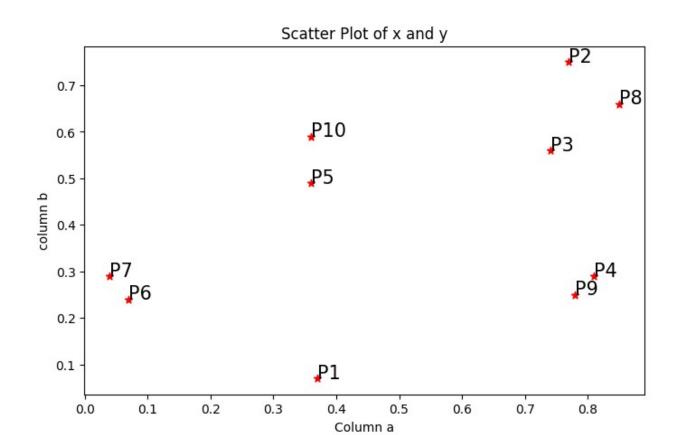
```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import scipy.cluster.hierarchy as shc
from scipy.spatial.distance import squareform, pdist
```

Creating a random dataset with 2 features, a real time dataset is not used because, in hierarchial clustering we need to create n clusters for n points in the start (divisive) or in the end (agglomerative), so the plotting will be very difficult for large no of points. so for learning purpose ive used a random data with 10 points and 2 features

```
a = np.random.random sample(size = 10)
b = np.random.random sample(size = 10)
point = ['P1','P2','P3','P4','P5','P6','P7','P8','P9','P10']
data = pd.DataFrame({'Point':point, 'a':np.round(a,2),
'b':np.round(b,2)})
data = data.set index('Point')
data
         a b
Point
P1
      0.37 0.07
P2
       0.77 0.75
P3
       0.74 0.56
P4
      0.81 0.29
P5
       0.36 0.49
P6
       0.07 0.24
P7
       0.04 0.29
P8
       0.85
           0.66
P9
       0.78 0.25
P10
       0.36 0.59
```

Plotting the points

```
plt.figure(figsize=(8,5))
plt.scatter(data['a'], data['b'], c='r', marker='*')
plt.xlabel('Column a')
plt.ylabel('column b')
plt.title('Scatter Plot of x and y')
for j in data.itertuples():
    plt.annotate(j.Index, (j.a, j.b), fontsize=15)
```



Calculating the distance matrix

<pre>dist = pd.DataFrame(squareform(pdist(data[['a', 'b']]), 'euclidean'), columns=data.index.values, index=data.index.values) dist</pre>						
	P1 P2	P3	P4	P5	P6	
P7 \						
P1 0.0000	90 0.788923	0.614003	0.491935	0.420119	0.344819	
0.396611		0 102254	0 461726	0 405400	0.066000	
P2 0.7889 0.862844	23 0.000000	0.192354	0.461736	0.485489	0.866083	
P3 0.6140	0.192354	0.000000	0.278927	0.386394	0.742496	
0.750267						
P4 0.4919	35 0.461736	0.278927	0.000000	0.492443	0.741687	
0.770000						
P5 0.4201	19 0.485489	0.386394	0.492443	0.000000	0.382884	
0.377359 P6 0.3448	19 0.866083	0.742496	0.741687	0.382884	0.000000	
0.058310	19 0.000003	0.742490	0.741007	0.302004	0.00000	
P7 0.3966	11 0.862844	0.750267	0.770000	0.377359	0.058310	
0.00000						
P8 0.7605	92 0.120416	0.148661	0.372156	0.518652	0.885889	
0.890505						

```
P9
     0.447772 \quad 0.500100 \quad 0.312570 \quad 0.050000 \quad 0.483735 \quad 0.710070
0.741080
P10 0.520096 0.440114 0.381182 0.540833 0.100000 0.454533
0.438634
           P8
                              P10
P1
     0.760592 0.447772 0.520096
P2
     0.120416 0.500100 0.440114
P3
     0.148661 0.312570 0.381182
P4
     0.372156 0.050000 0.540833
P5
     0.518652 0.483735 0.100000
P6
     0.885889 0.710070 0.454533
P7
     0.890505 0.741080 0.438634
P8
     0.000000 0.415933
                         0.494975
P9
     0.415933 0.000000
                         0.540370
P10
     0.494975 0.540370
                         0.000000
```

perform single link clustering method, the shortest distance between 2 clusters is considered when one or both the clusters have 2 or more points

```
def single linkage(dist matrix):
    n = len(dist matrix)
    while n > 1:
        min val = float('inf')
        min index = None
        for i in range(n):
            for j in range(i+1, n):
                if dist matrix.iloc[i, j] < min val and</pre>
dist matrix.index[i] != dist matrix.columns[j]:
                    min val = dist matrix.iloc[i, j]
                    min index = (i, j)
        if min val == float('inf'):
            break
        i, j = min index
        cluster1, cluster2 = dist matrix.index[i],
dist matrix.columns[j]
        print(f'Merging clusters {cluster1} and {cluster2} with
distance {min val}')
        new cluster = f'({cluster1}, {cluster2})'
        dist matrix[new cluster] = dist matrix[[cluster1,
cluster2]].min(axis=1)
        dist matrix.loc[new cluster] = dist matrix.loc[[cluster1,
cluster2]].min(axis=0)
        dist_matrix = dist_matrix.drop([cluster1, cluster2], axis=0)
        dist matrix = dist matrix.drop([cluster1, cluster2], axis=1)
```

```
n -= 1
        print(dist matrix)
        print("")
# Perform single linkage clustering
print("Single Linkage Clustering:")
single linkage(dist.copy())
Single Linkage Clustering:
Merging clusters P4 and P9 with distance 0.05
                                                          P6
                                                                    P7
                          P2
                                               P5
               Ρ1
                                     P3
P8 \
P1
         0.000000
                    0.788923
                              0.614003
                                        0.420119
                                                   0.344819
                                                              0.396611
0.760592
         0.788923
                    0.000000
                              0.192354
                                         0.485489
                                                   0.866083
                                                              0.862844
P2
0.120416
P3
                    0.192354
                              0.000000
                                         0.386394
                                                   0.742496
                                                              0.750267
         0.614003
0.148661
P5
                    0.485489
         0.420119
                              0.386394
                                         0.000000
                                                   0.382884
                                                              0.377359
0.518652
P6
         0.344819
                    0.866083
                              0.742496
