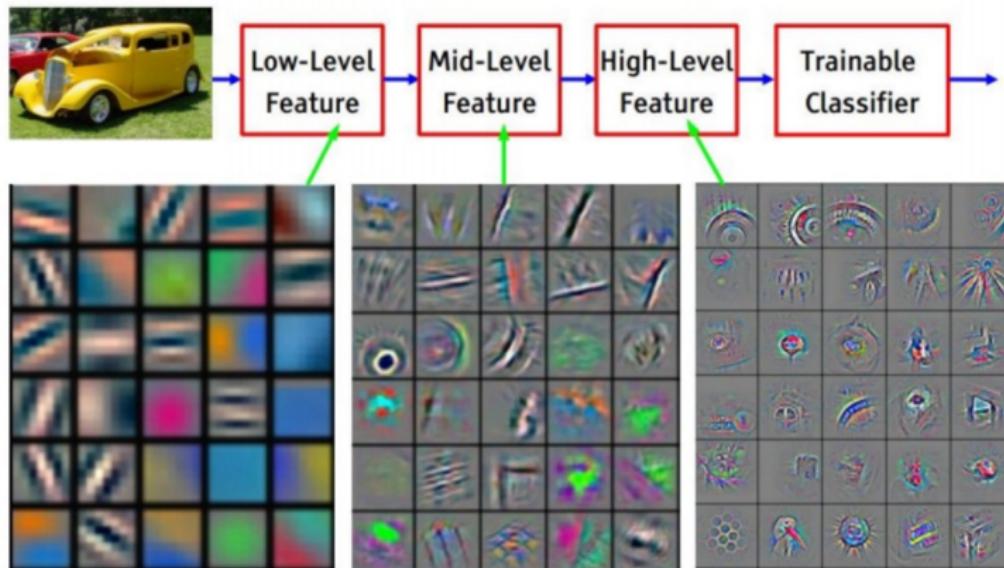
# CNN Overview

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We input an image and each layer applies a set of filters that identify local features in the network.

Typically the deeper we go in the network, high level content is identified as opposed to just pixel values.

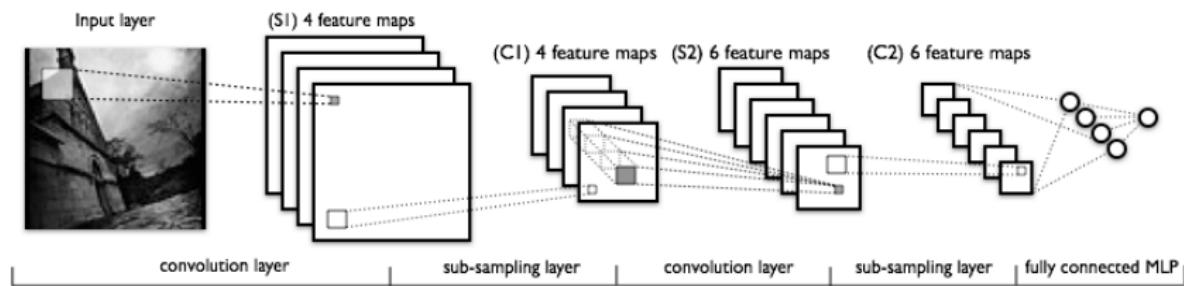
# CNN Overview



Feature visualization of convolutional net trained on ImageNet from [Zeiler & Fergus 2013]

# Feature Maps

Suppose layer  $l$  of the network has  $N_l$  filters, we will refer the collection of filtered images the **feature maps** at layer  $l$ .



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Properties of VGG.

- Won ImageNet with a 7.3% top 5 error rate.
- Only 3x3 Conv stride 1, pad 1
- 2x2 MAX POOL stride 2
- 140 Million parameters

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The key finding of this paper is that the representations of “content” and “style” in the Convolutional Neural Network are separable.

We will make precise what we mean by style and content, but first, let us set up the problem formally.

