

NLP – Ex2

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Or Perel - 200732444

Q1

b. #trigrams: 413540

#bigrams: 122930

#unigrams: 2000

#tokens: 1118296

#perplexity for lambda1(left) lambda2(top) grid search:

	000.000	000.100	000.200	000.300	000.400	000.500	000.600	000.700	000.800	000.900
000.000	189.624	115.665	094.730	082.688	074.630	068.860	064.621	061.564	059.628	059.293
000.100	104.210	082.635	072.622	066.031	061.319	057.858	055.376	053.845	053.720	-01.000
000.200	087.509	071.626	064.313	059.421	055.935	053.475	051.972	051.850	-01.000	-01.000
000.300	079.029	065.420	059.467	055.555	052.887	051.272	051.076	-01.000	-01.000	-01.000
000.400	074.226	061.614	056.499	053.306	051.411	051.057	-01.000	-01.000	-01.000	-01.000
000.500	071.732	059.390	054.885	052.407	051.753	-01.000	-01.000	-01.000	-01.000	-01.000
000.600	071.141	058.488	054.581	053.320	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000
000.700	072.652	059.060	056.248	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000
000.800	077.440	062.138	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000
000.900	090.453	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000	-01.000

#best coefficients (lambda1, lambda2) are (0.4, 0.5) with perplexity 51.0567551405

2. Loss

$$CE(y, \hat{y}) = - \sum_i y_i \log(\hat{y}_i)$$

$$y = (0, \underset{j \rightarrow}{1}, 0) \text{ and } (k$$

$$i \neq j \text{ or } y_i = 0 \Rightarrow -\log(\hat{y}_j)$$

$$= -\log(\text{Softmax}(\theta)_j)$$

$$= -\log\left(\frac{\exp(\theta_j)}{\sum_i \exp(\theta_i)}\right)$$

$$= -\log(\exp(\theta_j)) + \log\left(\sum_i \exp(\theta_i)\right)$$

$$= -\theta_j + \log\left(\sum_i \exp(\theta_i)\right)$$

$$\frac{\partial CE(y, \hat{y})}{\partial \theta_j} = -1 + \frac{1}{\sum_i \exp(\theta_i)} \cdot \exp(\theta_j)$$

$$= \frac{\exp(\theta_j)}{\sum_i \exp(\theta_i)} - 1$$

$$= \text{Softmax}(\theta)_j - 1$$

$$\frac{\partial CE(y, \hat{y})}{\partial \theta_k} = \frac{1}{\sum_i \exp(\theta_i)} \cdot \exp(\theta_k)$$

(k ≠ j)

$$= \frac{\exp(\theta_k)}{\sum_i \exp(\theta_i)}$$

$$= \text{Softmax}(\theta)_k$$

$$\boxed{\frac{\partial CE(y, \hat{y})}{\partial \theta} = \hat{y} - y}$$

⇐

100 (?)

$$\theta = h w_2 + b_2$$

$$h = \sigma(z)$$

$$z = x w_1 + b_1$$

chain rule

$$\frac{\partial CE(y, \hat{y})}{\partial x} = \frac{\partial CE(y, \hat{y})}{\partial \theta} \cdot \frac{\partial \theta}{\partial h} \cdot \frac{\partial h}{\partial z} \cdot \frac{\partial z}{\partial x}$$

$$\frac{\partial CE(y, \hat{y})}{\partial \theta} = \hat{y} - y$$

$$\frac{\partial \theta}{\partial h} = w_2^T$$

$$\frac{\partial h}{\partial z} = \sigma(z) (1 - \sigma(z))$$

$$\frac{\partial z}{\partial x} = w_1^T$$

$$\Rightarrow \frac{\partial CE(y, \hat{y})}{\partial x} = [(\hat{y} - y) w_2^T \sigma(z) (1 - \sigma(z))] w_1^T$$

↑
chain rule

d.

#params: 104550

#train examples: 1118296

training took 0 seconds (re-run for evaluation after training)

dev perplexity : 112.967665327

3.5ke

(12)

$$\begin{aligned} E_{p_{drop}} [h_{drop}]_i &= p_{drop} \cdot [\gamma \cdot 0 \cdot h_i] + (1 - p_{drop}) [\gamma \cdot 1 \cdot h_i] \\ &= (1 - p_{drop}) \cdot \gamma \cdot h_i \end{aligned}$$

$$E_{p_{drop}} [h_{drop}]_i = h_i$$

lin 2
: 1051

$$(1 - p_{drop}) \cdot \gamma \cdot h_i = h_i$$

$$\boxed{\gamma = \frac{1}{1 - p_{drop}}}$$

Q3

c.

Perplexity for each epoch:

```
[598.2366782129152, 258.35566638496755, 186.748500751412,  
153.8955940469948, 133.7895546230422, 119.46139157102863,  
109.51243179110595, 101.60273449526015, 95.69344691128141,  
90.6552240888448, 86.34052603632608, 82.98170482530692, 80.04136627427236,  
77.28627441036822, 75.2353598328523, 73.01505584565827, 71.32777081434989,  
69.88417041995659, 68.37327530689748, 67.18151719599369]
```

Finished training

Epoch: 20 Validation Perplexity: 104.119