                                         0.382884
                                                   0.000000
                                                              0.058310
0.885889
P7
         0.396611
                    0.862844
                              0.750267
                                         0.377359
                                                   0.058310
                                                              0.000000
0.890505
P8
         0.760592
                    0.120416
                              0.148661
                                         0.518652
                                                   0.885889
                                                              0.890505
0.000000
                    0.440114
P10
         0.520096
                              0.381182
                                         0.100000
                                                   0.454533
                                                              0.438634
0.494975
(P4, P9)
         0.447772
                    0.461736
                              0.278927
                                         0.483735
                                                   0.710070
                                                              0.741080
0.372156
              P10
                     (P4, P9)
P1
         0.520096
                    0.447772
P2
         0.440114
                    0.461736
Р3
         0.381182
                    0.278927
P5
         0.100000
                    0.483735
P6
         0.454533
                    0.710070
P7
         0.438634
                    0.741080
P8
         0.494975
                    0.372156
         0.000000
P10
                    0.540370
(P4, P9)
         0.540370
                    0.000000
Merging clusters P6 and P7 with distance 0.058309518948452994
               P1
                          P2
                                     P3
                                               P5
                                                          P8
                                                                   P10
(P4, P9)
P1
         0.000000
                    0.788923
                              0.614003
                                        0.420119
                                                   0.760592
                                                              0.520096
0.447772
P2
         0.788923
                    0.000000
                              0.192354
                                        0.485489
                                                   0.120416
                                                              0.440114
```

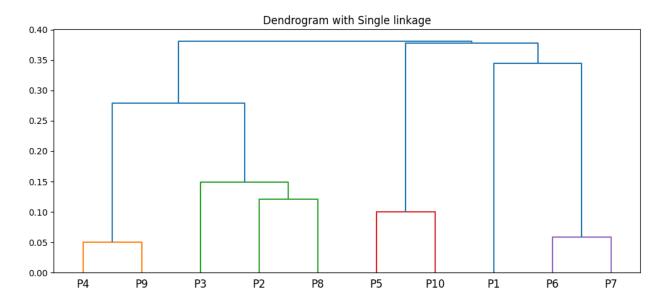
```
0.461736
                   0.192354
                              0.000000
                                        0.386394
                                                  0.148661
P3
         0.614003
                                                             0.381182
0.278927
P5
         0.420119
                   0.485489
                              0.386394
                                        0.000000
                                                  0.518652
                                                             0.100000
0.483735
         0.760592
                   0.120416
                              0.148661
                                        0.518652
                                                  0.000000
                                                             0.494975
P8
0.372156
                   0.440114
                              0.381182
                                        0.100000
P10
         0.520096
                                                  0.494975
                                                             0.000000
0.540370
(P4, P9)
         0.447772
                   0.461736
                              0.278927
                                        0.483735
                                                  0.372156
                                                             0.540370
0.000000
(P6, P7)
         0.344819
                   0.862844
                              0.742496 0.377359
                                                  0.885889
                                                             0.438634
0.710070
          (P6,P7)
P1
         0.344819
P2
         0.862844
P3
         0.742496
P5
         0.377359
         0.885889
P8
P10
         0.438634
(P4, P9)
         0.710070
(P6, P7)
         0.000000
Merging clusters P5 and P10 with distance 0.099999999999998
                Ρ1
                           P2
                                     Р3
                                               Р8
                                                     (P4, P9)
                                                               (P6,P7)
(P5, P10)
P1
          0.000000
                    0.788923
                               0.614003
                                         0.760592
                                                   0.447772
                                                              0.344819
0.420119
                    0.000000
                               0.192354
                                         0.120416 0.461736
P2
          0.788923
                                                              0.862844
0.440114
P3
          0.614003
                    0.192354
                               0.000000
                                         0.148661
                                                   0.278927
                                                              0.742496
