# Quantum Benchmarking Of Molecular Ground-State Energy Estimation











## Khuram Shahzad <sup>1,</sup> Rosa De Felice <sup>2-3</sup> Guido Goldoni <sup>1-2</sup>

- <sup>1</sup> Department of Physics, Computer Science and Mathematics, University of Modena and Reggio Emilia, Italy
- <sup>2</sup> CNR-NANO-Istituto for Nanosciences, Modena, Italy
- <sup>3</sup> University of Southern California, Los Angeles, California, 90089, USA

#### Overview

- Ground-state energy estimation (GSEE) and excited-state energy estimation (ESEE) are at the core of predicting and controlling chemical reactions, with huge impact in various technologies.
- Classical algorithms for GSEE scale exponentially with system size and are elusive to even the most powerful supercomputers for useful system sizes.
- Hence, quantum computation (QC) emerges as a powerful alternative with a potentially linear scaling. Results of QC algorithms must be benchmarked on reliable data.
- The Variational Quantum Eigen solver (VQE) is a hybrid quantum-classical algorithm for approximating molecular ground-state energies on near-term quantum devices.
- We demonstrate VQE for methylene (CH<sub>2</sub>) and Benzene (C<sub>6</sub>H<sub>6</sub>) using quantum software and running on CPU and GPU devices. While we cannot draw conclusions on energy accuracy, we prove the GPU acceleration of VQE.

## **Electronic Configuration**

$$\hat{H} = \sum_{i=1}^{N} \left( -\frac{1}{2} \nabla_i^2 - \sum_{A} \frac{Z_A}{r_{iA}} \right) + \sum_{i < j} \frac{1}{r_{ij}}$$

1. Electronic Hamiltonian

 $\hat{H} = \sum_{pq} h_{pq} a_p^{\dagger} a_q + \frac{1}{2} \sum_{pqrs} h_{pqrs} a_p^{\dagger} a_q^{\dagger} a_r a_s$ 3. Second Quantization Hamiltonian

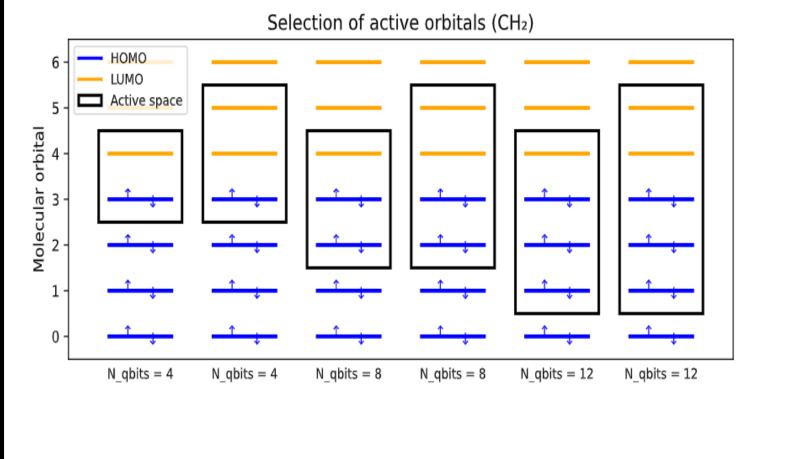
$$\Psi_{HF} = \frac{1}{\sqrt{N!}} \det[\psi_1(\mathbf{x}_1) \, \psi_2(\mathbf{x}_2) \, \cdots \, \psi_N(\mathbf{x}_N)]$$

