

Another Design Example 15-14-12-8-0

Design a digital circuit that counts

15 - 14 - 12 - 8 - 0 back to 15

1111 - 1110 - 1100 - 1000 - 0000 back to 1111

Soln 1: Minimal flip-flops

PS NS OUT

ABC ABC Y[3~0]

000 001 1111

001 010 1110

010 011 1100

011 100 1000

100 000 0000

101 xxx xxxx

110 xxx xxxx

111 xxx xxxx

$$DA = BC$$

$$DB = BC' + B'C = B \oplus C$$

$$DC = A'C'$$

$$Y3 = A'$$

$$Y2 = A'C' + A'B'$$

$$Y1 = A'B'$$

$$Y0 = A'B'C'$$

----- Solution 2 -----

Design a digital circuit that counts $15 \rightarrow 14 \rightarrow 12 \rightarrow 8 \rightarrow 0$ then back to 15.

Use D-ff.

Soln 2: Moore, use 4-flip-flops

PS	NS
ABCD	$ABCD = \{DA, DB, DC, DD\}$
0000	1111
1000	0000
1100	1000
1110	1100
1111	1110
else	xxxx

$$DA = A' + B$$

$$DB = A' + C$$

$$DC = A' + D$$

$$DD = A'$$

$$OUT = \{QD, QC, QB, QA\}$$