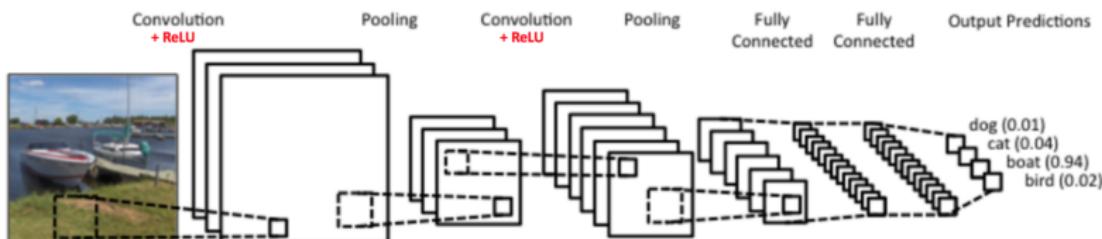
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Our aim is to construct an image  $x$  with the content of image  $p$  in the style of image  $a$ .

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We suppose that in our network, layer  $l$  has  $N_l$  filters, each with spatial dimension  $M_l$  (the product of its width and height).



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The feature maps extracted by the network from the original image  $\mathbf{p}$ , the style image  $\mathbf{a}$  and the stylized image  $\mathbf{x}$  we denote by  $\mathbf{P}^l$ ,  $\mathbf{S}^l$ , and  $\mathbf{F}^l$  respectively.

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The dimensionality of these feature maps is  $N_l \times M_l$ .

## Content Representation

Each layer aims to learn a different aspect of the image content. It is reasonable to assume that two images with similar content should have similar feature maps at each layer.

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We will say  $x$  matches the content of  $p$  at layer  $l$ , if their feature responses at layer  $l$  of the network are the same.

## Content Loss

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We define the content loss at layer  $l$  to be,

$$\begin{aligned}\mathcal{L}_c^l(\mathbf{x}, \mathbf{p}) &= \frac{1}{2N_l M_l} \|\Phi^l(\mathbf{x}) - \Phi^l(\mathbf{p})\|_2^2 \\ &= \frac{1}{2N_l M_l} \sum_{i,j} |F_{ij}^l - P_{ij}^l|^2\end{aligned}$$

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We define our content reconstruction  $\mathbf{x}_c^l$  to be

$$\mathbf{x}_c^l = \operatorname{argmin}_{\mathbf{x}} \mathcal{L}_c^l(\mathbf{x}, \mathbf{p})$$

## Content Loss

We have  $\mathcal{L}_c^I$  satisfies

$$\frac{\partial \mathcal{L}_c^I}{\partial F_{ij}^I} = \begin{cases} (\mathbf{F}^I - \mathbf{P}^I)_{ij} & F_{ij}^I > 0 \\ 0 & F_{ij}^I < 0 \end{cases}$$

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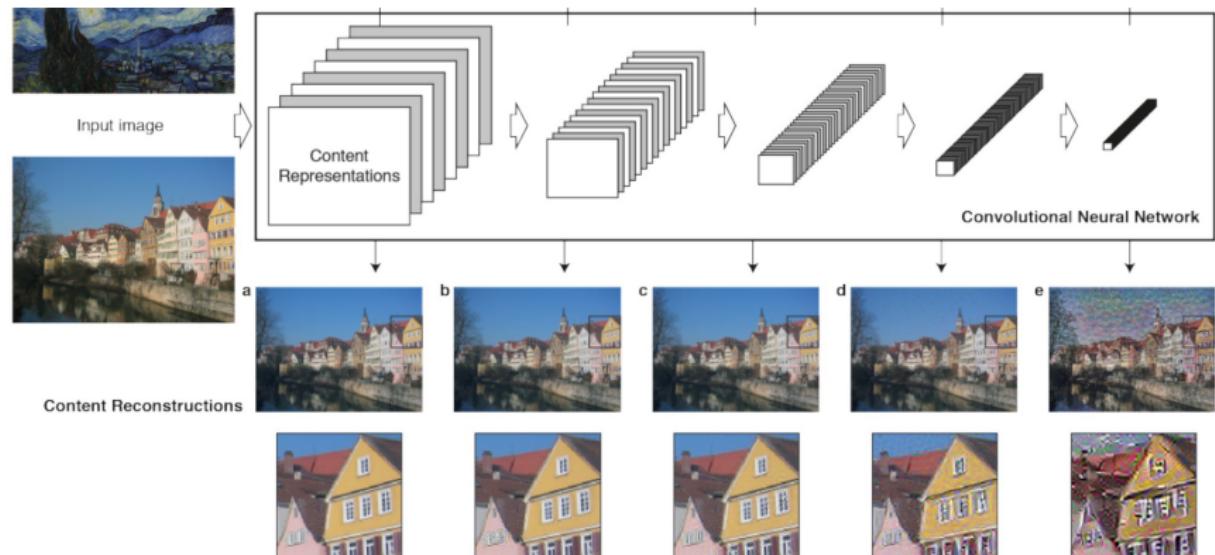
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Normally  $\mathbf{x}$  is initialized as a Gaussian white noise.