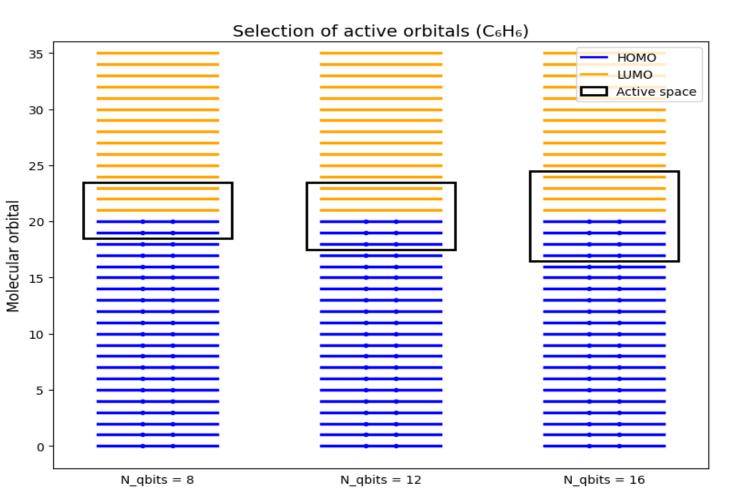
 $H^{AS} = \sum_{na}^{\text{active}} \tilde{h}_{pq} \hat{a}_p^{\dagger} \hat{a}_q + \frac{1}{2} \sum_{pqrs}^{\text{active}} g_{pqrs} \hat{a}_p^{\dagger} \hat{a}_q^{\dagger} \hat{a}_r \hat{a}_s + E_{\text{core}}$ 

2. Hartree-Fock Approximation 5. Active Space Hamiltonian

## Methodology

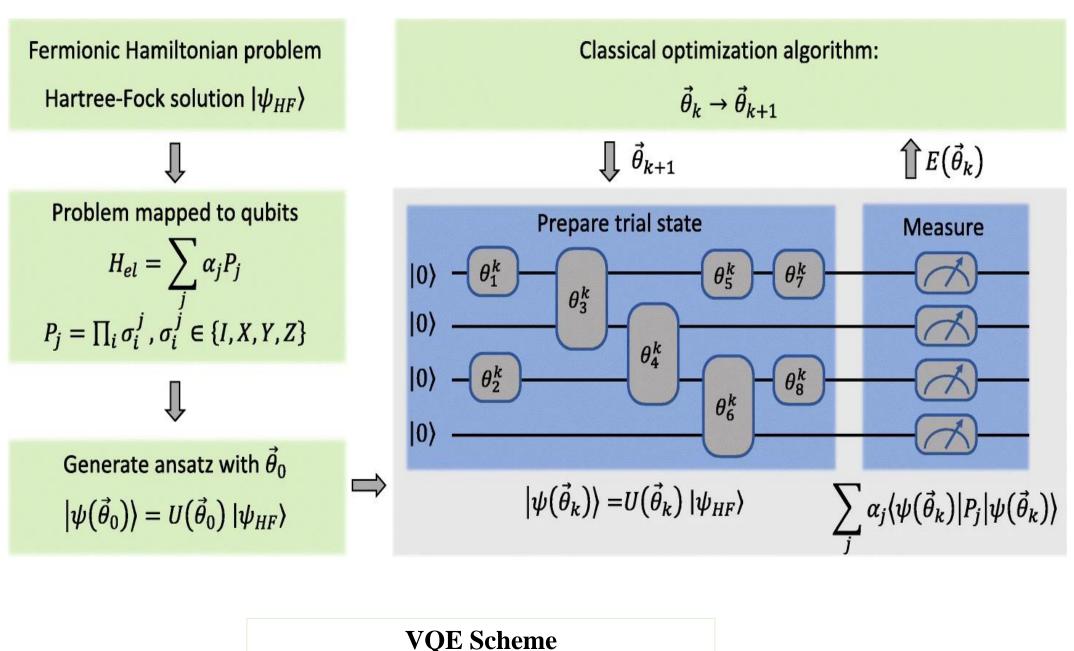
- We use the CUDA Quantum (CUDA-Q) framework, enabling simulations on both CPU and GPU backends.
- Within the chosen basis set (sto-3g) for the molecular Hamiltonian, we downsize the active space by freezing "core" orbitals and restricting the simulation to chemically relevant "reactive" orbitals, thus balancing computational cost with chemical accuracy.





