

Cats have Tails

1 Search Problem

We run a search from each of the three terms in the query fact. That is, for each of a_1, r, a_2 , we create a search problem as defined below. The paths from the result of these searches are used as features in the learning problem (see Section 2).

We define the problem by specifying the state space, the valid transitions, along with the weights of the transitions. The algorithm used is a Uniform Cost Search, leading to the additional challenge of ensuring that the cost of each transition is very fast – that is, on the order of microseconds to keep pace with the memory accesses for the search.

Before delving into the search problem, we define the notion of a **node**. A node is, at a high level, a phrase such as one which would correspond to an argument or a relation. It is:

- Case sensitive, but normalized to be either capitalized, all capitals, or all lowercase.
- Lemmatized and normalized where appropriate. For instance, *has* and *had* are the same node. In particular, the ReVerb normalized relation is used.
- In the case when the phrase maps exactly to a word form in WordNet, it is the WordNet synset.

The definition of the search problem is:

State A state is a tuple of the *current* node, as well as the node that the search directly came from; and, whether the query fact has been following a valid series of steps for natural logic entailment. The state space is thus squared with respect to the size of the vocabulary, and is utterly impractical to enumerate directly.

We can denote a state as (n_{-1}, n) .

Transitions A valid transition is one between states (n_{-1}, n) and (n, n_{+1}) , such that in relation to n, n_{+1} is one of:

- **Add/Remove a closed class word**. This is a class of transitions denoted by $ins(w)$ or $del(w)$ where w is the word being added or removed. For example, transitioning from *cat* to *a cat* or *every cat* or visa versa.

- **Add/Remove an adjective.** Similar to above, but with adjectives. These are distinguished from the above in that they have meaning for natural logic entailment.
- **WordNet hypernymy.** This is a class of transitions denoted by $hyper(n)$ or $hypo(n)$, where n denotes the number of levels up or down the tree we are jumping. For example, we could transition from *cat* to *feline* or to *animal*
- **WordNet relations.** This is a class of transitions related to the other WordNet relations (e.g., antonymy), primarily to capture some of the inferences in natlog.
- **Freebase relations.** This is a class of transitions aimed primarily for proper nouns, traversing Freebase relations. These are denoted by $freebase(r)$, where r denotes the freebase relation we have traversed. For example, *Barack Obama* could transition to *USA* via the *employee_of* relation.
- **ReVerb relation.** As in the Freebase case, we can move along a ReVerb relation, denoted as $reverb(r)$.
- **Acronym and de-acronym.** Expanding or creating an acronym, denoted by *acronym* and *deacronym*.
- **Nearest neighbor similarity.** The fallback is to search for nearest neighbors in similarity space. This is, roughly, the equivalent of the CoNLL paper.

Weights The weight of a transition from (n_{-1}, n) to (n, n_{+1}) is given by appealing to the transitions between n_{-1} and n , and between n and n_{+1} .

We denote the type of transition (e.g., $ins(w)$ or $freebase(r)$) between n_{-1} and n to be ϕ_{-1} , and the type of transition between n and n_{+1} to be ϕ_0 . For both of these, we define weights $w_{\phi_{-1}}$ and w_{ϕ_0} , as well as a weight for the bigram of the two: w_{ϕ_{-1}, ϕ_0} . Lastly, we incur a cost for exiting the domain of natural logic entailments: w_{nle} . Our cost is thus given by:

$$\text{cost} = -w_{\phi_0} - w_{\phi_{-1}, \phi_0} - \mathbb{1}(\text{broke entailment}) \cdot w_{nle} \quad (1)$$

We constrain $w_{\phi} \leq 0$ to ensure that the cost is always positive.

Note, furthermore, that this is a natural decomposition of a log-linear model where ϕ denote features and w denote the weights of the features. The cost of a path will become:

$$\sum_i \text{cost}_i = - \sum_i [w_{\phi_i} + w_{\phi_{i-1}, \phi_i}] \quad (2)$$

If we exponentiate the negative of this, we arrive at:

$$\exp(\sum_i cost_i) = \exp\left(\sum_i [w_{\phi_i} + w_{\phi_{i-1}, \phi_i}]\right) \quad (3)$$

Over two classes: *true* and *false*; and, defining notation where ϕ denotes the vector of active path types taken and w denotes the global weight vector, we arrive at our log-linear model:

$$P(true) \propto e^{w^T \phi} \quad (4)$$

This decomposition is important, as it allows our search to get smarter along with our learning algorithm, and allows us to find better support for facts as we learn what patterns entail “good” support.

Start State The start state is the relevant word from the fact we are beginning from, normalized to a valid node (i.e., lemmatized, properly cased, etc.). For example, the search from a_1 of *cats have tails* would be *cat*.

Terminal State The terminal state of the search is any node which is attached to a known fact on the correct term. For example, a search from a_1 of *cats have tails* would finish at *dog* if there is a fact in the database such as *dogs have tails*.

2 Learning Problem

The prediction problem is a binary prediction task: is the given fact true or false, given a database of known facts.