# Content Reconstruction



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## Content Reconstruction

Higher layers in the network capture the high-level content in terms of objects and their arrangement in the input image but do not constrain the exact pixel values of the reconstruction.

In contrast, reconstructions from the lower layers simply reproduce the exact pixel values of the original image.

The feature responses in higher layers better encode the content of the image.

## Style Representation

The feature responses of an image  $\mathbf{a}$  at layer  $l$  encode the content, however to determine style we are less interested in any individual feature of our image but rather how they all relate to each other.

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This was the main insight of Gatys, et al.

## Style Representation

We will encode the correlations of the feature maps into the Graham Matrices,

$$A_{ij}^l = \mathbf{S}_{i\bullet}^l \cdot \mathbf{S}_{j\bullet}^l = \sum_{k=1}^{M_l} S_{ik}^l S_{jk}^l$$

$$G_{ij}^l = \mathbf{F}_{i\bullet}^l \cdot \mathbf{F}_{j\bullet}^l = \sum_{k=1}^{M_l} F_{ik}^l F_{jk}^l$$

$\mathbf{A}^l$  and  $\mathbf{G}^l$  define a  $N_l \times N_l$  dimension matrix, where  $N_l$  is the number of filters in layer  $l$ .

# Style Loss

We define the style loss at layer  $l$  to be,

$$\begin{aligned}\mathcal{L}_s^l(\mathbf{x}, \mathbf{a}) &= \frac{1}{4N_l^2 M_l^2} \|\mathbf{G}^l - \mathbf{A}^l\|_F^2 \\ &= \frac{1}{4N_l^2 M_l^2} \sum_{i,j} |G_{ij}^l - A_{ij}^l|^2\end{aligned}$$

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We define our style reconstruction  $\mathbf{x}_s^l$  to be

$$\mathbf{x}_s^l = \operatorname{argmin}_{\mathbf{x}} \mathcal{L}_s^l(\mathbf{x}, \mathbf{a})$$

# Style Loss

Similar to the content loss, we have  $\mathcal{L}_s^I$  satisfies

$$\frac{\partial \mathcal{L}_s^I}{\partial F_{ij}^I} = \begin{cases} \frac{1}{N_i^2 M_i^2} ((\mathbf{F}^I)^T (\mathbf{G}^I - \mathbf{A}^I))_{ij} & \mathbf{F}_{ij}^I > 0 \\ 0 & \mathbf{F}_{ij}^I < 0 \end{cases}$$

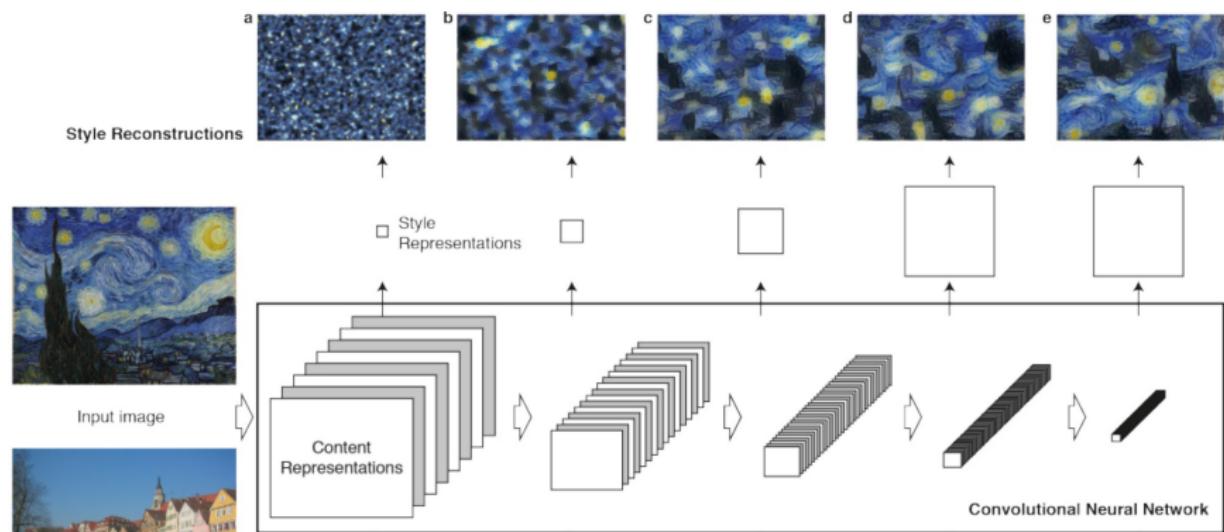
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We can use back propagation and descent methods to iteratively minimize  $\mathcal{L}_s^I$  and learn  $\mathbf{x}_s^I$

# Style Reconstruction



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Note the size and complexity of local image structures from the input image increases along the hierarchy.

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Heuristically, the higher layers learn more complex features than lower layers, and produce a more detailed style representation.

# Image Construction

We now want to combine the content and style constructions outlined previously to develop an image  $x$  which simultaneously tries to match the content of  $p$  with the style of  $a$ .

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We will define our content (style) loss as the weighted average of the style (content) loss at each layer.

$$\mathcal{L}_c(\mathbf{x}, \mathbf{p}) = \sum_I \alpha^I \mathcal{L}_c^I(\mathbf{x}, \mathbf{p})$$

$$\mathcal{L}_s(\mathbf{x}, \mathbf{a}) = \sum_I \beta^I \mathcal{L}_s^I(\mathbf{x}, \mathbf{p})$$

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Often we take the  $\alpha^I = 0$  for low  $I$ , and  $\beta^I = 1$ .

# Image Construction

To match the content we need to minimize  $\mathcal{L}_c$  and to match the style we need to minimize  $\mathcal{L}_s$ . Therefore we will minimize both simultaneously by minimizing

$$\mathcal{L}(\mathbf{x}, \mathbf{p}, \mathbf{a}) = \alpha \mathcal{L}_c(\mathbf{x}, \mathbf{p}) + \beta \mathcal{L}_s(\mathbf{x}, \mathbf{a}).$$

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If  $\frac{\alpha}{\beta}$  is high, we favour matching the content more than the style.

If  $\frac{\alpha}{\beta}$  is low, we favour matching the style more than the content.

