

Problem Chosen
ABCDEF

2025
MCM/ICM
Summary Sheet

Team Control Number
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The MCM Thesis of Team 12345678

Summary

This is a summary.

Keywords: keyword1, keyword2, keyword3

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1 Introduction

1.1 Problem Background

Wordle, developed by Jonathan Feinberg in 2008, was created to help students expand their vocabulary. However, due to its simple gameplay, it quickly went viral on social media at the end of 2021 and was later acquired by The New York Times in 2022, integrating it into their online games section. It is a web-based game with two difficulty modes: easy and hard. It focuses on user experience and game logic, and there are many variations of the game, such as Quordle (guessing 4 words simultaneously), Octordle (guessing 8 words simultaneously), and Worldle (a geography version where players guess a country or region). The rules for the hard mode are as follows.

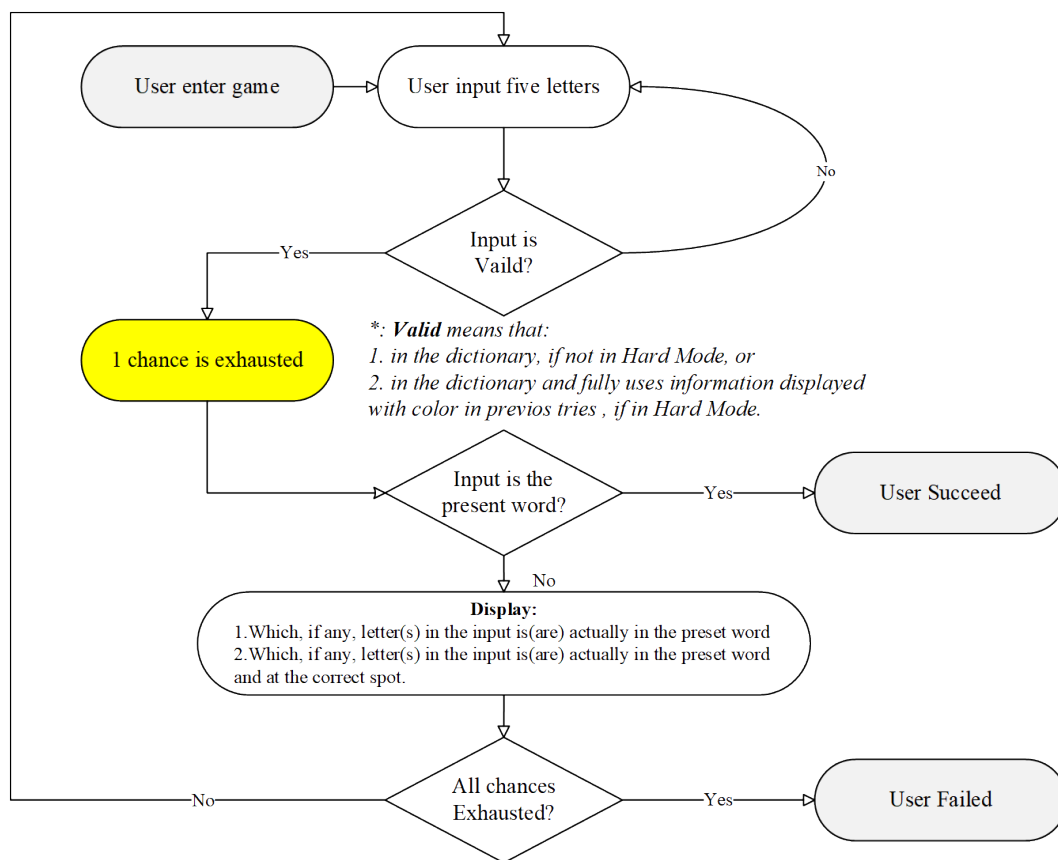


Figure 1: Game Rules

1.2 Restatement of the Problem

We need to analyze the data provided by The New York Times and address the following tasks:

- **Problem 1:** Develop a model to explain the variations in the daily reported results and predict the range of reported results for March 1, 2023. Additionally, analyze which word attributes influence players' decisions to select Hard Mode.

- **Problem 2:** Build a prediction model to estimate the percentage distribution of results (1, 2, 3, 4, 5, 6, X) for a future day, with specific predictions for "EERIE" on March 1, 2023, and assess the model's accuracy.
- **Problem 3:** Develop a classification model to categorize words by difficulty level and identify their attributes. Conduct a detailed analysis for "EERIE" and evaluate the model's accuracy.
- **Problem 4:** Explore and describe any other interesting insights or patterns found within the data.