0.381182
P8
          0.760592
                    0.120416
                               0.148661
                                         0.000000
                                                   0.372156
                                                              0.885889
0.494975
(P4, P9)
          0.447772 0.461736 0.278927
                                         0.372156 0.000000
                                                              0.710070
0.483735
(P6, P7)
          0.344819
                    0.862844
                               0.742496
                                         0.885889
                                                   0.710070
                                                              0.000000
0.377359
(P5, P10)
          0.420119
                    0.440114
                              0.381182
                                         0.494975
                                                   0.483735
                                                              0.377359
0.000000
Merging clusters P2 and P8 with distance 0.1204159457879229
                                                               (P2,P8)
                P1
                           P3
                                (P4, P9)
                                          (P6, P7)
                                                    (P5, P10)
P1
          0.000000
                               0.447772
                    0.614003
                                         0.344819
                                                   0.420119
                                                              0.760592
P3
          0.614003
                    0.000000
                               0.278927
                                         0.742496
                                                   0.381182
                                                              0.148661
          0.447772
                                                   0.483735
(P4, P9)
                    0.278927
                               0.000000
                                         0.710070
                                                              0.372156
(P6, P7)
          0.344819
                    0.742496
                               0.710070
                                         0.000000
                                                   0.377359
                                                              0.862844
                               0.483735
(P5, P10)
          0.420119
                    0.381182
                                         0.377359
                                                   0.000000
                                                              0.440114
(P2, P8)
          0.760592
                    0.148661
                               0.372156
                                         0.862844
                                                   0.440114
                                                              0.000000
```

```
Merging clusters P3 and (P2,P8) with distance 0.14866068747318503
                                                         (P3, (P2, P8))
                     P1
                          (P4, P9)
                                     (P6,P7)
                                              (P5, P10)
P1
              0.000000
                         0.447772
                                   0.344819
                                              0.420119
                                                             0.614003
(P4, P9)
                         0.000000
                                   0.710070
                                                             0.278927
              0.447772
                                              0.483735
(P6, P7)
              0.344819
                         0.710070
                                   0.000000
                                              0.377359
                                                             0.742496
              0.420119
                                   0.377359
                                              0.000000
                                                             0.381182
(P5, P10)
                         0.483735
(P3, (P2, P8))
              0.614003
                         0.278927
                                   0.742496
                                              0.381182
                                                             0.000000
Merging clusters (P4,P9) and (P3,(P2,P8)) with distance
0.2789265136196271
                               P1
                                    (P6, P7) (P5, P10) ((P4, P9), (P3,
(P2, P8)))
P1
                         0.000000
                                   0.344819
                                             0.420119
0.447772
(P6, P7)
                         0.344819
                                   0.000000
                                             0.377359
0.710070
(P5, P10)
                         0.420119
                                   0.377359
                                             0.000000
0.381182
((P4,P9),(P3,(P2,P8)))
                         0.447772
                                   0.710070 0.381182
0.000000
Merging clusters P1 and (P6,P7) with distance 0.34481879299133333
                         (P5, P10)
                                   ((P4,P9),(P3,(P2,P8)))
                                                             (P1, (P6, P7))
(P5, P10)
                         0.000000
                                                  0.381182
                                                                 0.377359