## Artistic Style Transfer

### └ The Gatys et al Construction

#### └ Image Construction

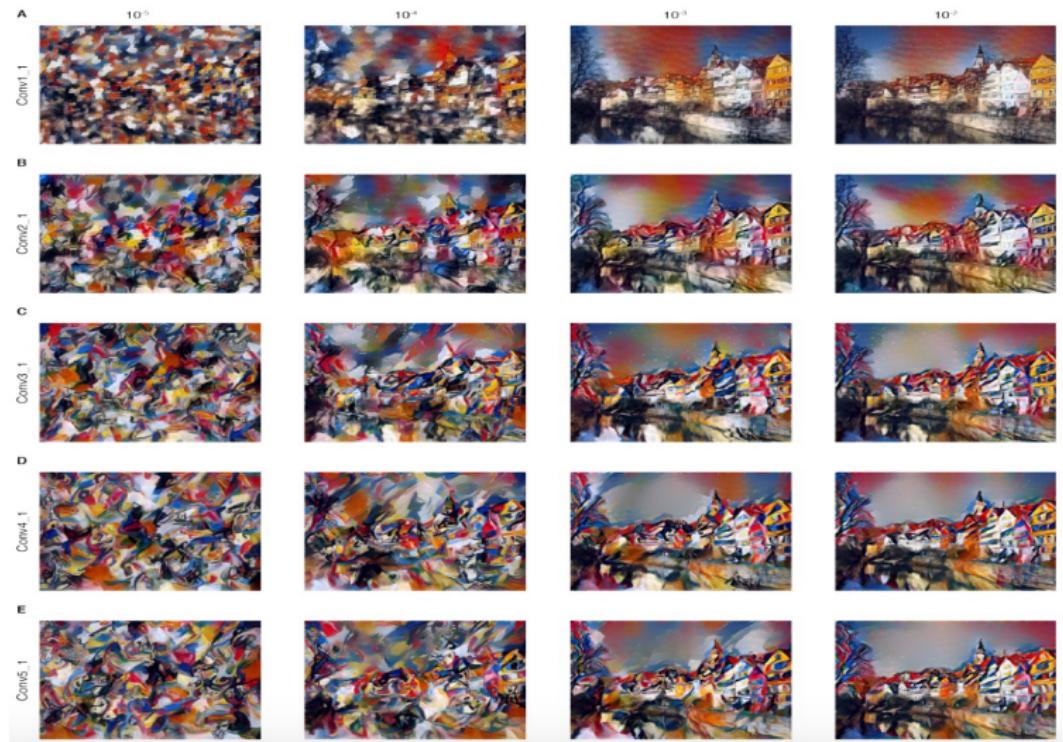


Figure: Columns:  $\frac{\alpha}{\beta}$ . Row: Layer of network



# Examples



**Figure:** **Left:** Neckarfront in Tübingen, Germany, **B:** *The Shipwreck of the Minotaur* by J.M.W. Turner, 1805

# Examples



**Figure:** **Left:** Neckarfront in Tübingen, Germany, **C:** *The Starry Night* by Vincent van Gogh, 1889

# Examples



**Figure:** Left: Neckarfront in Tübingen, Germany, D: *Der Schrei* by Edvard Munch, 1893

## Examples



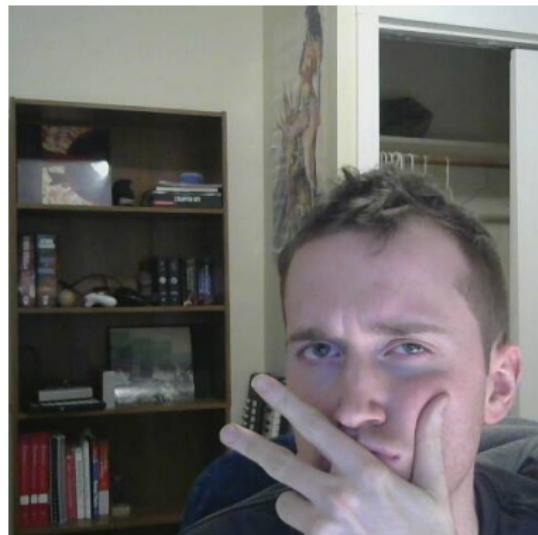
**Figure:** **L**eft: Neckarfront in Tübingen, Germany, **E**: *Femme nue assise* by Pablo Picasso, 1910

## Examples



**Figure:** **L**eft: Neckarfront in Tübingen, Germany, **F**: *Composition VII* by Wassily Kandinsky, 1913

## Examples



**Figure:** **Left:** My friend Grant, **Right:** Grant as a pizza

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- “Perceptual Losses for Real-Time Style Transfer and Super-Resolution” (Johnson, et al, Mar 2016)
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Following Gatys, et al. Li and Wand, tried to match the content and style simultaneously by trying to minimize a linear combination of content and style loss function in addition to a regularizer.

$$\mathcal{L}^{MRF}(\mathbf{x}, \mathbf{p}, \mathbf{a}) = \alpha \mathcal{L}_c(\mathbf{x}, \mathbf{p}) + \beta \tilde{\mathcal{L}}_s(\mathbf{x}, \mathbf{a}) + \lambda R(\mathbf{x})$$

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Where  $\mathcal{L}_c$  is the same content loss function used in the Gatys construction.