The molecular Hamiltonian is constructed via PySCF and OpenFermion libraries, and the UCCSD ansatz is implemented as the variational circuit within CUDA-Q.

Overview of the Variational **Eigensolver (VQE)** Quantum workflow. electronic problem first is structure fermionic mapped operators to qubit-based Pauli operators. wavefunction is prepared using a parameterized quantum circuit (ansatz) based on the Hartree-Fock reference. Expectation values of the Hamiltonian are measured on a quantum device, and the energy is evaluated classically. A classical optimizer updates parameters iteratively hybrid energy, quantum-classical optimization loop.



We systematically evaluate energy convergence, qubit and parameter counts, and computational runtimes across various active space configurations.

#### Conclusion

- Our results show a significant acceleration in runtime for GPU based simulations compared to CPU implementations, while maintaining comparable energy accuracy within mHa differences.
- The gain increases monotonically with the size of the active space.
- The approach is generalizable to other molecular species, including open-shell molecules.

#### Methylene (CH<sub>2</sub>):

- ✓ For large active space (e.g. nele\_cas=6, norb\_cas=5), GPU can be ~30× faster than CPU.
- ✓ For small active space, the speedup is marginal or negligible.
- ✓ In one case, CPU was even slightly faster (likely due to overhead/delay in GPU scheduling or under-utilization).

#### Benzene ( $C_6H_6$ ):

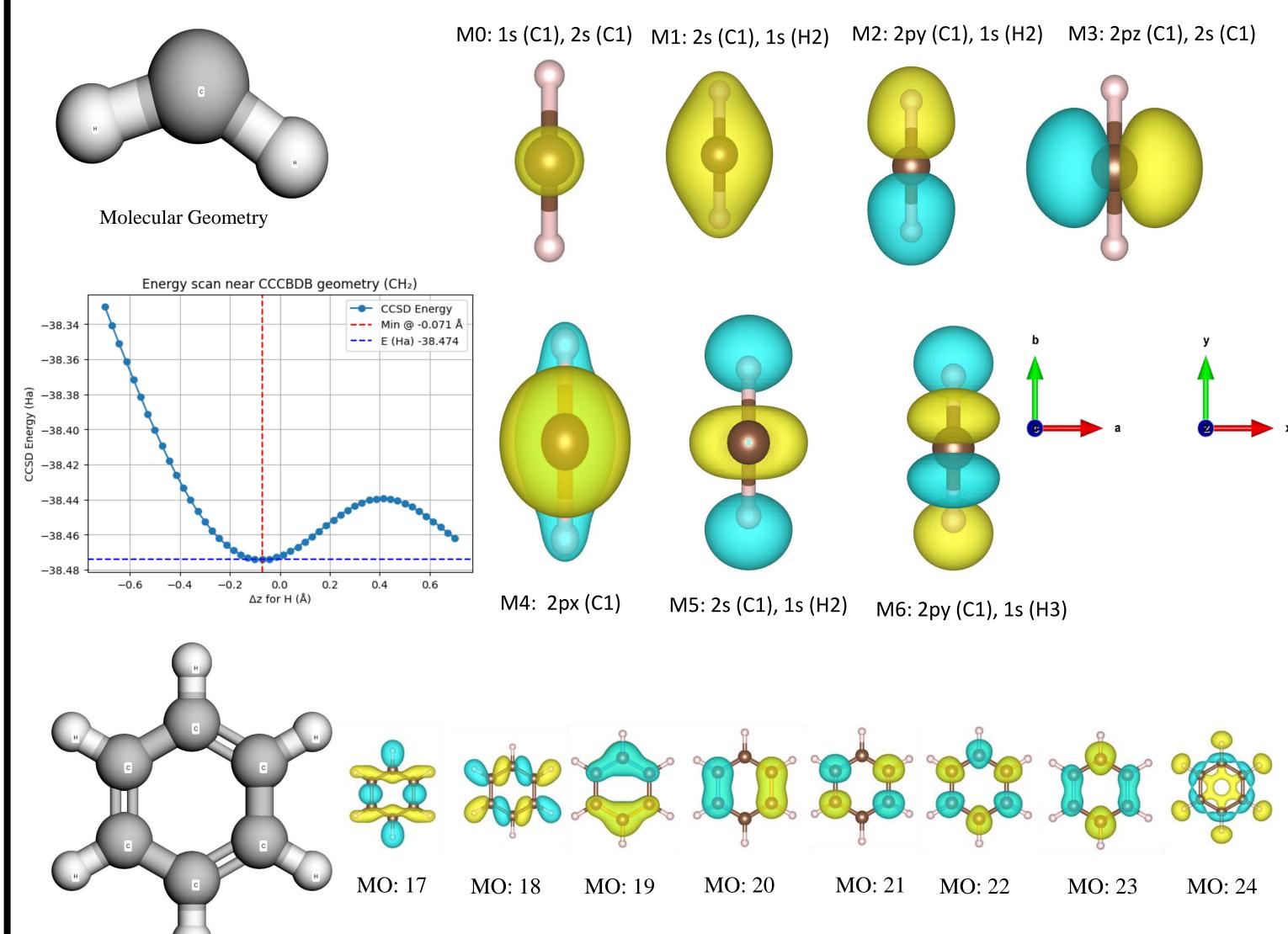
- ✓ The large active space (e.g. ncore=14, nele\_cas=14, norb\_cas=8) shows over 260× speedup, highlighting GPU superiority for large-scale quantum simulations.
- ✓ For the smallest case, GPU is still about 2.3× faster than CPU.

#### Geometry

- We take initial geometry coordinates from the Computational Chemistry Comparison and Benchmark Database (CCCBDB).
- Then we scanned more less energy near by it.

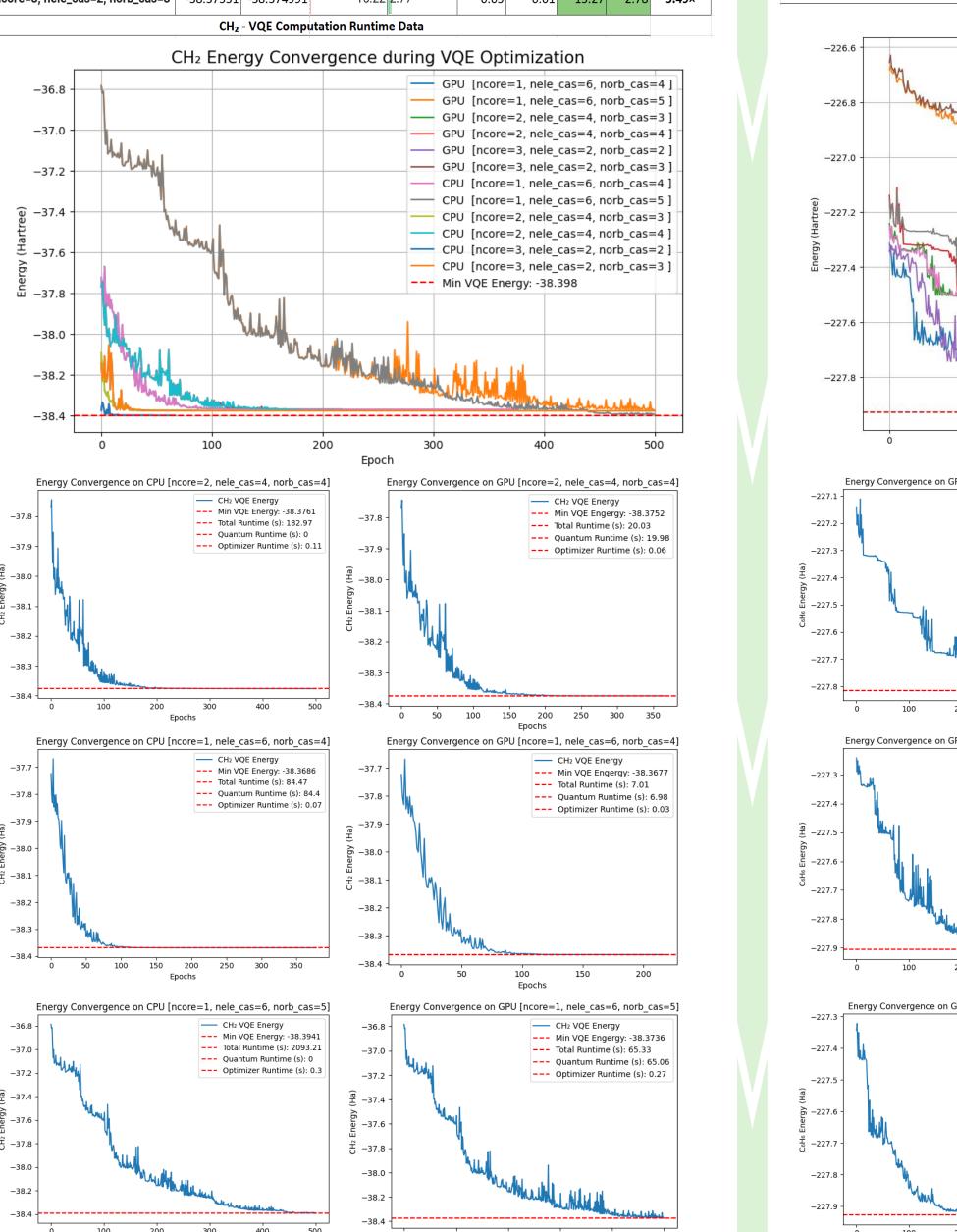
Molecular Geometry

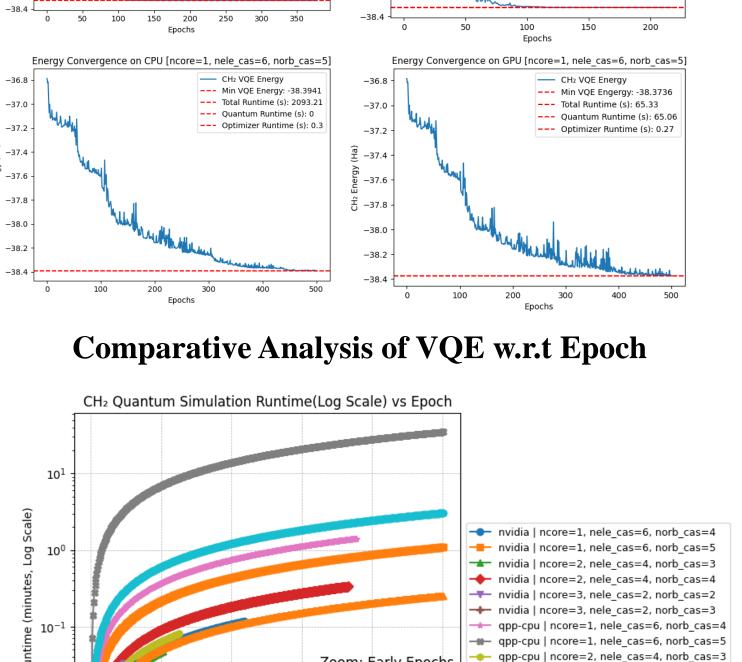
The Isosurface plot of Molecular Orbital using basis set (sto-3g).



## Result Methylene Results (CH<sub>2</sub>) Benzene Results (C<sub>6</sub>H<sub>6</sub>) C<sub>6</sub>H<sub>6</sub> - VQE Computation Runtime Data C<sub>6</sub>H<sub>6</sub> Energy Convergence during VQE Optimization CH2 Energy Convergence during VQE Optimization — CPU [ncore=18, nele cas=6, norb cas=6

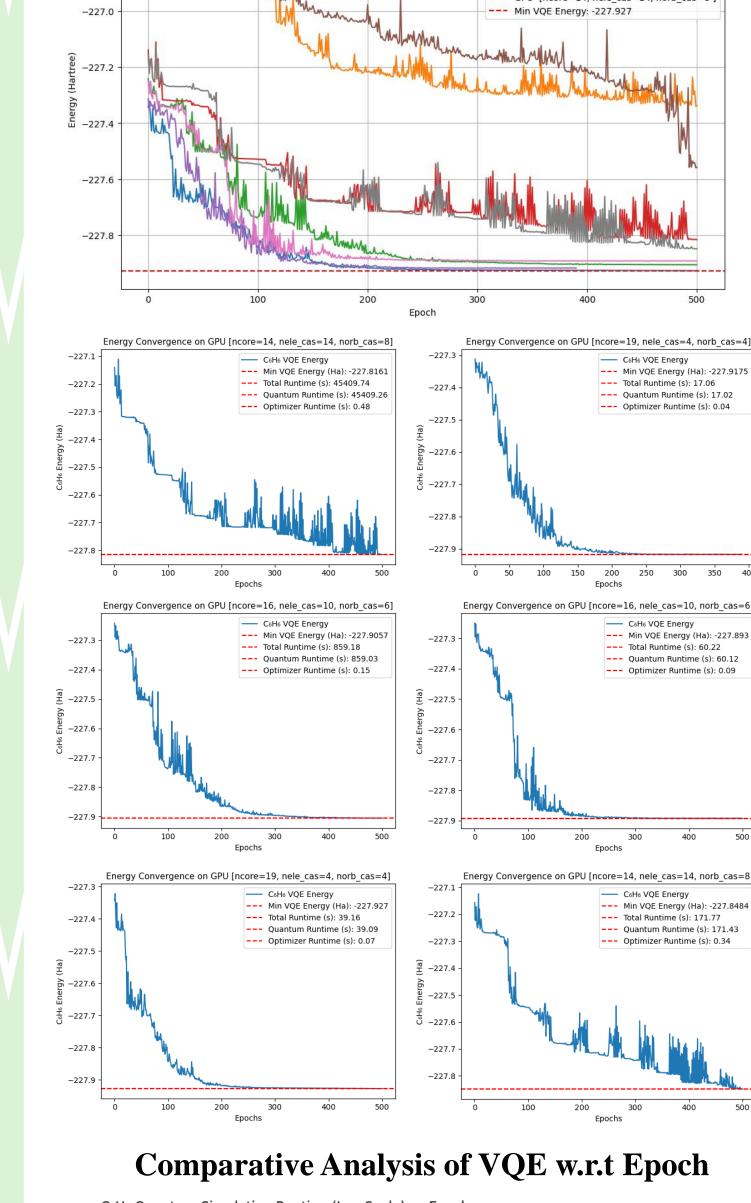
Molecular orbitals used in the active space





qpp-cpu | ncore=2, nele\_cas=4, norb\_cas=4 qpp-cpu | ncore=3, nele\_cas=2, norb\_cas=2

qpp-cpu | ncore=3, nele\_cas=2, norb\_cas=3



GPU [ncore=14 nele cas=14 norb cas=8]

### C6H6 Quantum Simulation Runtime(Log Scale) vs Epoch qpp-cpu | ncore=19, nele\_cas=4, norb\_cas=4 gpp-cpu | ncore=18, nele cas=6, norb cas=6 qpp-cpu | ncore=16, nele\_cas=10, norb\_cas=6 qpp-cpu | ncore=14, nele\_cas=14, norb\_cas=8 idia | ncore=19, nele\_cas=4, norb\_cas=4 nvidia | ncore=18, nele\_cas=6, norb\_cas=6 nvidia | ncore=16, nele\_cas=10, norb\_cas=6 - nvidia | ncore=14, nele\_cas=14, norb\_cas=8

## References