1.3 Our Work

2 Assumptions and Notations

2.1 Assumptions

2.2 Notations

Symbol	Decription
f_t	forget gate
i_t	input gate
o_t	output gate
h_t	hidden state
c_t	cell state
x_t	LSTM's input
$W_{f,i,c,o}$	Bias
$b_{f,i,c,o}$	Weight Matrix

3 Model 1-Prediction Model based on LSTM

By analyzing *Problem_C_Data_Wordle.xlsx*, we found that the Wordle data is collected and analyzed daily. By analyzing this data, we can clearly see that the results of Wordle change over time and exhibit time dependence. Therefore, we chose the LSTM algorithm, which is specifically designed to capture and utilize long-term dependencies in sequential data. This fits well with the time-varying Wordle results presented in the problem. We ultimately used this algorithm to simulate the data for March 1, 2023.

3.1 Description of LSTM

LSTM is a neural network structure that can effectively capture long-term dependencies in time series data. By introducing gating mechanisms, it can selectively retain and forget information, solving the vanishing and exploding gradient problems inherent in radial RNNs. Although LSTM is computationally expensive, it performs excellently in many tasks, especially in processing sequential data. Its main features are the memory

cell and gating mechanisms, which introduce three gates: the forget gate, input gate, and output gate, allowing for selective retention or discarding of data. Its update equations are as follows.

$$\begin{aligned}
 f_t &= \sigma(W_f \cdot [h_{t-1}, x_t] + b_f) \\
 i_t &= \sigma(W_i \cdot [h_{t-1}, x_t] + b_i) \\
 o_t &= \sigma(W_o \cdot [h_{t-1}, x_t] + b_o) \\
 \tilde{c}_t &= \tanh(W_c \cdot [h_{t-1}, x_t] + b_c) \\
 c_t &= f_t \cdot c_{t-1} + i_t \cdot \tilde{c}_t \\
 h_t &= o_t \cdot \tanh(c_t)
 \end{aligned} \tag{1}$$

3.2 Prediction on March 1,2023

3.2.1 Data settings

Machine learning algorithms are very sensitive to the input data values. To prevent certain results (e.g., Christmas 2022) from being significantly smaller or larger than other features, which could cause biases in the algorithm's processing of data, we applied a formula to temporarily scale all data to the range [0, 1] to facilitate computation. The formula is as follows (Formula 7).

$$x_{scaled} = \frac{x - \min(x)}{\max(x) - \min(x)} \tag{2}$$

We then divided the given data into training and test sets. After analyzing the data, we found that the results of Wordle generally showed a decreasing trend. When the proportion of the training set was not particularly large (7:3 or even 8:2), due to the lack of early and late results, the final predicted result would be much higher or lower than the actual data from December 31, 2022. Therefore, we chose a 9:1 data split. We also decided to use data from the previous month (30 days) to predict the results. It is well known that during statutory holidays, the statistics may significantly drop because people need to spend time with family and friends. According to website data¹, in high-GDP countries, there are about 12 statutory holidays a year on average, which means that there is almost always one holiday per month. Therefore, using the previous 30 days of data would almost cover a holiday, leading to results that better reflect the actual situation. Finally, we used the formula below (Formula 8) for inverse normalization to restore the data to its original form.

$$x_{original} = x_{scaled} \times (\max(x) - \min(x)) + \min(x) \tag{3}$$

3.2.2 Results on March 1,2023

After setting the parameters, we ran the model. Since the data for March 1 is about 60 days after December 31, we first used data from October 1 to December 31 (about 90 days) for preliminary fitting to observe the model's prediction results. The specific data is shown in Figures 2.