## Style Loss

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The patches are of dimension  $k \times k \times N_l$ , where  $k$  is the width and height of the patch (typically  $k$  is small) and  $N_l$  is the number of filters in layer  $l$ .

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The patches are of dimension  $k \times k \times N_l$ , where  $k$  is the width and height of the patch (typically  $k$  is small) and  $N_l$  is the number of filters in layer  $l$ .

Our goal will be to match patches of  $\Phi^l(\mathbf{x})$  to  $\Phi^l(\mathbf{a})$  in some layer  $l$ .

# Style Loss

Let  $\Psi(\Phi^l(\mathbf{x})) = \{\Psi_i(\Phi^l(\mathbf{x}))\}_{i=1}^{m_l}$  be an ordered list of all local patches extracted from  $\Phi^l(\mathbf{x})$ .

# Style Loss

Let  $\Psi(\Phi'(\mathbf{x})) = \{\Psi_i(\Phi'(\mathbf{x}))\}_{i=1}^{m_1}$  be an ordered list of all local patches extracted from  $\Phi'(\mathbf{x})$ .

Given  $i$ , we define  $NN(i)$  to be the position of the patch in  $\Psi(\Phi'(\mathbf{a}))$  that deviates the most from  $\Psi_i(\Phi'(\mathbf{x}))$ . I.e.

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$$NN(i) = \operatorname{argmin}_j \frac{\Psi_i(\Phi'(\mathbf{x})) \cdot \Psi_j(\Phi'(\mathbf{a}))}{|\Psi_i(\Phi'(\mathbf{x}))| \cdot |\Psi_j(\Phi'(\mathbf{a}))|}$$

So we define  $\tilde{\mathcal{L}}_s$  to be

$$\tilde{\mathcal{L}}_s(\mathbf{x}, \mathbf{a}) = \sum_{i=1}^{m_l} \|\Psi_i(\Phi'(\mathbf{x})) - \Psi_{NN(i)}(\Phi'(\mathbf{a}))\|^2$$

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We defining the discrete gradient of  $\mathbf{x}$  as

$$\Delta \mathbf{x}_{i,j} = (x_{i+1,j} - x_{i,j}, x_{i,j+1} - x_{i,j}).$$

There is smoothness in the image when  $\|\Delta \mathbf{x}\|_2^2$  is small, so we let

$$R(\mathbf{x}) = \|\Delta \mathbf{x}\|_2^2 = \sum_{i,j} (x_{i+1,j} - x_{i,j})^2 + (x_{i,j+1} - x_{i,j})^2$$

# Examples



Input A



Input B



Content A + Style B



Content B + Style A

# Examples



Content Image

Gatys et al

Ours

# Examples



Input style



Input content



Gatys et al



Ours

# Examples



# Examples

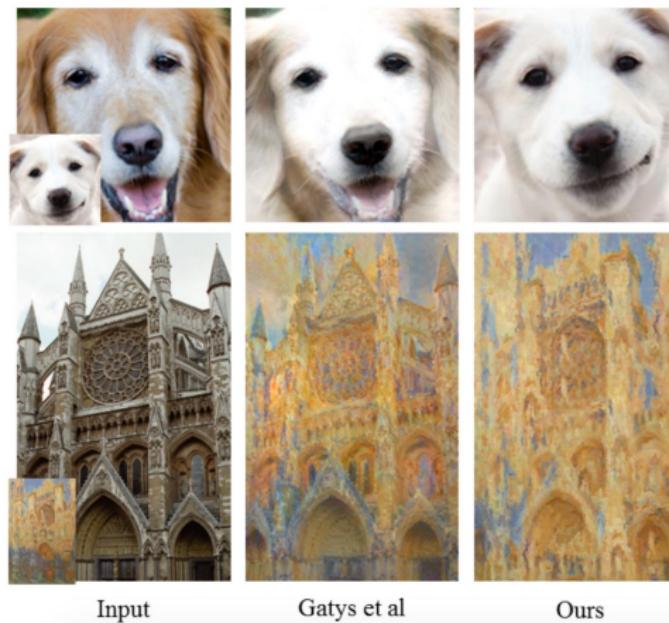


Figure: Example of Gatys, et al performing better

# Outline

## 1 Introduction

## 2 Review of CNN

- VGG Network

## 3 The Gatys et al Construction

- Content Representation
- Style Representation
- Image Construction
- Examples

## 4 Alternative Methods

- MRF Construction
- Examples

## 5 AST For video

- Example

# Artistic Style Transfer for Video

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The two main issues we will have to deal with is the initialization of the optimization procedure and the temporal consistency between frames.

# Notation

We use the following notation: Let  $\mathbf{p}$  be the content video with frames  $\mathbf{p}^i$ , and  $\mathbf{a}$  be the style image. We want to create a video  $\mathbf{x}$  such that each frame  $\mathbf{x}^i$  has the content of  $\mathbf{p}^i$  and style  $\mathbf{a}$ .

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Our goal will be to determine  $\mathbf{x}^i$  in chronological order. We will also denote  $\mathbf{x}_0^i$  to be the initialization of in the optimization procedure to determine  $\mathbf{x}^i$ .

## Naive Method

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The next natural step would be to initialize the optimization procedure by  $\mathbf{x}_0^i = \mathbf{x}^{i-1}$ .

If there is motion in the scene, this simple approach does not perform well since moving objects are initialized incorrectly.

## Optical Flow to the rescue

The **optical flow** in a the content video  $\mathbf{p}$  between frame  $j$  to  $i$  (denoted by  $w_j^i$ ) is a function that warps a given image  $\mathbf{p}^j$  using the optical flow field that was estimated between frame  $\mathbf{p}^j$  and  $\mathbf{p}^i$ .

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Intuitively, it can be thought of as a function that predicts frame  $i$  in  $\mathbf{p}$  given frame  $j$ . I.e.

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Given the optical flow of  $w_{i-1}^i$  between frame  $\mathbf{p}^{i-1}$  and  $\mathbf{p}^i$  of the content video, we can initialize  $\mathbf{x}_0^i$  via

$$\mathbf{x}_0^i = w_{i-1}^i(\mathbf{x}^{i-1}).$$

## Temporal consistency

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We define the temporal loss to be

$$\mathcal{L}_{temp}(\mathbf{x}, \mathbf{w}, \mathbf{c}) = \frac{1}{D} \sum_{k=1}^D c_k (x_k - w_k)^2$$

Where  $D$  is the dimension of the image. And  $c_k = 0$  if the motion at pixel  $w_k$  is a boundary point, and 1 otherwise.  $\mathbf{c}^i$  can be approximated using optical flow. For details of this procedure see Arxiv 1604.08610.

# Temporal Consistency

To force some consistency between consecutive frames, we can minimize

$$\begin{aligned}\mathcal{L}_{short}(\mathbf{x}^i, \mathbf{p}^i, \mathbf{a}) = & \alpha \mathcal{L}_c(\mathbf{x}^i, \mathbf{p}^i) + \beta \mathcal{L}_s(\mathbf{x}^i, \mathbf{a}) \\ & + \gamma \mathcal{L}_{temp}(\mathbf{x}^i, w_{i-1}^i(\mathbf{x}^{i-1}), \mathbf{c}^i)\end{aligned}$$

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To get a smoother result, it is better to achieve some long term consistency between not just the previous frame, but rather the previous  $J$  frames (typically  $J = 1, 2, 4$ ).

$$\begin{aligned}\mathcal{L}_{long}(\mathbf{x}^i, \mathbf{p}^i, \mathbf{a}) = & \alpha \mathcal{L}_c(\mathbf{x}^i, \mathbf{p}^i) + \beta \mathcal{L}_s(\mathbf{x}^i, \mathbf{a}) \\ & + \gamma \sum_{j=1}^J \mathcal{L}_{temp}(\mathbf{x}^i, w_{i-j}^i(\mathbf{x}^{i-j}), \mathbf{c}^{i-j})\end{aligned}$$

# Example

See <https://www.youtube.com/watch?v=Khuj4ASIdmU>