((P4,P9),(P3,(P2,P8)))
                         0.381182
                                                  0.000000
                                                                 0.447772
(P1, (P6, P7))
                         0.377359
                                                  0.447772
                                                                 0.000000
Merging clusters (P5,P10) and (P1,(P6,P7)) with distance
0.37735924528226417
                          ((P4,P9),(P3,(P2,P8))) ((P5,P10),(P1,
(P6, P7)))
((P4,P9),(P3,(P2,P8)))
                                         0.000000
0.381182
((P5,P10),(P1,(P6,P7)))
                                         0.381182
0.000000
Merging clusters ((P4,P9),(P3,(P2,P8))) and ((P5,P10),(P1,(P6,P7)))
with distance 0.38118237105091834
                                                    (((P4,P9),(P3,
(P2,P8))),((P5,P10),(P1,(P6,P7))))
(((P4,P9),(P3,(P2,P8))),((P5,P10),(P1,(P6,P7))))
0.0
```

Visualising the dendogram for single link clustering

```
plt.figure(figsize=(12,5))
plt.title("Dendrogram with Single linkage")
```

```
dend = shc.dendrogram(shc.linkage(data[['a', 'b']], method='single'),
labels=data.index)
```



perform complete link clustering method, the longest distance between ${\sf 2}$ clusters is considered when one or both the clusters have ${\sf 2}$ or more points

```
def complete linkage(dist matrix):
    n = len(dist matrix)
    while n > 1:
        min val = float('inf')
        min index = None
        for i in range(n):
            for j in range(i+1, n):
                if dist matrix.iloc[i, j] < min val and</pre>
dist matrix.index[i] != dist matrix.columns[j]:
                    min val = dist matrix.iloc[i, j]
                    min index = (i, j)
        if min val == float('inf'):
            break
        i, j = min index
        cluster1, cluster2 = dist matrix.index[i],
dist matrix.columns[j]
        print(f'Merging clusters {cluster1} and {cluster2} with
distance {min val}')
        new cluster = f'({cluster1}, {cluster2})'
        dist matrix[new cluster] = dist matrix[[cluster1,
cluster2]].max(axis=1)
```

```
dist matrix.loc[new cluster] = dist matrix.loc[[cluster1,
cluster2]].max(axis=0)
        dist matrix = dist matrix.drop([cluster1, cluster2], axis=0)
        dist matrix = dist matrix.drop([cluster1, cluster2], axis=1)
        n -= 1
        print(dist matrix)
        print("")
# Perform complete linkage clustering
print("Complete Linkage Clustering:")
complete linkage(dist.copy())
Complete Linkage Clustering:
Merging clusters P4 and P9 with distance 0.05
                          P2
                                                         P6
                                                                   P7
               Ρ1
                                    Р3
                                              P5
P8 \
         0.000000
                    0.788923
                              0.614003
                                        0.420119
                                                   0.344819
P1
                                                             0.396611
0.760592
                    0.000000
P2
         0.788923
                              0.192354
                                        0.485489
                                                   0.866083
                                                             0.862844
0.120416
P3
         0.614003
                   0.192354
                              0.000000
                                        0.386394
                                                   0.742496
                                                             0.750267
0.148661
P5
         0.420119
                    0.485489
                              0.386394
                                        0.000000
                                                   0.382884
                                                             0.377359
0.518652
P6
         0.344819
                   0.866083
                              0.742496
                                        0.382884
                                                   0.000000
                                                             0.058310
0.885889
P7
         0.396611
                    0.862844
                              0.750267
                                        0.377359
                                                   0.058310
                                                             0.000000
0.890505
P8
         0.760592
                   0.120416
                              0.148661
                                        0.518652
                                                   0.885889
                                                             0.890505
0.000000
         0.520096
                    0.440114
                              0.381182
                                        0.100000
                                                   0.454533
                                                             0.438634
P10
0.494975
(P4,P9)
         0.491935
                    0.500100
                              0.312570
                                        0.492443
                                                   0.741687
                                                             0.770000
0.415933
              P10
                     (P4, P9)
P1
         0.520096
                    0.491935
P2
         0.440114
                    0.500100
P3
         0.381182
                    0.312570
P5
         0.100000
                    0.492443
P6
         0.454533
                    0.741687
P7
         0.438634
                    0.770000
P8
         0.494975
                    0.415933
P10
         0.000000
                    0.540833
(P4, P9)
         0.540833
                   0.050000
Merging clusters P6 and P7 with distance 0.058309518948452994
                                               P5
                                                         P8
                                                                   P10
               Ρ1
                          P2
                                    Р3
```

```
(P4, P9)
         0.000000
                               0.614003
                                         0.420119
                                                    0.760592
P1
                    0.788923
                                                               0.520096
0.491935
P2
         0.788923
                    0.000000
                               0.192354
                                         0.485489
                                                    0.120416
                                                               0.440114
0.500100
P3
         0.614003
                    0.192354
                               0.000000
                                         0.386394
                                                    0.148661
                                                               0.381182
0.312570
P5
         0.420119
                    0.485489
                               0.386394
                                         0.000000
                                                    0.518652
                                                               0.100000
0.492443
P8
         0.760592
                    0.120416
                               0.148661
                                         0.518652
                                                    0.000000
                                                               0.494975
0.415933
P10
         0.520096
                    0.440114
                               0.381182
                                         0.100000
                                                    0.494975
                                                               0.000000
0.540833
(P4, P9)
         0.491935
                    0.500100
                               0.312570
                                         0.492443
                                                               0.540833
                                                    0.415933
0.050000
(P6, P7)
                               0.750267
         0.396611
                    0.866083
                                         0.382884
                                                    0.890505
                                                               0.454533
0.770000
          (P6,P7)
         0.396611
P1
P2
         0.866083
Р3
         0.750267
P5
         0.382884
P8
         0.890505
P10
         0.454533
(P4, P9)
         0.770000
         0.058310
(P6, P7)
Merging clusters P5 and P10 with distance 0.099999999999998
                 Ρ1
                           P2
                                      Р3
                                                 P8
                                                      (P4, P9)
                                                                 (P6,P7)
(P5, P10)
          0.000000
                     0.788923
                                0.614003
                                          0.760592
P1
                                                     0.491935
                                                                0.396611
0.520096
P2
          0.788923
                     0.000000
                                0.192354
                                          0.120416
                                                     0.500100
                                                                0.866083
0.485489
P3
          0.614003
                     0.192354
                                0.000000
                                          0.148661
                                                     0.312570
                                                               0.750267
0.386394
P8
          0.760592
                     0.120416
                                0.148661
                                          0.000000
                                                     0.415933
                                                                0.890505
0.518652
(P4, P9)
          0.491935
                     0.500100
                                0.312570
                                          0.415933
                                                     0.050000
                                                                0.770000
0.540833
(P6, P7)
          0.396611
                     0.866083
                                0.750267
                                          0.890505
                                                     0.770000
                                                                0.058310
0.454533
(P5, P10)
          0.520096
                     0.485489
                                0.386394
                                          0.518652
                                                     0.540833
                                                                0.454533
0.100000
Merging clusters P2 and P8 with distance 0.1204159457879229
                 P1
                                 (P4, P9)
                                            (P6, P7)
                                                     (P5, P10)
                            P3
                                                                 (P2,P8)
P1
          0.000000
                     0.614003
                                0.491935
                                          0.396611
                                                     0.520096
                                                                0.788923
P3
                                0.312570
          0.614003
                     0.000000
                                          0.750267
                                                     0.386394
                                                                0.192354
```

```
(P4, P9)
                     0.312570
                               0.050000
                                          0.770000
                                                               0.500100
          0.491935
                                                    0.540833
(P6, P7)
          0.396611
                     0.750267
                               0.770000
                                          0.058310
                                                    0.454533
                                                               0.890505
(P5, P10)
          0.520096
                     0.386394
                               0.540833
                                          0.454533
                                                    0.100000
                                                               0.518652
(P2, P8)
          0.788923 0.192354
                               0.500100
                                          0.890505
                                                    0.518652
                                                               0.120416
Merging clusters P3 and (P2,P8) with distance 0.1923538406167134
                          (P4, P9)
                                              (P5, P10)
                                                         (P3, (P2, P8))
                     Ρ1
                                     (P6,P7)
              0.000000
                         0.491935
P1
                                    0.396611
                                              0.520096
                                                             0.788923
(P4.P9)
                                              0.540833
              0.491935
                         0.050000
                                    0.770000
                                                             0.500100
(P6, P7)
              0.396611
                                                             0.890505
                         0.770000
                                   0.058310
                                              0.454533
(P5, P10)
              0.520096
                         0.540833
                                    0.454533
                                              0.100000
                                                             0.518652
              0.788923
                         0.500100
                                   0.890505
                                             0.518652
                                                             0.192354
(P3, (P2, P8))
Merging clusters P1 and (P6,P7) with distance 0.3966106403010388
               (P4, P9)
                                                  (P1, (P6, P7))
                         (P5, P10)
                                    (P3, (P2, P8))
(P4, P9)
              0.050000
                         0.540833
                                        0.500100
                                                       0.770000
(P5, P10)
                         0.100000
                                        0.518652
                                                       0.520096
              0.540833
(P3, (P2, P8))
              0.500100
                         0.518652
                                        0.192354
                                                       0.890505
(P1, (P6, P7)) 0.770000
                         0.520096
                                        0.890505
                                                       0.396611
Merging clusters (P4,P9) and (P3,(P2,P8)) with distance
0.5000999900019995
                         (P5, P10)
                                    (P1, (P6, P7))
                                                   ((P4,P9),(P3,(P2,P8)))
(P5, P10)
                                        0.520096
                         0.100000
                                                                 0.540833
                                        0.396611
                                                                 0.890505
(P1, (P6, P7))
                         0.520096
((P4,P9),(P3,(P2,P8)))
                         0.540833
                                        0.890505
                                                                 0.500100
Merging clusters (P5,P10) and (P1,(P6,P7)) with distance
0.5200961449578337
                          ((P4,P9),(P3,(P2,P8))) ((P5,P10),(P1,
(P6, P7)))
((P4,P9),(P3,(P2,P8)))
                                         0.500100
0.890505
((P5,P10),(P1,(P6,P7)))
                                         0.890505
0.520096
Merging clusters ((P4,P9),(P3,(P2,P8))) and ((P5,P10),(P1,(P6,P7)))
with distance 0.8905054744357274
                                                     (((P4,P9),(P3,
(P2, P8))),((P5, P10),(P1,(P6, P7))))
(((P4,P9),(P3,(P2,P8))),((P5,P10),(P1,(P6,P7))))
0.890505
```

Dendogram for complete link clustering

```
plt.figure(figsize=(12,5))
plt.title("Dendrogram with Complete linkage")
dend = shc.dendrogram(shc.linkage(data[['a', 'b']],
method='complete'), labels=data.index)
```