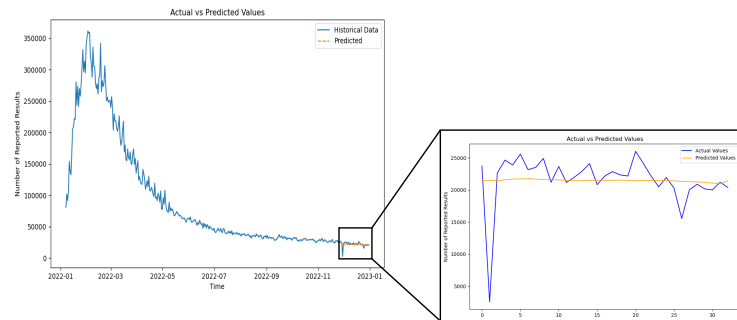


Figure 2: Actual vs Predicted Values

We found that the results of this fitting had a good correlation with the actual values, so we also used the model to predict the next 90 days. The results are shown in Figure 3.

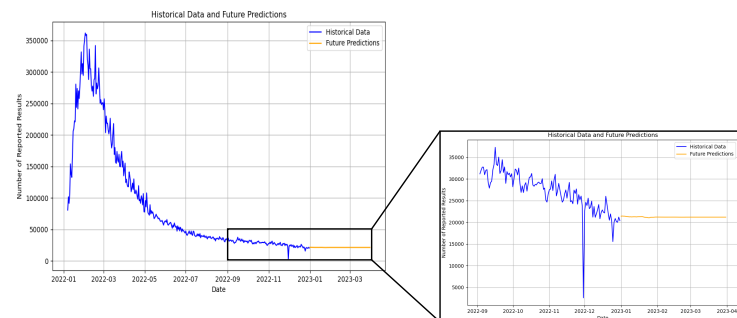


Figure 3: Historical Data and Future Predictions

We also tracked the changes in training loss and validation loss over time. As the number of iterations increased, the training loss gradually decreased, indicating that our model was increasingly fitting the training data and learning the underlying patterns. Eventually, it stabilized around 2model had converged and reached an optimal point. To prevent overfitting, we also closely monitored the changes in validation loss. Initially, we observed that the validation loss increased during the early iterations, likely due to the model adapting to the training data. However, after four iterations, it started to decrease, showing signs of generalization. By the 10th iteration, the validation loss had also stabilized, indicating that the model was no longer overfitting. We took the error value at

the 10th iteration as the final result, and the data plot is shown in Figure 4, reflecting the training dynamics throughout the process.

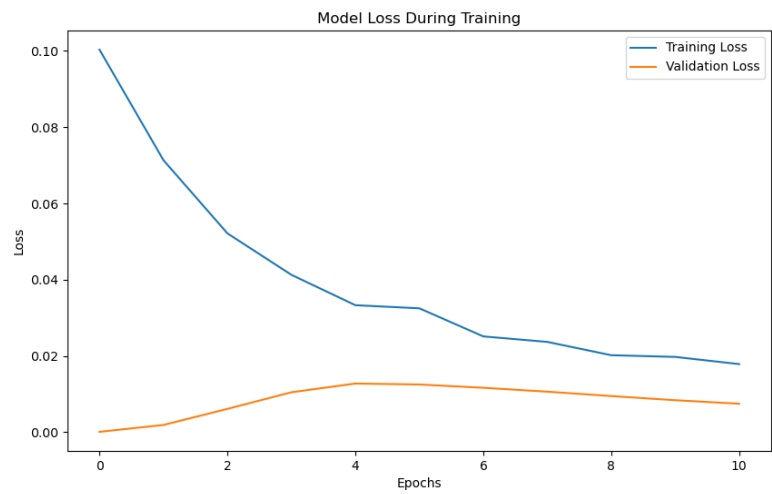


Figure 4: Model Loss During Training

Based on our model, the predicted range for the number of reported results on March 1, 2023, is:

$$x_{March1,2023} = 21137 \pm 2.01425\% \tag{4}$$

3.3 Relationship of Word Attributes and Scores from Percentage

4 Model 2

5 Model 3

6 Interesting Findings

7 Sensitivity Analysis

8 Model Assessment

8.1 Strengths

8.2 Weaknesses

9 Letter

$$E = mc^2 \tag{5}$$

$$E = mc^2$$

- This is a item.
- This is a item.
- This is a assumption.
- This is a assumption.
- This is a assumption.
- This is a assumption.

I love math.

I love math.

I love math.

References

[1] <https://holidays-calendar.net/>

Appendices

MEMORANDUM

To: MCM office

From: MCM Team 12345678

Subject: MCM

Date: January 13, 2025

This is a memorandum.

Appendix A First appendix

Here are simulation programmes we used in our model as follow.

MATLAB source code:

Appendix B Second appendix

Python source code: